

MATLAB MODELS OF ACMS IN CONTROL SYSTEMS

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Abstract: Asynchronous communication mechanisms (ACMs) are potentially useful in systems with heterogeneous timing as data connectors between processes belonging to different timing domains. In distributed, concurrent and embedded digital systems, there is often a desire to have some temporal decoupling between different parts of a system. ACMs provide a means with which concurrent processes can communicate with one another and yet still avoid synchronization. This paper describes efforts to implement MATLAB-based models of existing ACM algorithms. These techniques will facilitate the inclusion of ACMs in such application fields as distributed control and signal processing systems.

1 INTRODUCTION

Inter-process asynchrony is inevitable for computation networks in the future, firstly because different and diverse functional elements, especially those connecting to analogue domains, tend to have different timing requirements (Kelly et al 2003, Simpson 2003), and secondly because concurrent and distributed system implementations lead to greater asynchrony between components as semiconductor technology advances and the degree of integration increases (ITRS 2003 "Design" document emphasizes multiple clock domains and source-synchronous signalling and predicts networks of self-timed blocks). The size of computation networks is becoming larger, and the traffic between the processing elements is increasing. Handling the data communications which make up the traffic, therefore, may determine much of the performance and characteristics of such systems.

In truly distributed systems such as sensor networks (Kelly et al 2003, Min et al 2001)[1, 4], there is often a desire to have temporal decoupling of various kinds between digital processes. For instance, parts of a distributed control system may consist of control laws mapped onto hardware embedded into parts of the plant environment, whilst the higher hierarchies of the system may be implemented with software running in general purpose processors which are shared multitasking units. It can be very important to have temporal decoupling between these two parts of the control algorithm at the hardware level because of such reasons as avoiding deadlock propagation through

the system, the desire to have low power characteristics in remote and battery powered units, the physical impossibility of keeping everything synchronized in distributed systems, different parts of a system requiring radically different processing speeds, etc.

Asynchronous communication mechanisms (ACMs) have been investigated since the 1980s and have by now developed into a coherent field including classification, specification, and techniques for implementation, analysis and verification (Simpson 2003, Xia et al 2002). ACMs are potentially useful in systems with heterogeneous timing as data connectors between processes belonging to different timing domains, which may exist either out of necessity or desirability. They can also be useful as digital mimics for various types of data connections in analogue systems, with different types of ACMs suiting different data requirements. ACM classification was successfully expanded to include types providing more qualitative asynchrony and richer data properties than the traditional FIFO buffer. This made it clear that these applications can be envisaged. The successful work in synthesis and verification of implementations made them practical (Simpson 2003, Xia et al 2002).

An ACM, as defined here, is a connector between two asynchronous processes, a writer and a reader, through which a sequence of data items can be passed (Simpson 2003, Xia et al 2002) [2, 5]. The general scheme of these kinds of data communication mechanisms is shown in Figure 1. Most ACM implementations tend to include shared memory, accessible to both writer and reader, for the

data being transferred, and control variables, each of which is usually set by one side and read by the other.

ACMs emphasize the asynchrony between the reader and writer processes during data transfer, and are therefore especially suitable for systems of the future where multiple time domains not fully synchronized with one another predominate. ACMs can be classified into four types according to the qualitative properties of the inter-process asynchrony during data transfer as shown in Table 1.

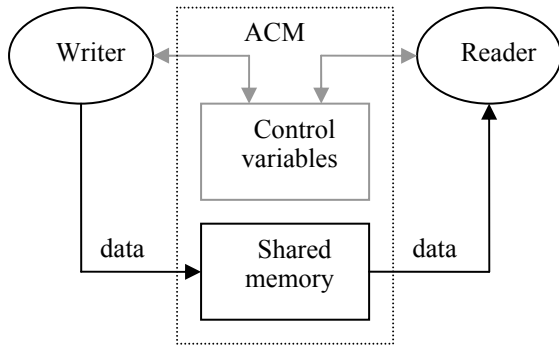


Figure 1: ACM with shared memory and possibly control variables

When discussing ACMs, we assume that the data being transferred consists of a stream of items of the same type, and the writer and reader processes are single-thread loops, during each cycle of which a single item of data is transferred to or from the ACM.

Table 1: ACM classification

| | NRR | RR |
|-----|-------|----------|
| NOW | BB | RR-BB |
| OW | OW-BB | OW-RR-BB |

In Table 1, which follows the tradition of 2x2 matrix classification schemes found in (Simpson 2003, Xia et al 2002), NRR and RR stand for non-rereading and rereading, while NOW and OW mean non-overwriting and overwriting. Whether rereading is permitted determines if the reader may be held up waiting for new data to appear in the ACM. Whether overwriting is permitted determines if the writer may be held up waiting for previous data in the ACM to be accessed by the reader. Therefore, a BB or bounded buffer without overwriting and rereading provisions, which includes most traditional inter-process data buffering schemes, may require either process to wait under certain circumstances. An RR-BB may require the writer to wait when previous data items have not been read. An OW-BB may require the reader to wait when no newer data has been made available by the writer after the previous

read. An OW-RR-BB, however, does not require either side to wait under any circumstances.

The study of ACMs so far, though extensive, has not extended to their direct modelling in application-level tools. Previous proposals for modelling ACMs at a higher level, treating them as components in larger systems, have employed Petri nets (Xia 2000). This was suitable for the case where systems containing ACMs can be regarded and analysed as general discrete event digital systems. However, in order to study the effect of including ACMs in such engineering application systems as control systems, especially when analogue parts are present, ACM models need to be integrated into popular application-level tools such as MATLAB.

2 STATEFLOW MODELS OF ACMS

MATLAB is a widely used modelling, simulation and analysis tool for engineering application systems in such fields as control, signal processing, large scale hybrid systems with analogue and discrete parts, etc. It also includes a Stateflow facility with which discrete state-transition subsystems such as ACMs can be modelled. In order to broaden the application space of ACMs, we have developed a method to model and simulate ACMs using MATLAB, based on Stateflow. The two examples in this section illustrate the method with RR-BB algorithms.

2.1 Represent Handshake in the Stateflow Model

The progress of ACM algorithms can be controlled by the writer and reader processes via request-acknowledgement handshakes. A four phase handshake protocol follows this order: sending a request, waiting for the acknowledgement sent from the other side, releasing (resetting) the request, and resetting the acknowledgement from the other side.

This can be modelled in Stateflow as shown in Figure 2. One handshake cycle is represented in the following way: a request is generated in the state entry actions (the “En” statements), which are executed when entering the state; the state itself represents waiting for the acknowledgement in the transition conditions (the conditions in the square brackets, in the case of Figure 2, ACK becoming 1), which lead to the exit from the state (end of waiting) and executions of the transitions; on exiting a state, the requests are released (in the “Ex” statements); and then the acknowledgements can be reset.

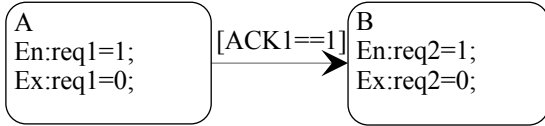


Figure 3: Handshake protocol in Stateflow

We built the Stateflow models of ACMs. based on this representation of the handshake protocol.

2.2 Global View of RR-BB ACM

A Bounded Buffer (BB) ACM can be implemented with a ring structure formed by identical memory cells (see Figure 4). One cell stores one data item at a time. The cells can be added or removed to change the size of the buffer. The two arrows in the figure indicate the reader pointer and the writer pointer. Each pointer points to the cell which is being accessed by its corresponding process. After the completion of a data access, the reader and writer pointers are moved forward according to the specific algorithm.

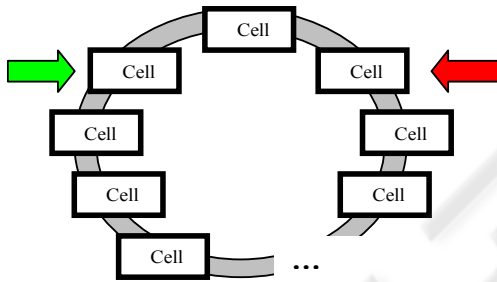


Figure 4: Ring organization of ACM buffer

If the writer cycle is much longer than that of the reader, its pointer may point to the cell immediately ahead of the reader pointer. In this case the buffer is empty, i.e. all the data items in the buffer have already been read by the reader. Conversely, if the writer cycle is much shorter than the reader cycle, its pointer will likely point to the cell just behind the reader pointer. The buffer is full in this case and none of the data items in the buffer have been read by the reader.

Rereading, if permitted, only occurs when the

var $w: 0..n+1$; $r: 0..n+1$; initialized sensibly (e.g. $r=w-1$) and initialize data in the cells.

| Writer | Reader |
|------------------------------|---------------------------------|
| wr: write cell w ; | r0: if $(r+1 \bmod n+1) \neq w$ |
| w0: $w := (w+1 \bmod n+1)$; | then $r := (r+1 \bmod n+1)$; |
| ww: wait until $r \neq w$; | rd: read cell r ; |

Figure 2: $n+2$ Cells RR-BB ACM algorithm

buffer is empty with a new read request arriving. Overwriting, if permitted, only happens when the buffer is full with a new write request coming.

The RR-BB ACM allows rereading but not overwriting. A multi-cell RR-BB algorithm is described in Figure 3.

Here n is the number of free cells which are not occupied by the pointers w and r . Therefore for this algorithm, $n+2$ is the total number of the memory cells in the ring.

The algorithm can be implemented based on the handshake protocol. For instance, each cycle of the writer part of the algorithm can be connected to the external writer process through a handshake during each cycle of operation (i.e. request from writer process to start wr, acknowledged by the writer part of the algorithm at the end of w0). This also applies to the reader side. The relationships between statements rd and wr and the cell memory can also be modelled as such handshakes. Both the writer and reader algorithm cycles have wait states from which they emerge only when the condition is correct (external request arrives and additionally in the writer's case, r becoming different from w).

Figure 5 shows the Stateflow model for the algorithm in Figure 3. In the writer, the wr statement is matched to the writing state because it handshakes with the shared memory. The w0 statement, which updates w , is mapped to the transition action after the writing state. After updating w , the write cycle is completed and the done state handshakes with the environment. The ww statement is merged into the idle state, which represents waiting for the next cycle request from the external writer, because it is also conditional waiting. The two wait conditions are "AND-ed" to produce the equivalent result.

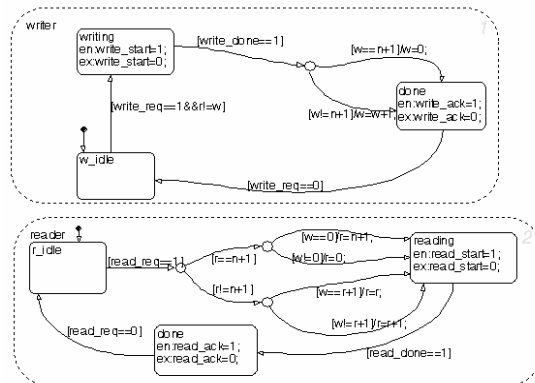


Figure 5: Stateflow Model for Algorithm in Figure 2

In the reader, what r0 does is modelled in the transition actions before the reading state. The rd statement is mapped to the reading state because of the handshake. A done state follows reading to acknowledge to the environment the completion of

the read cycle. An idle state is added at the end to wait for the next request.

The initial state in the writer part is w_idle . The writer will not become active until the write request (the request signal from the external writer wishing to start a write data access – statement wr) comes and w is not the same as r . When the writer becomes active, a $write_start$ signal is sent to the cells, in order to write the new data item to the corresponding cell. When the writer receives a $write_done$ signal from the buffer, indicating the completion of wr , it will change w to point to the next cell. Because of the ring configuration, the writer needs to check if the current cell is the one with the highest index. If it is, w will be set to 0, which is the cell with the lowest index. Otherwise, the value w will simply be incremented. After that, a $write_ack$ is sent back to the environment. Then the writer will wait for the resetting of the $write_req$ signal before going back to the w_idle state.

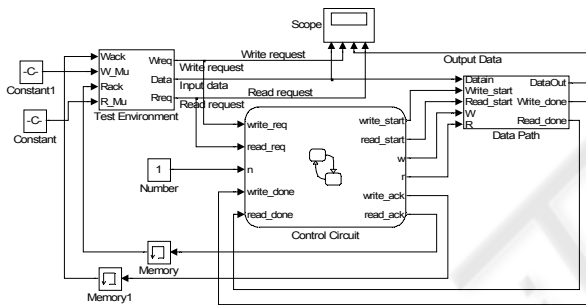


Figure 6: The Model in Figure 5 with Test Environment

The reader is similar to the writer. The initial state is r_idle . When a read request comes from the

environment, the reader will check if the next cell is occupied by the writer or not. The same $r+1 \bmod n+1$ exercise is carried out to determine the index of the next cell (either $r+1$ or 0). If the next cell is occupied by the writer, the reader pointer will remain at the current cell (for rereading). If not, the reader pointer will be moved forward according to the $r+1 \bmod n+1$ rule. Then the reader sends a $read_start$ signal to the buffer in order to read the data item in the corresponding cell. On completion of reading, the reader will receive a $read_done$ signal from the cells. A $read_ack$ is sent to the environment, and then the active state moves to the r_idle state waiting for the next $read_req$ signal.

This Stateflow model can be plugged into the Simulink environment. This is shown in Figure 7.

The test environment generates write requests, read requests and the input data items. The data path is made of memory slots (one slot per cell) to which the data items are written in and from which the data items are read out.

This ACM was simulated in this environment, with resulting waveforms shown in Figure 6. Rereading occurred when read requests came without new data items available, as in the case after the data items 4 and 5 were read (encircled in the diagram). In this simulation, n was set to 1, i.e. the total number of cells was 3. Therefore, the writer waited if two consecutive data items have not been read, as in the case after items 3 and 8 were written (encircled in the diagram).

The algorithm in Figure 3, though neat and easily understandable, is not suitable for hardware implementation. In particular, the integer control variables w and r will need many protections in order to be considered atomic. The global view nature of the indexing also means that the actual setting and reading

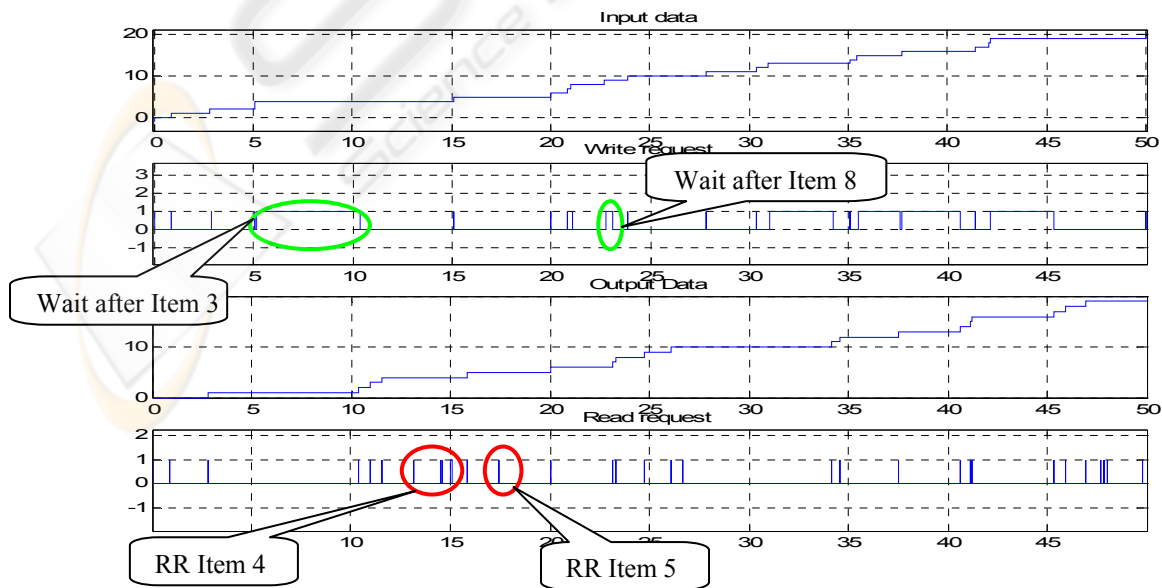


Figure 7: Simulation Waveforms for Figure 6

of these variables will include multiplexing and demultiplexing on a scale depending on the number n . The fork and join operations needed mean that an implementation of $n+3$ cells, for instance, cannot be easily built upon one of $n+2$ cells.

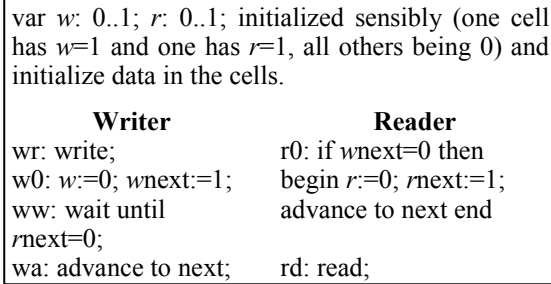


Figure 9: Modular Design RR-BB ACM Algorithm

2.3 Modular Design Model

The cellular structure of this kind of buffered ACMs suggests that it may be possible to construct a standard individual cell, complete with its own local control variables, then use n of these for an n -cell solution. This *modular design* approach is much better suited for hardware implementations.

A localized algorithm for a single cell is described in Figure 9.

The action “advancing to next cell” causes the end of execution of the current cell’s writer/reader algorithm and the beginning of the next cell’s one from wr/r0. The reader algorithm loops at the same cell until the condition $w_{next}=0$ is met. The writer will wait at a cell until the condition $r_{next}=0$ is met. Note that the writer algorithm sets both w and w_{next} and reads r_{next} , and the reader algorithm sets both r and r_{next} and reads w_{next} .

Because of the existence of the action “advance to next”, one more handshake is in the writer/reader in addition to the two mentioned in the previous algorithm. After the writer/reader has advanced to the next cell, the current one enters an idle state, and it cannot respond to external requests until the current w/r is set again (the process completing a cycle of the ring). This needs to be dealt with using an additional state in the model.

Figure 8 shows the Stateflow model of the

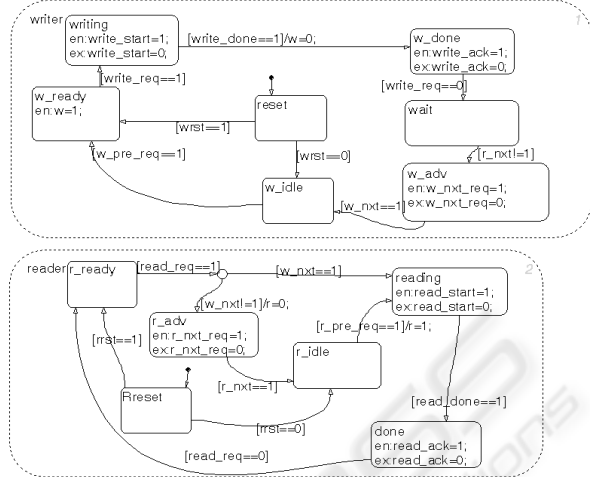


Figure 8: Stateflow model of the algorithm in Figure 9

algorithm in Figure 9. In the writer part, the wr and w0 statements were represented in Stateflow in the same way as in Figure 3. After the w_done state, a wait state is used to represent the ww statement, instead of being merged into the following state. The reasons of doing that are: 1) releasing the write request is the only condition of finishing a write cycle; 2) the only prerequisite of advance is r in the next cell having been reset. These two conditions cannot be combined together. The next statement wa was mapped to the w_adv state. w_idle and w_ready represented the two different states mentioned before.

The reader part consists of the three handshake states, the idle and the ready state.

The model worked as follows: when the write pointer points to the current cell (and with current $w=1$) and a write request comes, the writer writes the input data item into the memory of the cell. After that, w is reset to 0 and w_{next} set to 1. At this point, the write cycle is finished, a write acknowledgement is sent back to the environment. However, the writer pointer will not move to the next cell until r_{next} becomes 0.

When a read request comes, the reader firstly checks if the next cell is occupied by the writer or not (if w_{next} is 1 or not). If it is not, it moves the pointer to the next cell and does the reading.

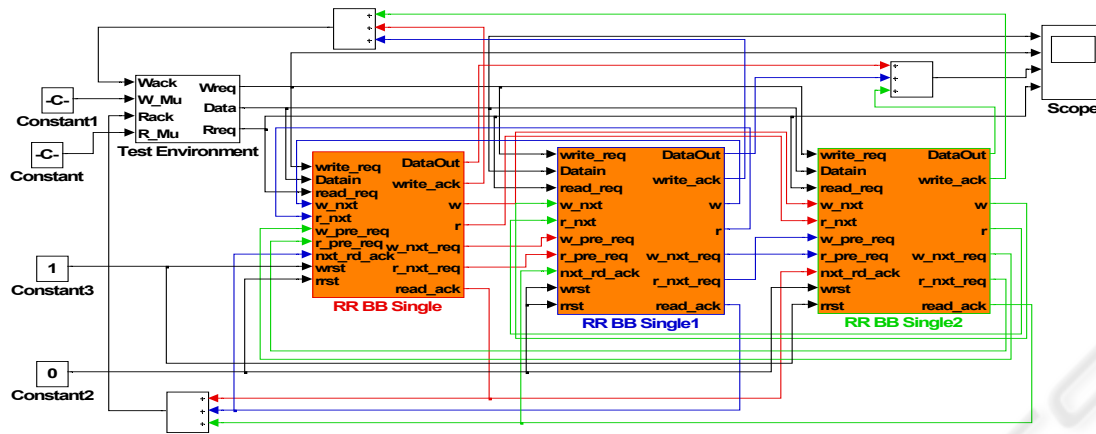


Figure 10: Modular 3 Cell RR-BB ACM Simulink model

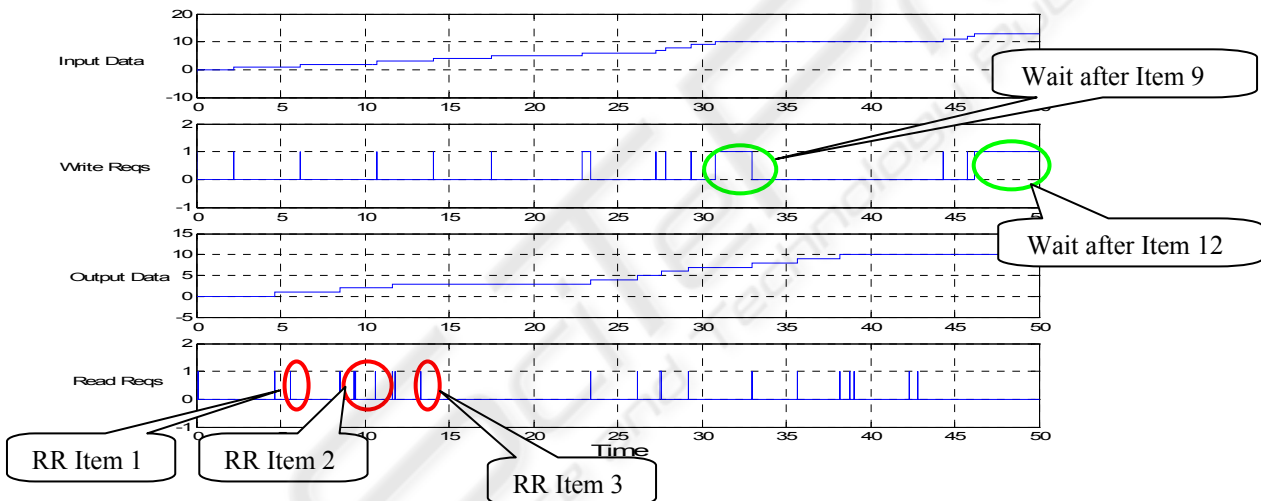


Figure 11: Simulation of the RR-BB ACM model in Figure 10

otherwise, it stays the current cell and rereads its data item.

The ready states in the Stateflow are used to initialise the position of the pointers. If the pointer moves to the current cell, the system is in the ready state, otherwise, it is in the idle state.

Consider the control flow from w_ready state to w_done state in the writer: After releasing the acknowledgement, the writer does not send the advance request until $r_nxt = 0$ (next cell is no longer accessed by the reader). When the writer receives the w -setting acknowledgement from the next cell, it releases the request, moves to the idle state, and waits for the advance request from the previous cell.

When a read request comes to the current cell, the reader sends an advance request to the next cell if it is no longer accessed by the writer (w_nxt is not 1), and goes to the idle state when r in the next cell is set. At the same time, the next cell moves the active state from idle to reading. After finishing reading, the reader sends an acknowledgement and goes back to the ready state.

The Simulink model showing connections between cells is in Figure 10. Figure 11 shows the simulation results for the model in Figure 10. Rereading occurred after data items 1, 2, 3 were read, and writer waiting happened after data items 9, 12 were written. These correspond with the properties specified for the RR-BB ACM.

3 A MOTOR CONTROL SYSTEM WITH ACM

Here we use an example application system case study to demonstrate the usefulness of these kinds of ACM models.

Figure 12 shows the basic structure of a distributed motor control system found in (Kappos et al 1990). The vC and iC blocks are the velocity and current/torque controllers, both integrated into the same ASIC in (Kappos et al 1990). The velocity and current control laws are implemented digitally.

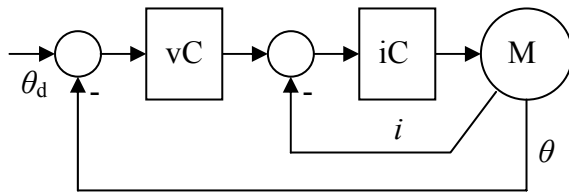


Figure 12 Schematic of dual-loop motor control system

Because of the different speed requirements (the inner loop requiring considerably faster control actions than the outer one), the digital parts of the ASIC controller were implemented in a dual-speed fashion. The link between vC and iC is in effect implemented as an analogue connection, with the digital output from vC first converted into analogue then re-sampled to provide the input for iC.

This kind of temporal decoupling is essential in these kinds of distributed systems. In motor control systems especially, if the inner and outer loops are not temporally decoupled, potential digital hazards such as deadlocks can propagate through from one loop to another. The function of the inner control loop is normally safety-critical, because even temporary failure there could have catastrophic effects such as causing the power electronic elements or fuses to fail. If such a motor is used in a safety-critical application (for instance in an aeroplane fuel pump), such failures which cannot be recovered on-line must always be avoided. As a result, the capability of the inner loop to continue functioning even when the outer loop has stopped working is of vital importance. This means that even though both vC and iC may be integrated into the same piece of silicon, they must in reality be temporally independent of each other.

Because of the difference in speed requirements for the vC and iC parts, assuming the same technology is being used to implement them in hardware, the part of the hardware where vC is implemented could have large amounts of excess computational capacity. This makes it attractive to attempt to make use of this capacity for other tasks, i.e. to effectively implement the vC part as one of

the threads in a multi-tasking processing element. This makes it possible for its progress to be affected by other factors outside the immediate control system boundary. Well-implemented operating systems such as real-time kernels may take care of the safety-critical implications of such complications by ensuring that critical threads do not wait for information from other threads.

At the basic hardware level of the data connection between the iC and vC parts of an embedded hard-wired controller chip, this kind of non-blocking communication can be implemented by using an analogue link. However, this implies an analogue/digital hybrid chip.

With ACMs, the same kind of temporal decoupling can be realized without resorting to inserting an analogue wire between two digital devices. The OW-RR-BB type ACMs, especially, mimics this function of an analogue wire perfectly. When an OW-RR-BB is “full”, the writer overwrites one of the items in it instead of waiting for a space to appear, and when it is “empty” the reader rereads the item it read during the previous cycle instead of waiting for a new item to appear. This is functionally the same as connecting the writer with the reader through a D/A and A/D converter pair, assuming perfect level-matching in the converters.

We have implemented a Stateflow OW-RR-BB ACM model using the techniques outlined in the previous section. It was then inserted into a MATLAB model of the system in Figure 12.

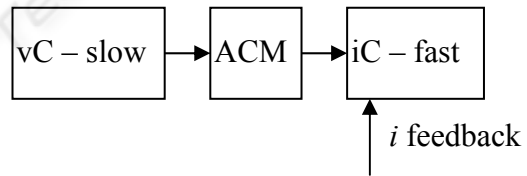


Figure 13: ACM connecting fast and slow circuits

Figure 13 shows the way in which an OW-RR-BB ACM was used to connect the fast and slow controllers in the motor control system. The iC part of the control law has a sampling frequency of 30 kHz and the vC part of the control law has a sampling frequency of 1 kHz. Our simulations with a single-cell OW-RR-BB ACM show that the reader part of the ACM reads each data item approximately 30 times, as expected, and overwriting rarely occurred. Some artificial perturbations were put into the frequencies of the clock signals going into both the vC and iC parts as a form of noise.

The simulation results were compared with results from simulating an entirely analogue version of the same system. There were no detectable differences from the output waveforms of both θ and i . This is expected because an OW-RR-BB ACM is

the digital emulation of direct analogue connection, if the latency/delay associated with the buffering can be neglected. It behaves the same as a D/A \rightarrow perfect analogue connection with delay \rightarrow A/D combination in this case. Because of the vastly faster inner loop the latency caused by the buffering associated with the single cell in the ACM is unimportant.

4 SUMMARY AND FUTURE WORK

We have developed a series of techniques with which MATLAB/Simulink models can be implemented for ACM algorithms. Initial simulation results show that these models perform as expected, i.e. the same as predicted theoretically from the algorithms.

An initial case study successfully demonstrated that these kinds of ACM models can be plugged into MATLAB models of control systems for the purpose of simulation.

MATLAB direct to hardware fast prototyping tools are becoming available (Xilinx), potentially making it possible to save the step of implementing DSP hardware through the traditional VLSI process. Future developments in this direction could potentially lead to the direct hardware implementation of application systems containing ACMS designed and verified in MATLAB. This provides another motivation for this kind of work.

Future work includes the further development of MATLAB/Simulink models for non-ACM components which would highlight the effect of the various degrees of temporal decoupling ACMS bring to systems.

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