# A VISUAL SERVOING ARCHITECTURE USING PREDICTIVE CONTROL FOR A PUMA560 ROBOT

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Abstract: A control system for a six degrees freedom Puma robot using a Visual Servoing architecture is presented. Two different predictive controllers, GPC and MPC, are used. A comparison between these two ones and the classical PI controller is performed. In this system the camera is placed on the robot's end-effector and the goal is to control the robot pose to follow a target. A control law based on features extracted from camera images is used. Simulation results show that the strategy works well and that visual servoing predictive control is faster than a PI control.

# **1 INTRODUCTION**

The controller has a crucial role in the visual servoing system performance. Most of the developed works in visual servoing systems do not take into account the dynamics of the manipulator.

The term Model Predictive Control (MPC) includes a very wide range of control techniques which make an explicit use of a process model to obtain the control signal by minimizing an objective function (Camacho 98). The MPC is formulated almost often in a state space form conceived for multivariable constrained control, Generalized Predictive Control (GPC), which was first introduced in 1987 (Clarke et al., 1987), is primarily suited for single variable and the model is presented in a polynomial form. Model Predictive control has been adopted in industry as an effective way of dealing with multivariable constrained control problems (Lee and Cooley 1997). A work developed in the field of visual servoing used a predictive controller in small displacements (Gangloff, 98). Other work compares a GPC with respect to a PID and a feedforward controller in a pan-tilt camera (Croust, 99).

To carry out this work it was created a toolbox that allows incorporating vision in the Puma control

architecture. Its great versatility, allowing the easy interconnection of different types of controllers, becomes this type of tools very advantageous. The Puma 560 model and the used 2D visual servoing architecture can be found in (Ferreira 2003). In this paper the results of a set of experiences in the area of the modelling, identification and control of a visual servoing system for a Puma 560 are presented.

This paper is organised as follows: Section 2 introduces the principles of Predictive Control (GPC and MPC) and the identification of the Puma ARMAX model. The experimental settings and the results for a PI, a GPC and a MPC controller are given in section 3. Section 4 concludes the paper and section 5 suggests the continuity of this work.

# **2 PREDICTIVE CONTROL**

#### **2.1 Generalized Predictive Control**

The basic idea of GPC is to calculate a sequence of future control signals in such a way that it minimizes a cost function defined over a prediction horizon (E.F.Camacho 1998).

The system model can be presented in the ARMAX form (Camacho 98):

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$$A(z^{-1})y(t) = B(z^{-1})u(t - T_e) + \frac{C(z^{-1})\xi(t)}{1 - z^{-1}}$$
(1)

Where  $A(z^{-1})$ ,  $B(z^{-1})$  and  $C(z^{-1})$  are the matrix parameters of transfer function H(z). To compute the output predictions is necessary to know the system model that must be controlled (Fig. 1).



Figure 1: Manipulator system block diagram controlled by vision.

The parameters used by the GPC are obtained from the configuration shown in figure 7 and the transfer function is given by:

$$H(Z) = \frac{p(z)}{\dot{p}^{*}(z)} = J_{c}F(z)J_{c}^{-1}\frac{T_{a}}{2}\frac{z+1}{z-1}\frac{1}{z} \quad (2)$$

The parameters of this function are used in predictive controller implementation.

The robot model is obtained by identifying each of the joints dynamics to obtain a six order linear model:

$$F_i(Z) = \frac{b_5 z^{-5} + b_4 z^{-4} + b_3 z^{-3} + b_2 z^{-2} + b_1 z^{-1} + b_0}{Z^{-6} + a_5 z^{-5} + a_4 z^{-4} + a_3 z^{-3} + a_2 z^{-2} + a_1 z^{-1} + a_0}$$

System Identification .In the identification procedure is used a PRBS as input signal. A prediction error method (PEM) was used to identify the Robot dynamics. The noise model  $C(z^1)$  of order 1 was selected. In this approach the identification of H(Z)(Fig.1) is performed around a reference condition. Since the robot is controlled in velocity and because the dynamics depend almost from the first joints and the displacement is small is possible to linearize the system in turn of the position q. It was also necessary to consider a diagonal inertia matrix. Assuming those conditions, is possible to consider that the Jacobian matrix is constant and therefore H(Z). This procedure is valid at low velocities. This means that the cross coupled terms are neglected.

#### **2.2 A MPC Controller**

In this approach the model used is in a space state format. The model of the plant to be controlled is described by the linear discrete-time difference equations:

$$\begin{cases} x(t+1) = Ax(t) + Bu(t), \ x(0) = x_0 \\ y(t) = Cx(t) \end{cases}$$
(3)

Where x(t) is the state, u(t) is the control input and y(t) is the output.



Figure 2: State space scheme of the manipulator controlled in velocity

In Fig. 2 is represented the scheme of a manipulator controlled in velocity. The parameters values of  $A_t$ ,  $B_t$  and  $C_t$  are obtained from the prediction error method identification algorithm and eq.3 is computed by the following definitions:

$$B = B_t J^{-1} \quad C = C_t J \quad A = A$$

The algorithm of the predictive control is:

- 1. At time t predict the output from the system,  $\hat{y}(t+k/t)$ ,  $k=N_1,N_1+1,...,N_2$ . These outputs will depend on the future control signals,  $\hat{u}(t+j/t)$ ,  $j=0,1,...,N_3$ .
- 2. Choose a criterion based on these variables and optimise with respect to  $\hat{u}(t + j/t), j = 0, 1, ..., N_3$ .
- 3. Apply  $u(t) = \hat{u}(t / t)$ .
- 4. At time t+1 go to 1 and repeat.

#### **3 EXPERIMENTAL PROCEDURE**

#### 3.1 System configuration

The implemented Visual Servoing package allows the simulation of different kind of cameras. In this particular case, it was chosen a Costar camera placed in the end-effector and positioned according with  $o_z$ axis. It was created a target of eight coplanar points that will serve as control reference. The accuracy of the camera position control in the world coordinate system was increased by the use of redundant features (Hashimoto, 1998). The centre of the target corresponds to the point with coordinates (0,0) and the remaining points are placed symmetrically in relation to this point. The target pose is referenced to the Robot base frame. In the case of servoing a trajectory, the target is remained fixed and the desired point is variable. As the primitive of the target points is obtained it is possible to estimate the operational coordinates of the camera position point.

#### 3.2 2D visual servoing with PI control

In 2D Visual Servoing the image characteristics are used to control the Robot. Images acquired by the camera are function of the end effector's position, since the camera is fixed on the end effector of the robot. They are compared with the corresponding desired images. In the present case the image characteristics are the centroids of the target points. Fig. 3 represents the model simulation of the implemented 2D visual servoing configuration. In this case CT is a PI controller.



Figure 3: Model simulation of 2D visual servoing

# 3.3 Predictive Visual servoing implementation.

In this approach our goal is also to control the relative pose of the Robot in respect to the target. The model corresponds to Fig.3 but substituting the controller – in the first case is used a GPC and in another is used a controller MPC. The target object is composed of eight coplanar points. From the projection of these points in the image frame, the estimated pose of the object in the sensor frame is computed (Gangloff 99). In both experiments all the condition and characteristics of the robot are the same. The goal is control the end effector from the image error between a current image and desire image.

# 3.4 Visual servoing control results

*PI Controller* .To eliminate the position error was chosen a PI controller considering points in operational coordinates:

$$p_i = [0.35 - 0.15 \ 0.40 \ \pi \ 0 \ \pi]^{\mathrm{T}}$$
$$p_d = [0.45 - 0.10 \ 0.40 \ \pi \ 0 \ \pi]^{\mathrm{T}}$$

The points  $p_i$  and  $p_d$  correspond to the Robot position from which the images used to control the robot are obtained. In Fig. 4 it can be observed the translation and rotation of the end-effector around  $o_x$ ,  $o_y$  and  $o_z$  axis.



Figure 4: Stabilization in a desire point using a PI.

*Predictive GPC Visual servoing control.* In this case it was used a 2D visual servoing architecture with a GPC controller. To compare the performance of this system the same initial and desire position were used.



When compared with the 2D visual servoing with a PI controller it can be seen that the GPC has a more linear trajectory and is faster for the same displacement (more displacement around the x and y axes). Figure 5 and 6 show that the rise time to PI is around 0.6s while to the GPC and MPC are 0.1s and 0.2s. The settling time is 1s for the PI, 0.3s for the GPC and 0.9s for the MPC.

*Predictive MPC Visual servoing control.* In this case it was used a MPC controller. To compare the performance of this system the same initial and desire position were used.

From Figure 6, it can be seen that the rise time for the MPC is 0.3s. The result was not so good

mainly in turn of z and for rotation of the end-effector.



Figure 6: Results of a 2D architecture using a MPC controller .

Table	1.	r m s	values	for	the	control	alg	orithm
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SSR	T <sub>x</sub>	Ty	Tz	$\theta_{\mathbf{x}}$	$\theta_{\rm y}$	$\theta_z$	error
PI	2.50	2.40	1.20	2.20	0.30	0.47	1.51
GPC	2.14	0,81	0.22	1.84	0.22	0.02	0.87
MPC	1.36	0.67	3.01	0.76	6.3	6.21	3.04

Table 1 presents the computer errors for each algorithm which reveals the best performance for the GPC.

### **4** CONCLUSIONS

A vision control system for a six degrees of freedom robot was studied.

A prediction error method was used to identify the Robot dynamics and implement a predictive control algorithm (MPC and GPC).

The controllers (PI, GPC and MPC) were used to control the robot in a 2D visual servoing architecture.

The three different algorithms always converge to the desired position. In general we can conclude that in visual servoing is obvious the good performance of both predictive controllers.

The examples show also that the 2D algorithm associated with the studied controllers allow to control larger displacements than those referred in (Gangloff 99).

From the analysis of r.m.s error presented in Table 1 we can conclude the better performance of the GPC. In spite of better MPC results for the translation in the *xy* plane when compared to the GPC, the global error is worse. These results can still eventually be improved through a refinement of the controllers parameters and of the identification procedure. In the visual servoing trajectory is obvious the good perfomance of this approach. The identification procedure has a great influence on the results. The evaluation of the graphical trajectories and the computed errors allow finally concluding that the GPC vision control algorithm leads to the best performance.

# **5 FUTURE WORKS**

In future works, another kind of controllers such as intelligent, neural and fuzzy will be used. Other algorithms to estimate the joints coordinates should be tested. These algorithms will be applied to the real robot in visual servoing path planning. Furthermore others target (no coplanars) and other visual features should be tested.

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