

Forecasting Emergency Department Crowding using Data Science Techniques

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Keywords: Hospital Emergency Department (ED) Predictions, Emergency Department Overcrowding, Time Series Forecasting, Neural Networks.

Abstract: The provision of insufficient resources during periods of high demand can lead to overcrowding in emergency departments. This issue has been extensively addressed through time series forecasting and regression problems. Despite the fact the increasing number of studies, accurate forecasting of demand remains a challenge. Thus, the purpose of this study was to develop a tool to predict the future evolution of emergency department occupancy in order to anticipate overcrowding episodes, avoid their negative effects on health and improve efficiency. This article presents a novel approach under the premise that the ability of the system to drain patients is the most determining factor in overcrowding episodes as opposed to previous approaches focused on patient demand. The forecasts model were based on the hourly number of patients occupying the general Emergency Department of Insular University Hospital of Gran Canaria Island, mainly given data of the flow of patients through the emergency department as well as performance indicators from other areas of the hospital extracted from the information system.

1 INTRODUCTION

The application of information technologies in healthcare during the last decade, mainly the implementation of Electronic Medical Records, has generated a large volume of health data, making this field attractive for scientific studies as corroborated by the growth in the number of scientific publications in recent years (Islam et al., 2018). Data mining is the non-trivial extraction of implicit, previously unknown information from the data. Machine learning is a branch of artificial intelligence whose goal is to give computers the ability to learn a task without being explicitly programmed to perform it. We use the term data science to include these techniques and their systematic application to face some of the current challenges of healthcare management.

Emergency departments (hereinafter referred to as ED) are an organization of healthcare professionals that offers multidisciplinary assistance, located in a specific area of the hospital to attend to emergencies and urgencies. A complete and precise definition of acute care can be found in (Hirshon et al., 2013). The aging of the population (Division, 2019), the chronic-

ity of diseases, together with the sustained increase over time in the demand for medical care, has aroused growing concern about the sustainability of the public healthcare system (Pammolli et al., 2011). This situation especially affects emergencies, which is the fastest growing medical service according to (Ministry of Health, 2017), where the provision of insufficient resources during periods of high demand can lead to overcrowding. Saturation hinders correct patient care and causes diagnostic delays, which is related to an increase in morbidity (Trzeciak and Rivers, 2003), and it also favors human error and increases mortality (Hoot and Aronsky, 2008). Anticipating overcrowding would allow us to ensure the quality of the service, as well as improves efficiency, adjusting resources to the real demand.

This problem can be analyzed from systems theory for a better understanding, trying to model the different parts of the emergency system and how changes in some of these parts affect the others. A conceptual model of (inputs, throughput, output) of overcrowding is presented in (Asplin et al., 2003) to understand its causes and develop potential solutions. The causes of overcrowding in ED have been exten-

sively studied (Derlet and Richards, 2000). Factors related to saturation can be external or internal to ED. External pressure is produced by patients visits, this is stochastic and unplanned, generating a discontinuous flow determined by multiple factors, such as working hours, meals, and days of the week. The flow also varies in holidays, social events, epidemics, climatic and atmospheric events. Internal causes include insufficient material and human resources or an inadequate physical structure. External causes are delay of radiology and laboratory tests and time required to find a bed for admitted patients (Morley et al., 2018). An internal pressure is caused by patients who remain in the department pending complementary tests, admission and discharge. The availability of beds and the resolution of complementary tests are at the same time affected by the demand for the scheduled activity. When hospital occupancy is high, these demands compete and the scheduled activity is usually prioritized.

Increases in external and internal pressure are the triggers for overcrowding. Therefore, studying the historical evolution of these patient flows and their relationship with previous episodes of overcrowding can help to predict them. It seems like a suitable problem for the application of data science techniques and methods. Measuring the moment in which overcrowding begins has been object of study, a list of proposed criteria can be found in (Boyle et al., 2011). Two of these conditions of overcrowding are the percentage of occupancy greater than 100% and the number of patients waiting for a bed greater than 10%. But it is not specified how many of these criteria are sufficient. Furthermore, these criteria should be adapted to the specific characteristics of each location. The number of patient visits or patient arrivals is mostly used as an indirect indicator of overcrowding because the service quality is significantly related to the patient demand, but as previously stated, it is only one of the factors involved. In this research we focus on the internal performance of the hospital, under the hypothesis that it has a greater impact on the overcrowding than the patients demand. Thus, we explore some variables of performance from the ED itself and from other hospital departments as independent variables and we use the number of patients occupying the ED as target variable.

This paper is organized as follows. Section 2 will review the related works. Section 3 contains the formal description of data, models and experimental settings. Section 4 presents the experimental results, section 5 the conclusion.

2 RELATED WORKS

Overcrowding in ED appears to be an universal problem (Pines et al., 2011) evidenced by the large number of recent articles that address the problem through a statistical forecasting approach. An exhaustive review is presented in (Gül and Celik, 2018) where the works are classified according to the flow of patients (inputs, throughput, output), the majority of articles focus on forecasting patient demand, other researchers have approached this problem by focusing on the characteristics of particular groups of patients, such as influenza (Araz et al., 2014) and Asthma (Ram et al., 2015). The frequent throughput objective is the forecast of the length of stays and the forecast of admissions in the case of outputs. Other application themes includes crowding, utilisation of resources, patient waiting time, ambulance diversion and inpatient admissions. Our paper does not seem to fit into one of these three categories since our target variable is related to all of them, ED occupancy increases with demand raise, in the same way when patient outflow and treatment capabilities decline.

The overcrowding of ED has been extensively addressed through time series forecasting and regression problems. Regression is a statistical process to estimate the relationships between a dependent variable called target and one or more independent continuous variables, called characteristics. These characteristics are properties of a phenomenon that is observed, overcrowding in the problem at hand. When making a prediction, new characteristic values are provided and a regression model provides an answer for the target variable.

Time series is a collection of observations measurements over time and time series forecasting using mathematical models to forecast the future values of a series based on previously observed values. Several techniques have been proposed for time series forecasting (Hamilton, 1994). These techniques can be univariate or multivariate, depending on how many variables are analyzed simultaneously. According to the desired time horizon, it can be short and long term forecasting. Finally, data can be sampled in lower or higher frequency. Time series can be decomposed into three components. The trend component is a systematic linear increasing or decreasing of the series over time. The stationary component are cycles repeated over time. The noise component are unsystematic fluctuations that cannot be explained by the model. The linear components of time series is well explained by classical time series models, unlike non-linear components. For the latter, modern machine learning techniques have been proposed.

Most researches use time series forecasting as supervised learning, using future time step as labels. Auto-regressive Integrated Moving Average (ARIMA) (Boyle et al., 2011) models and their variant SARIMA (Jones et al., 2008) are the most used. In recent years, the use of modern machine learning methods such as Artificial Neural Networks (Gul and Guneri, 2016), Support Vector Machine (Zlotnik et al., 2015), Decision Tree (Nas and Koyuncu, 2019), Random Forest, and Naive Bayes (Hertzum, 2017) has been incorporated. In recent works, some researchers explore hybrid models, which are the combination of two or more models, expecting to achieve better results comparing with the single model: (Xu et al., 2016) combines ARIMA and LR in a sequential manner, because of its ability to capture seasonal trend and effects of predictors. This model outperforms single models in terms of forecasting accuracy. (Zhang et al., 2019) use a hybrid ARIMA-SVR approach to forecast daily radiology emergency patient flow, the hybrid SARIMA-NARNN model to forecast daily number of admission inpatients is proposed by (Zhou et al., 2018). This approach has encouraged us to explore the use of new hybrid model, our proposal is to forecast the components separately and assemble the predictions and compare the results with previous proposals to evaluate their performance.

The frequency of the data collected and used for the study most used is daily, followed by monthly and hourly. Higher frequency time series usually have more seasonal patterns. Hourly data has daily, weekly, monthly and annual patterns. Some researchers have shown complications in predicting hourly patient arrivals (Wargon et al., 2009). Moreover the daily pattern of arrivals is well known and hourly data show null values. Managers use daily measurement because overcrowding episodes are not usually resolved in a few hours. However when use the census or occupation variable only hourly data has sense because occupancy can fluctuate during the day. In addition, we avoid nulls and our forecast can be more accurate.

The data collection period varied widely, from 1 year to 7 years. In most situations a larger set of training improves the results of the model. But this is not always true, it is possible that when adding older data we will incorporate noise. In some cases, noise can be easily eliminated, but in other cases there may be changes in the physical structure of the location or in the information system that produce trend fluctuations or null values. The forecast horizon ranges from 1 to 24 hours, from 1 to 30 days and from 1 to 4 months. Most forecast 1 day ahead, which seems insufficient for resource planning and to avoid over-

crowding episodes. Forecast error generally increase with the length of the forecast horizon as can be seen in (Calegari et al., 2016).

We could categorize the variables into the following groups: Calendar, Meteorological, Patient and Miscellaneous. The most used calendar variables are: weekday, month, holidays and different categories of holidays. Some works have incorporated meteorological variables such as maximum and minimum temperature, humidity, wind speed, isolation, rainfall, snowfall and pollution. Other data patient used are gender, triage level, arrival mode, diversion status, laboratory orders and radiography orders. Other miscellaneous variables are google flu trends, flue test results.

3 MATERIAL AND METHODS

For this work, we have evaluated classic time series forecasting and machine learning methods, instead of building a deterministic simulation model of the system. We will use the different variables that we can identify to train a stochastic forecasting model, which simplifies the construction of the model and we can discover new relationships and patterns in the data. As stated before, overcrowding depends on several variables, so we have faced the problem as multivariate, we have tried different time horizons and sampling frequencies. The general Emergency Department of the Insular University Hospital of Gran Canaria Island has been selected for this work. Data of the flow of patients through the ED as well as performance indicators from other areas of the hospital have been extracted from the information system.

This initial phase focuses on understanding the project objectives and requirements. The stakeholders has many competing objectives and constraints that must be considered. This stage has carried out by literature review and through interviews with the hospital managers and domain experts. As a result of these interviews, a series of improvement objectives were identified and a better understanding of the flow of patients and the care process was obtained, as well as potential features and data sources were identified. As result of the previous literature review, some research questions were established and an initial assessment of tools and techniques were performed. The major research questions we investigate are:

- What insights can be obtained from exploratory data analysis?
- Can we predict the ED occupation without using the patient demand?

- Can we obtain better results using internal hospital performance variables?
The major research objectives to achieve are:
- To develop a tool to predict the future evolution of emergency department occupancy.
- To analyze the correlation of the internal hospital performance variables with ED overcrowding.

3.1 Data Preparation

The first step was to collect the data using Extraction Transformation and Data Loading (ETL) tools. The raw data consists of 395.380 rows and 121 columns that correspond to the patients who have been treated in the ED from January 1, 2017 to March 1, 2021. As part of feature engineering process 37 features was created from raw data grouping by hour and aggregate by the average, resulting 36.933 rows and 38 columns. These features were selected to increase the predictive power of the learning algorithm, the full list of features is shown in Table 1. Some of the attention times have been approximate measured by taking the time of entry into the information system. From these features, others are derived by shifting back rows. This method, called the sliding window, is used to transform time series into supervised learning dataset. Count of patients occupying the ED (Census) is the dependent (target) variable in hourly time series format. The labels used in the supervised training were generated by shifting the census series several hours ahead, the chosen forecast horizon range was 24 to 720 hours. Rows with null values resulting from shifting were removed and the missing values were replaced with zeros. other strategies has been tested: mean, median and k-Nearest Neighbors. Finally, features was normalized by scaling each feature between 0 and 1.

Table 1: Features used in the study.

Name	Description
time	Hourly time stamps.
dayofyear	Day of the year from 1 to 365.
dayofweek	Day of the year from 1 to 7.
monthofyear	Day of the year from 1 to 12.
holiday	holiday=1, no_holiday=0.
holiday_period	Laboral=0, christmas=1, summer=2.
visits	Count of arrivals to the ED.
discharge	Count of discharges to the ED.
census	Count of patients occupying the ED.
tepcf	Minutes elapsed since the patient is admitted until the first medical consultation.

tpu	Minutes elapsed since the patient is admitted until the patient leaves the ED.
tss	Minutes elapsed since the medical discharge occurs until the patient leaves the ED.
tssh	Minutes elapsed since the medical discharge occurs until the patient is admitted to a hospital bed.
tam	Minutes elapsed since the start of the medical consultation until the medical discharge occurs.
tta	Minutes elapsed since the patient is admitted until the medical discharge occurs.
trc	Minutes elapsed since the patient is admitted until the beginning of triage.
tc	Minutes elapsed since the beginning until the end of the triage.
tpd	Minutes elapsed since the patient is admitted until the first diagnosis is made.
tea	Minutes elapsed since the beginning of the triage until the start of the first medical consultation.
tem	Minutes elapsed until enter a module.
tm	Minutes elapsed since the patient enter a module until the medical discharge occurs.
tom	Minutes elapsed since the patient enters a module until the patient leaves the ED.
age	Mean age of patients.
level1	level 1 of triage: absolute priority with immediate attention.
level2	level 2 of triage: very urgent, life-threatening situations that should not take more than 10/15 minutes.
level3	level 3 of triage: urgent but clinically stable situation, potentially life-threatening and with a maximum delay of 60 minutes.
level4	level 4 of triage: minor urgency with very low life risk and a maximum delay of 120 minutes.
census_hosp	Count of patients occupying a hospital bed.
sched_surg	Count of scheduled surgeries.
waiting_bed	Counting patients waiting for a bed.
traumatology	Patient typology.
severe_trauma	Patient typology.
cardiovascular	Patient typology.
gastrointestinal	Patient typology.
respiratory	Patient typology.
neurologic	Patient typology.
codes	Patient typology.
psycho_social	Patient typology.

3.2 Exploratory Data Analysis

Through an exploratory analysis of the data, we can understand the characteristics of the data which support the selection of appropriate model. Moreover, we can also verify our hypothesis about the causes of overcrowding, concluding if the factors are statistically significant. The tool to perform the data analysis has been Python with libraries pandas, numpy, matplotlib and seaborn. The hourly census time series shown in Fig.1 presents different patterns and high fluctuations, a significant decrease in the census can be observed during the declaration of the state of alarm and national lockdown of march 14, 2020 due to the covid-19 pandemic. Before this moment, a year stationary pattern can be recognized, for example, the census decreases in summer and increases in winter. However, the mean, the standard deviation and the distribution of values of each year are growing each year (Table 2). It could indicate that the series was non-stationary, but this is ruled out by performing the Augmented Dickey-Fuller unit root test (Dickey and Fuller, 1979) that can be seen in Table 3. The statistic test value of -13.68 is smaller than the 5% critical value of -2.86 and p-value is also smaller than significant threshold level of 0.05, so we can say the census time series is stationary and the way it changes remains constant, so it is predictable.

Table 2: Census Statistical Summary.

Time	count	mean	std	min	25%	50%	75%	max
2017	8759.0	73.0	26.0	13.0	52.0	69.0	90.0	183.0
2018	8759.0	86.0	27.0	21.0	65.0	83.0	105.0	203.0
2019	8759.0	91.0	32.0	18.0	67.0	89.0	113.0	215.0
2020	8783.0	86.0	37.0	14.0	58.0	82.0	110.0	227.0
2021	1933.0	116.0	34.0	39.0	90.0	112.0	139.0	230.0

Table 3: Results of Dickey-Fuller Test for census serie.

Test Statistic	-13.68
p-value	1.37601e-25
Lags Used	24
Number of Observations Used	36968
Critical Value (1%)	-3.43
Critical Value (5%)	-2.86
Critical Value (10%)	-2.57

The histogram of values presented in Fig.2, shows the bell curve-like shape of the Gaussian distribution with a longer right tail of outliers. Moreover, the large difference between 75th percentil and max values suggests that there are extreme values-outliers in our data set. Therefore, the data is slightly skewed to the right, and to eliminate this bias a Box-Cox power

transformation (Box and Cox, 1964) has been applied, verifying that it slightly improves the results.

A Pearson correlation among features is shown in Fig.3, Pearson's coefficient, denoted by the letter r , is the most commonly reported correlation coefficient. For non-normal distributions correlation coefficients should be calculated from the ranks of the data, not from their actual values. The closer correlation coefficient to 1 indicates a strong and positive correlation between two features and the correlation closer to 0, indicate a weak correlation. The closer coefficient to -1 also implies a strong correlation between the two series variables but in inverse way. The interpretation and the name of the correlation strength varies according to the authors and the research areas (Akoglu, 2018). We find that the correlation rates achieved by other authors are in ranges similar to ours. The p-value shows the probability that this strength may occur by chance, a statistically significant heatmap can be found in Figure 4. Therefore, there are strong correlations with level3, cardiovascular, respiratory and waiting_bed, there are moderate correlations with gastrointestinal, level2, neurologic, traumatology, census_hosp, level4, visits, level1, discharge and psycho_social. We notice a moderate inverse correlation with scheduled surgeries and day number of the week. Most of these variables have not been used before by other authors.

The census shifted ahead variables have stronger correlation with waiting_bed than visits, in addition census_hosp and visits have the same strength. This fact verifies our hypothesis about the higher influence of the hospital performance compared to external demand. Other performance variables are strongly correlated, especially patient typologies and emergency levels, we notice that cardiovascular and respiratory variables are stronger correlated than other categories, we also notice that level3 is more correlated than other more critical levels.

Time series can be analyzed through the decomposition of its time series components, hourly census decomposed by the additive model is shown in Figure 5. The Trend does not show long term positive or negative tendency in hourly frequency, however there is an annual growing trend. The Seasonal indicates a strong hourly pattern that also occurs daily, weekly and annually. Therefore, we expect that models suitable for multivariate time series with trend and multiple seasonal components will reach better results.

The ACF (Auto-Correlation Function) gives us auto-correlation measures of the series with its lagged values and PACF (Partial Auto-Correlation Function) give us auto-correlation measures of the residuals,

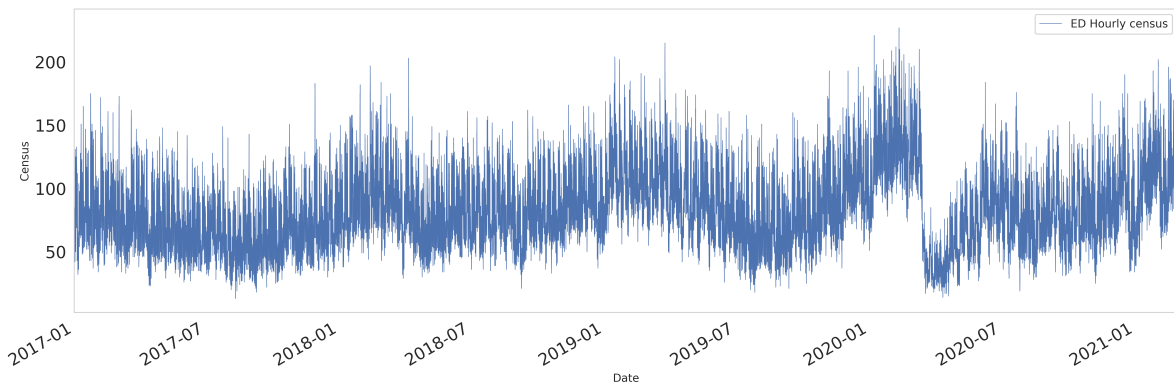


Figure 1: ED hourly census time serie.

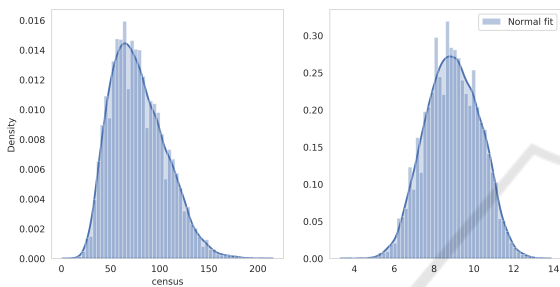


Figure 2: ED hourly census and normal fit census.

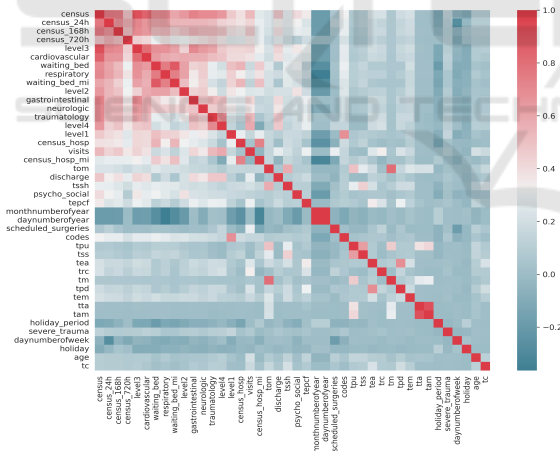


Figure 3: Correlation heatmap.

which remains after removing the seasonally and trend effects. ACF and PACF in Figure 6 show peaks that coincide with the seasonality daily period.

3.3 Experimental Design and Implementation

Several models have been selected from the literature review. The selection includes the models frequently applied in this problem, and others that have

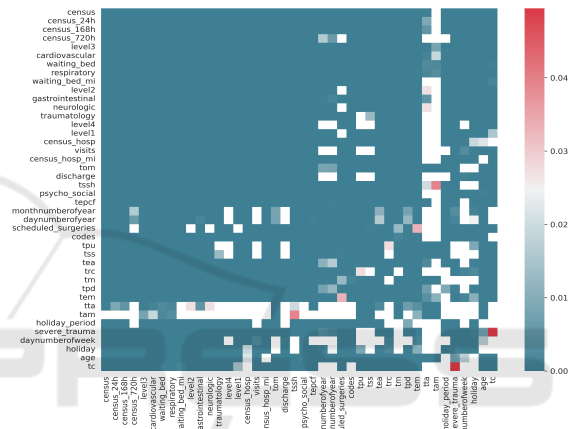


Figure 4: Statistically significant correlation.

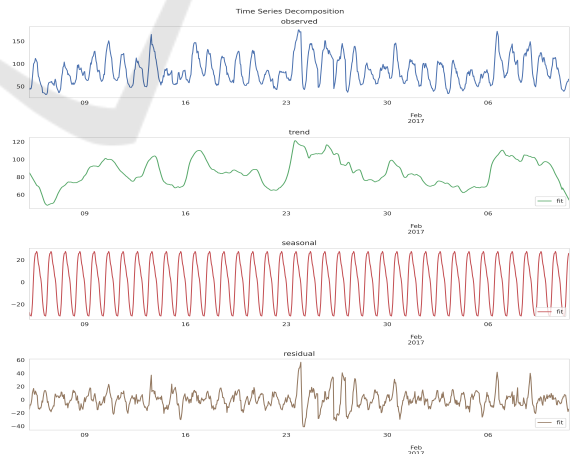


Figure 5: ED hourly census decompose.

exhibited good results applied to other forecasting and regression problems with time series. Different linear regression models have been compared to analyze the correlation of the internal hospital performance variables with ED overcrowding. Those linear meth-

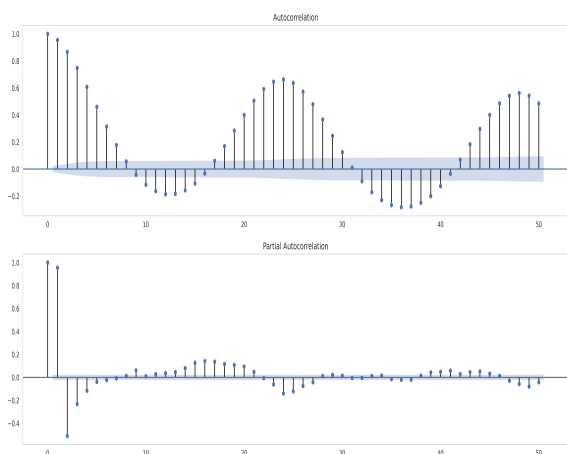


Figure 6: Auto-Correlation function.

ods are: standard linear regression (Standard), Ridge regression that includes the L2 regularization of the weights, Lasso optimization that includes the L1 regularization of the weights increasing the number of non-zero coefficients, and a combination of Ridge and Lasso named Elastic-Net that includes L1 and L2 regularization.

Before the dataset was split into training dataset (80%) and testing dataset (20%) a process of feature selection was tested to reduce the number of features by selecting the most significant. Feature selection reduces training time and can improve accuracy (Piramuthu, 2004). We have implemented feature selection through SelectFromModel method from sklearn library, a meta-transformer for selecting features based on importance weights. The selection has been made on the set of variables shown in Table 1. The inclusion in the set of the variables derived from these by the sliding window method also has been tested. All the tests we have performed of automatic feature selection have generated models with larger error scores than the exhaustive manual selection method. This means that the selection method is leaving out important variables. The set of features selected by exhaustive process is shown in Table 4. Different linear time window sizes have been tested obtaining optimal performance with 168 lags. The definitive set contains 3024 features derived from previous inputs of each of these 18 features by the sliding window method.

4 RESULTS AND DISCUSSION

To assess the performance of the methods, the following measures are the most widely used: Mean Absolute

Table 4: Features selected.

Name	Description
dayofyear	Day of the year from 1 to 365.
dayofweek	Day of the year from 1 to 7.
holiday	holiday=1, no_holiday=0.
holiday_period	Laboral=0, christmas=1, summer=2.
discharge	Count of discharges to the ED.
visits	Count of arrivals to the ED.
census	Count of patients occupying the ED.
tepcf	Minutes elapsed since the patient is admitted until the first medical consultation.
tssh	Minutes elapsed since the medical discharge occurs until the patient is admitted to a hospital bed.
trc	Minutes elapsed since the patient is admitted until the beginning of triage.
level1	level 1 of triage: absolute priority with immediate attention.
level2	level 2 of triage: very urgent, life-threatening situations that should not take more than 10/15 minutes.
level3	level 3 of triage: urgent but clinically stable situation, potentially life-threatening and with a maximum delay of 60 minutes.
level4	level 4 of triage: minor urgency with very low life risk and a maximum delay of 120 minutes.
census_hosp	Count of patients occupying a hospital bed.
waiting_bed	Counting patients waiting for a bed.
cardiovascular	Patient typology.
respiratory	Patient typology.
neurologic	Patient typology.

Percentage Error (MAPE), Root Mean Square Error (RMSE), Mean Absolute Error (MAE), and coefficient of determination (R-squared). Good accuracy is reached when the differences between the observations and the predicted values are small and unbiased. MAPE is the mean of the difference between the observations and the predicted, expressed as a percentage of the observations. Lower values indicate better model performance. It is used frequently for its easy interpretation. However, MAPE divides each error by the demand, so high errors during low-demand periods have a great impact. It is not a good measure to optimize a model because it will undershoot the demand. RMSE is the root squared mean of the squared differences between predicted and actual values. It gives more importance to the most significant errors, its version without square root MSE has been selected as regression loss function. MAE has easy interpretation and is less sensitive to outliers. R-squared is

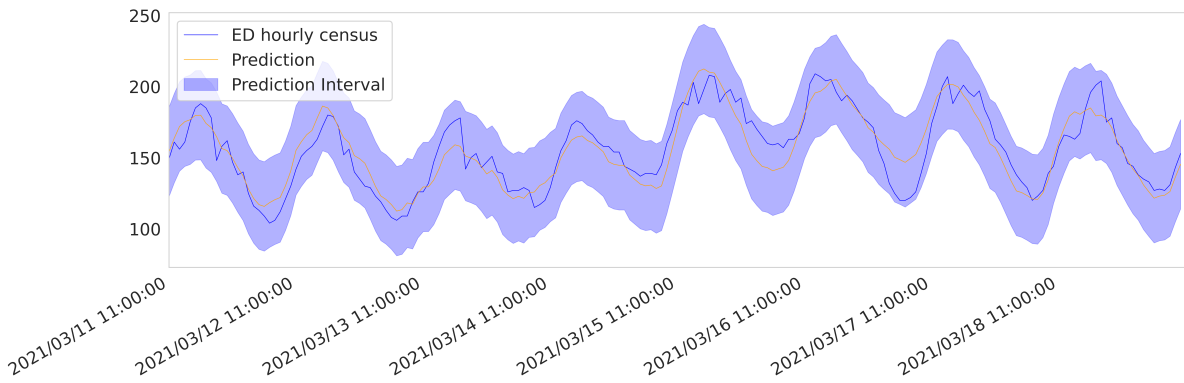


Figure 7: ED hourly census prediction 24 hours ahead with performance variables.

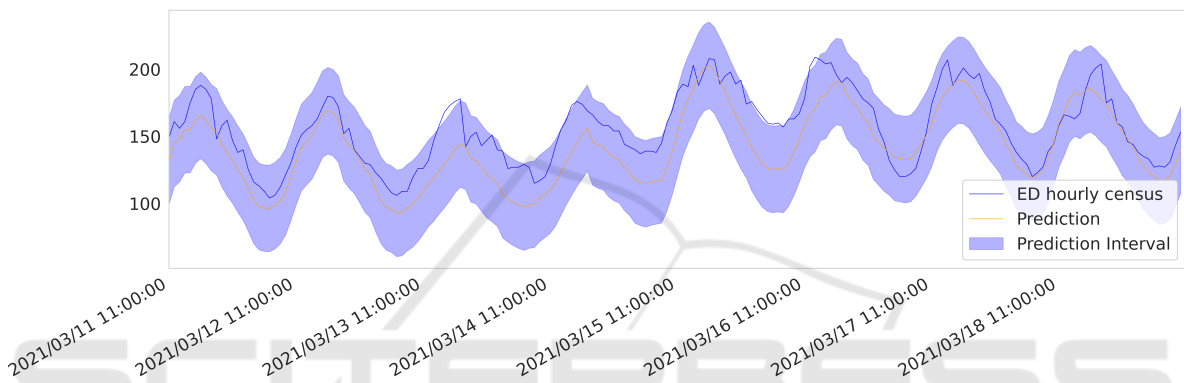


Figure 8: ED hourly census prediction 24 hours ahead without performance variables.

the percentage of explained variability by the model. Unlike the previous ones, it is unscaled and a higher R-squared value means a better model accuracy.

Table 5 shows the results obtained with the compared regression methods and it can be observed that all of them perform similarly. As expected, the forecast accuracy decreases as the time horizon go ahead. Figure 7 shows the predicted census 24 hours ahead by standard Linear Regression method and prediction interval with 95% of confidence.

To assess the significance of the internal hospital performance variables: census_hosp, waiting_bed, tepcf, tssh, and trc; an ablation study was carried out removing those variables from the model. Table 6 shows the results and it can be noted a decrease in the performance in all configurations, except for MAPE and 1-day ahead horizon, this can be seen in Figure 8, it can be observed that this model is a worse fit for the real census.

Table 5: Occupancy forecast using linear models and performance variables.

Method	Horizon	Test error		
		MAE	RMSE	MAPE R^2
Standard	1 day	12.64	15.89	12.70%0.81
	1 week	17.42	22.48	17.10%0.62
	1 month	20.86	26.72	19.52%0.46
Lasso	1 day	12.73	16.03	12.80%0.81
	1 week	17.45	22.48	17.13%0.62
	1 month	20.88	26.74	19.50%0.46
Ridge	1 day	12.64	15.89	12.70%0.81
	1 week	17.42	22.48	17.10%0.62
	1 month	20.86	26.72	19.52%0.46
ElasticNet	1 day	12.72	16.03	12.80%0.81
	1 week	17.45	22.49	17.13%0.62
	1 month	20.88	26.74	19.50%0.46

Table 6: Occupancy forecast using linear regression without performance variables.

Method	Horizon	Test error		
		MAE	RMSE	MAPE R^2
Standard	1 day	13.45	17.34	12.38%0.77
	1 week	23.90	31.04	20.88%0.27
	1 month	29.72	39.60	24.97%-0.18

5 CONCLUSIONS

We can now answer the research questions raised in section 3.

- What insights can be obtained from exploratory data analysis?: The exploratory analysis of the data shows us a higher predictive value of the internal performance variables. The dependent variable has a stronger correlation with waiting bed than visits, and census_hosp and visits have the same strength. This fact verifies our hypothesis about the higher influence of the hospital performance compared to external demand. Other variables are stronger correlated, especially patient typologies and critical levels. We notice that cardiovascular and respiratory variables are stronger correlated than other categories, we also notice that level 3 is more correlated than other more critical levels.
- Can we predict the ED occupation without using the patient demand? Although the influence of hospital performance is very important, we achieved better results by characterizing all factors related to overcrowding, both external and internal.
- Can we obtain better results using internal hospital performance variables? Definitely, incorporating the proposed variables improves the results of the ED overcrowding forecasting models. This has been confirmed with the ablation study where these variables were eliminated and the performance of the estimation decreased.

All the research objectives have been reached, the results show that ED occupation can be predicted from internal performance variables, even excluding external demand. A better understanding of the correlation of internal hospital performance variables with overcrowding in emergency departments has been reached.

The linear regression models used in the experiments are powerful enough to yield good performance but not so much complex to mask the influence of the variables in the results. Thus, they allow us to establish a baseline for future works to explore the use of different machine learning models like artificial neural networks and decisions trees. Another possible future work is to explore the use of exogenous variables.

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