VISUALIZING SOFTWARE PROJECT ANALOGIES TO SUPPORT COST ESTIMATION

Martin Auer, Bernhard Graser, Stefan Biffl Institute for Software Technology Vienna University of Technology

Keywords: Software project portfolio, portfolio decisions, portfolio visualization, multidimensional scaling, analogybased cost estimation.

Abstract: Software cost estimation is a crucial task in software project portfolio decisions like start scheduling, resource allocation, or bidding. A variety of estimation methods have been proposed to support estimators. Especially the analogy-based approach—based on a project's similarities with past projects—has been re-

ported as both efficient and relatively transparent. However, its performance was typically measured automatically and the effect of human estimators' sanity checks was neglected.

Thus, this paper proposes the visualization of high-dimensional software project portfolio data using multidimensional scaling (MDS). We (i) propose data preparation steps for an MDS visualization of software portfolio data, (ii) visualize several real-world industry project portfolio data sets and quantify the achieved approximation quality to assess the feasibility, and (iii) outline the expected benefits referring to the visualized portfolios' properties.

This approach offers several promising benefits by enhancing portfolio data understanding and by providing intuitive means for estimators to assess an estimate's plausibility.

1 INTRODUCTION

Cost and effort estimation (Jones, 1998; Boehm, 1981; Conte et al., 1986) is a ubiquitous task in software project environments, which are typically multi-project environments or *software project portfolios*. High-quality estimates are fundamental to stakeholders—success-critical project participants like project and portfolio managers, as well as quality managers—in making a variety of prominent software project portfolio decisions, for example, in the quotation phase and bidding process, in resource allocation, in project start scheduling, or in risk management. Estimation quality thus greatly affects a project portfolio's performance—*high-quality estimates are vital in making portfolio decisions*.

Estimates are typically created in a variant of a generic estimation process depicted in figure 1 (a more detailed process is proposed by (Agarwal et al., 2001)). The process is influenced by a variety of factors (data quality, estimators' expertise, used models, portfolio environment, etc.)—yet much research effort tries to automatically assess tools' or methods' estimation performance as measured by accuracy

metrics (Shepperd and Schofield, 1997).

While yielding important insights, these approaches are not sufficient to achieve much-needed high quality estimation, for two reasons:

- The estimator's influence is not addressed. Every estimate must finally be approved by the decision maker—as (Stensrud and Myrtveit, 1998) point out—, which greatly affects the results especially in case of outliers or unlikely estimates, where the mere automatic application of estimation tools notoriously fails.
- In addition to the often-used effectiveness criteria like accuracy and reliability, many other, secondary criteria must be addressed as well. Efficiency criteria (estimation effort, learning effort), usability (both to novices and experts), transparency of the model etc. greatly affect the acceptance of cost estimation methods and processes; if not addressed properly, decision makers will not apply the proposed approaches. (Hihn and Habib-Agahi, 1991) describe how few methods are actually applied in industrial environments; (Shepperd and Schofield, 1997) indicate that some complex estimation methods



Figure 1: Estimation in portfolio decision making

ods often provide little insight on why a specific estimate is proposed, which may be a reason for their lack of acceptance.

The estimator's performance and the acceptance and transparency of the method or process are thus elementary to achieve high-quality estimates. Therefore, the presentation of the model and portfolio data to the estimator becomes fundamental. Unfortunately, people are generally not performing well at analyzing typical raw project portfolio data-high-dimensional data sets-, due to the high search effort to link the data items literally spread out in a spreadsheet format. According to (Robinson and Shapcott, 2002), the assimilation of such information is not intuitive while visualization aids the understanding. According to (Larkin and Simon, 1987), features are often more easily extracted from diagrams than from tabular or sentential representations, because some diagram types can group together related concepts, while tabular representations may store related items in separate areas, resulting in higher search efforts for linking concepts.

Standard methods to handle such high-dimensional data (like regression analysis or traditional analogybased approaches) propose estimates, but it is difficult to understand if the result can be trusted—estimators do not know how confident they can be with an estimate proposal.

To overcome these fundamental analysis and recognition difficulties, this paper aims at applying advanced visualization methods to project portfolio data. Multidimensional scaling methods are applied to visualize high-dimensional data in two or three dimensions; this way, the project portfolio data becomes understandable as the data is clustered visually, yielding an immediate aggregate overview of the portfolio. The visualization relies on the concept of similarity or analogy between projects, which can be expressed using similarity (or dissimilarity) values between the *n* projects—n(n-1)/2 values in the symmetric case—, or Minkowski distance functions on the projects' features, i. e., the data dimensions.

This paper proposes an MDS-based user interface to high-dimensional project portfolio data to support software cost estimation. It applies this approach to several real-world industry project portfolio data sets and it quantifies the MDS approximation quality. Finally, it outlines promising benefits by referring to visualized project portfolio properties.

This approach should give estimators an intuitive insight into portfolio data and exploit human cognition and pattern processing, thus achieving an effective, efficient and accepted estimation method, as well as a better understanding of the correlation between data characteristics and estimation methods' accuracies.

- People can immediately assess the structure of portfolio data, especially the clusters of similar projects—this eases identification of outliers or unusual project behavior and allows for higher estimation accuracy and reliability. In addition, an estimate's confidence can easily be determined, for example, when the project to be estimated is similar to a large, dense cluster of projects performing similarly the estimator can be confident with an analogy-based estimate proposal.
- The method is visual, the mathematical model transparent, the process fast and easy-to-learn—this should guarantee high acceptance and low estimation effort. The interactive playing with the data set—i. e., choosing subsets of the data dimensions, zooming in on particular interesting project clusters—will enhance portfolio understanding and influence portfolio measurement.

More strictly, this papers outlines expected benefits in the areas of model transparency, portfolio overview and understanding, selection of methodology, operational data handling, and estimation confidence assessment.

Section 2 refers to related work in the areas of cost estimation and MDS. Section 3 outlines the MDS approach and some quantitative criteria for assessing the approximation quality. Section 4 applies MDS to some real-world industrial project portfolio data sets. Section 5 discusses the potential benefits of the proposed visualization in the area of software cost estimation. Section 6 gives an outlook on further research directions in this field.

2 RELATED WORK

Different approaches to software effort prediction have been proposed—algorithmic models like CO-COMO 2 have been proposed by (Boehm, 1981), neural networks are used by (Boetticher, 2001), other methods rely on regression analysis (e.g., (Schroeder et al., 1986)).

Several studies compare the different approaches' performance. (Kemerer, 1987) reports potentially high error rates for COCOMO of up to 600 percent. (Briand et al., 2000) compare different cost estimation techniques. The results illustrate the importance of defining appropriate similarity measures-without them the analogy method is outperformed by other methods. (Wieczorek and Ruhe, 2002) have investigated the question whether multi-organizational data is of more value to software project cost estimation than company-specific data. Different methods like analogy, ordinary least squares (OLS) regression, and analysis of variance between groups (ANOVA) were used to predict costs for a large portfolio of multiorganizational project data. Results showed that if a company's project portfolio contains homogenous data, more accurate results can be achieved by analyzing the company's own data than by using large portfolios from external sources.

(Shepperd and Schofield, 1997) compare analogybased approaches to regression analysis. Estimation results for regression methods and analogy are compared using a jack-knifing approach: one project is taken from the portfolio, its effort is predicted based on the remaining data, then the predicted effort is compared to the project's real effort; this is repeated for all projects. The result of this experiment was that analogy outperforms regression in most circumstances.

(Myrtveit and Stensrud, 1999), however, come to a different conclusion. The authors design an environment where experienced and less experienced estimators have to estimate project effort using regression analysis or an analogy-based approach. A main result is that both regression and analogy can substantially improve an estimator's performance, but that regression analysis is not outperformed by analogy.

Several publications point out the importance of graphical representations in data mining environments (Thearling, 2001). According to (Robinson and Shapcott, 2002) the assimilation of unprepared, tabular information is not intuitive and visualization therefore aids the understanding and the extraction of features. According to (Larkin and Simon, 1987) certain features are more easily extracted from diagrams than from tabular or sentential representations as diagrams can group together related concepts more easily than tabular representations. Tables may store related items in separate areas, which results in higher

search effort to link concepts.

Joseph B. Kruskal, a psychometrist, was one of the first to work with MDS and authored many of the early publications (Kruskal, 1964a; Kruskal, 1964b; Kruskal and Wish, 1978). (Leeuw, 2001) offers a general introduction to MDS. Application fields for MDS, the different types of MDS, the different loss functions and algorithms are presented along with examples to illustrate the theoretical information. Another introductions to MDS is given (Borg and Groenen, 1996).

MDS is used in a wide field of science disciplines. (Coxon and Davies, 1982) present a collection with many of the classical MDS papers. (Clouse and Cottrell, 1996) apply MDS methods to the field of information retrieval. (Goodhill et al., 1995) use MDS for understanding brain connectivity.

Finally, early research results (Auer et al., 2003) indicate the feasibility of the proposed approach for several portfolio decisions and point out specific applications, especially cost estimation and portfolio standard compliance visualization.

3 VISUALIZING HIGH-DIMENSIONAL DATA

This section sums up the method of MDS and explains quantitative and graphical criteria for assessing its approximation quality.

MDS is a method to transform high-dimensional data to lower dimensions—usually in order to visualize it (e. g., with 2D-charts). MDS is based on the analogy or similarity of the visualized entities in this case, software projects—, which are described as a vector of attributes or features. Originating from mathematical methods in psychology, MDS is gaining popularity in different areas such as medicine and knowledge management. We describe the procedure of preparing portfolio data, as well as an MDS tool in (Auer et al., 2003).

In particular, MDS offers several advantages over other multivariate statistical methods, as it (i) supports non-continuous, i.e., ordinal, data, (ii) allows for missing values, and (iii) makes no assumptions on the underlying data's distribution. These properties match typical properties of real-world data sets well.

The remaining section describes the following steps in applying MDS:

- 1. Prepare the portfolio data by selecting or weighting the data dimensions to cluster projects using the relevant dimensions.
- 2. Compute project dissimilarities to provide the input to the MDS visualization.

- 3. Visualize the dissimilarities using dedicated MDS tools.
- 4. Quantitatively assess the approximation quality of the MDS visualization and verify if the quality is within the boundaries of the MDS literature.

Sets of objects—in this case, projects—are characterized by the *dissimilarities*, i.e., distance-like quantities. The dissimilarities are denoted as δ_{ij} and are usually defined in a $n \times n$ *dissimilarity matrix*. The importance of a dissimilarity δ_{ij} can be reflected by its *weight* w_{ij} . Distances in the lower-dimensional space \mathbb{R}^m are denoted as $d_{ij}(X)$, with the *configuration* X representing the m coordinates of n entities in the m-dimensional space.

In order to compute the project dissimilatities, usually the Euclidean distance function is applied to two projects' features, where the feature values are first normilized to [0 - 1], and $w_{ij} = 1$ (Note: in our case the features used to calculate the dissimilarity did not include the feature "effort"; this so-called *target feature* is depicted on the resulting MDS visualization). However, each feature or dimension would have the same impact on the dissimilarity, which is unlikely. One approach to weight the dimensions is to use a brute force approach to weigth all dimension combinations and to assess each combinaion's mean magnitude of relative error (MMRE) value. A special case is weighting all combinations with 0 and 1, which is equivalent of selecting dimensions.

After selecting the dimensions' weights, the dissimilarity matrix can be computed using the Euclidean distance on the project dimensions, yielding the dissimilarity matrix. Then, tools are used to iteratively transform this matrix to coordinates in the lower-dimensional space \mathbb{R}^m .

In order to assess the approximation quality of an MDS visualization, a so-called stress value can be used. It compared the values of the original dissimilarities with the lower-dimensional distances to assess the degree, to which the new distances represent the original analogies or similarities in the high-dimensional feature space.

One example of a stress value function is *Kruskal's stress-1*; it gives the quality of the representation based on the square root of the squared errors of the representation compared with the disparities, divided by the sum of the squared distances on the representation:

$$\sigma_1 = \sqrt{\frac{\sum_{i < j} w_{ij} (\delta_{ij} - d_{ij})^2}{\sum_{i < j} w_{ij} d_{ij}^2}}$$

There is no general agreement on which value is acceptable; different authors define their own criteria. According to Kruskal's rule of thumb (Kruskal, 1964a), a Kruskal stress-1 value of 0.2 reflects a poor fit between the distances and the dissimilarities, while a value of 0.1 is considered fair, 0.05 is good, 0.025 excellent and 0 is perfect.

A more detailed analysis is possible with Shepard diagrams; they visualize original project dissimilarities vs. distances in the two-dimensional graphical representation. Good approximations therefore produce almost linearly aligned data points.

4 INDUSTRIAL PORTFOLIO DATA

In this section several high-dimensional real-world project portfolio data sets available in the public domain are visualized two-dimensionally using MDS. In addition, the approximation quality is assessed quantitatively and graphically. Please refer to the references given in table 1 for the original data sources.

Data sets could have been visualized using all the given dimensions; however, several dimensions contribute little or nothing to the clustering of projects. In the first step, the original number of dimensions was thus reduced by performing a brute-force search to achieve the optimal subset of dimensions. For this task we used the tool ArchANGEL¹ to select the subset of dimensions that minimizes the mean magnitude of relative error (MMRE) measure in a jack-knifing analysis. The MMRE value indicates how good an estimation approach is likely to perform in terms of accuracy or error percentage of estimated effort, in our case, ArchANGEL's analogy-based approach. However, this error value should rather be used to compare different approaches applied to the same data set, as it highly depends on the underlying portfolio data properties. Note, that the brute-force approach searches all combinations of dimensions by weighting them with either 0 or 1. A better result could be achieved by us-0.5, 0.75, 1).

In addition, dimensions describing project length or duration were excluded as these values are unlikely to be known at time of estimation.

Table 1 gives an overview of the data sets, giving the original number of data dimensions (including the feature "effort"), the optimal number of data dimensions according to ArchANGEL's procedure of searching all possible combinations of dimensions (excluding the feature "effort"), and the resulting MMRE value.

In the second step, the standard Euclidean distance function was applied to the normalized values of the selected features to calculate the dissimilarity matrix. This was performed by a custom spreadsheet macro.

¹http://dec.bmth.ac.uk/ESERG/ANGEL.

Table 1: Visualized data sets					
Data set		Dimensions	Subset	MMRE	
Albrecht		5	4	0,635	
(Albrecht and Gaffn	ey, 1983)				
Desharnais	1	9	1	0,368	
(Desharnais, 1989)					
Desharnais	2	9	3	0,388	
(Desharnais, 1989)					
Desharnais	3	9	3	0,343	
(Desharnais, 1989)					
Kemerer		2	1	0,676	
(Kemerer, 1987)					

1.

m 1 1 1 Tr

Table 2: Stress values					
Data set	2D stress	3D stress			
Albrecht	0.051	0.019			
Desharnais 2	0.007	-			
Desharnais 3	0.021	-			

In step 3, the dissimilarities were visualized using MDS (Note: only if the number of selected dimensions was greater than 2). In this paper Addinsoft's Excel plug-in XLSTAT 6.1 and Miner3D were used.

Finally, table 2 lists the stress values of the data sets with more than two dimensions to be visualized. According to Kruskal's rule of thumb (see previous section), the given visualizations are between good and excellent with respect to the approximation to the original data; the Shepard diagrams support this impression.

Figure 2 depicts the MDS visualization of Albrecht's data set. As it can be seen, several projects (depicted in the left-hand part of the graph) are fairly different, thus distant, from the other projects. These projects (1, 2, 20) also have the highest effort values of the portfolio. The project arranged more densely on the graph's right-hand part are more similar to each other, but still contain several outliers with respect to their effort value, for example, project 5.

Figure 3 displays the Shepard diagram for this MDS visualization. It seems to support the impression of an good overall approximation quality.

Further figures (MDS visualizations of the Desharnais 2 and 3 data sets in tables 4 and 6; the respective Shepard diagrams in tables 5 and 7) are given in the appendix.

It is important to point out some limitations of the analogy-based approach and its visualization using MDS. First, the collected portfolio measurement data should be consistent. If collected by different persons using different procedures, data quality can be compromised; analysis relying on it has to fail. In our case, existing portfolio data sets were visualized, with little context information available about the data quality. Applying analogy-based approaches



Figure 2: 2D MDS visualization of Albrecht data



Figure 3: Shepard diagram of Albrecht data set

and MDS in an industrial environment would require careful data collection and verification procedures to ensure data quality.

Furthermore, some portfolios might not be suited for analogy-based analysis, especially if they comprise of mostly innovative projects, involving mainly new, unknown technology—the concept on analogy is simply not well-suited in environments dealing with singular projects.

5 DISCUSSION AND BENEFITS

Although there are many different approaches to support people in estimating software project efforts (e.g., formal models like COCOMO 2, neural networks, regression analysis, etc.), few of them are actually applied in typical industrial environments. Several reasons can be identified—software projects typically involve substantial parts with new and unknown technologies and tools; often, the relevant constraints to a development project is quality rather than effort, and deadlines can be influenced by corporate politics as much as by precise estimations; not to forget, estimation needs to rely on measurement data which is costly and time-consuming to obtain. However, one important reason is certainly that many proposed methods lack of transparency and accessibility. Especially methods like neural networks give little insight on how they reach a certain estimate and do little to foster portfolio measurement data understanding.

But even seemingly simpler methods like analogybased approaches can be improved in providing human estimators with context information. Analogybased methods rely on similarities between projects expressed as distances between high-dimensional features or attribute sets. Humans, however, are not particularly good at analyzing high-dimensional data without the aid of visualization techniques. Thus, simple tools supporting analogy-based methods like spreadsheet applications are severely delimited. Even dedicated tools like ArchANGEL offer only slightly better results-e.g., they relieve the burden of timeconsuming and error-prone tasks like normalizing the measurement data-but their result is again a list of n projects/feature sets. The degree of the projects' similarities, as well as the structure of the project clusters and thus valuable addition information is not given.

This paper proposed to enhance analogy-based approaches by visualizing high-dimensional portfolio measurement data with multidimensional scaling. In many circumstances, this is a feasible method to reproduce high-dimensional feature sets graphically; the approximation quality can be measured by the stress value. Data sets with 6 and more dimensions were visualized successfully within reasonable stress boundaries given in (Kruskal, 1964a).

The benefits of visualizing portfolio data are manifold:

- Transparency. The proposed method is straightforward and transparent; even estimators not acquainted with it immediately grasp the process and the visualizations' implications. We are aware of several instances in industrial environments where estimation was hindered by its relation to software measurement being perceived differently by various stakeholders—by applying MDS to multidimensional data, the connection between metrics and result becomes transparent, and measurement procedures are easier to agree upon. Finally, as no model configuration or difficult-to-reproduce algorithms are involved, users are far more likely to accept and apply this method in the first place.
- Overview. MDS gives the user a visualization with a high information density. It is therefore easy to gain a fast overview of a project portfolio's properties, for example, its project cluster structures and sizes. If based on the same metrics, the method allows for a fast comparison of different portfolios the portfolios' entropy properties are visualized in a highly intuitive way.

For example, while the projects in the Desharnais 2 data set form some clusters (see figure 4), the projects in the Desharnais 3 data set are less coupled.

• Methodology. Several publications comparing estimation methods indicate that no method can generally be regarded as the best one; a method's performance depends highly on the underlying portfolio data properties. Visualizing the data can help estimators to assess whether it is reasonable to apply analogy-based methods in a specific circumstance or whether a particular project cluster structure is unlikely to yield high-quality analogy-based estimates. This could happen if the project to be estimated is distant to relevant project clusters, if the nearest cluster is very small, or if the effort variance in the nearest cluster is too high. In that case, other methods, like regression analysis, could be used to overrule the analogy-based estimate.

For example, projects 6 and 10 in the Desharnais 3 data set (see figure 6) should probably not be estimated using the analogy-based approach as they are distant to the rest of the projects.

• Operation. The task of analyzing analogies in portfolio data involves identifying similar project feature sets. This can be performed fast and reliably on a visual representation of the data, especially as the criteria are varying (e.g., in some cases a larger cluster could be used as basis for the estimate if it is dense, while in other cases instead of a fixed number of similar projects only one or few should be used due to a portfolio's high entropy). Outliers, which can degrade the estimate's quality considerably, can be identified and removed easily-both projects that are distant to all other projects, and projects that are within a cluster but behave differently with regard to the related effort value. It would be possible to enhance conventional tools to perform similar tasks, for example, by making them configurable using threshold values for distances and cluster homogeneity, but this would make the tool far less transparent and accessible.

For example, project 5 in the Albrecht data set (see figure 2) should probably not be allowed to influence estimates of nearby projects—its high effort value should first be analyzed to decide if this is a valid project to compare other projects to.

• **Confidence**. Finally, the benefits mentioned above (method transparency and user acceptance; coarse portfolio overview and understanding; assessment of a methodology's suitability; easy data selection and manipulation) contribute to increase the confidence in a particular estimation. Usually, estimation methods were compared using accuracy and reliability measures; they did not take into account

the confidence an estimator had in its estimate at the time of estimation. The transparency of the proposed visual support is likely to increase this confidence, which should allow—in many cases—to agree on more narrow estimates.

For example, the lower right project cluster of the Desharnais 2 data set (see figure 4) seems—despite some outliers—to increase confidence in an effort estimate range between 2500 and 3500.

6 CONCLUSION AND FURTHER RESEARCH

MDS provides a transparent method to visualize highdimensional data and to analyze analogies or similarities intuitively. In this paper we propose portfolio data preparation steps for an MDS visualization of highdimensional project portfolio data, we visualize several real-world data sets and assess the achieved approximation quality, and we outline several benefits of the approach referring to concrete portfolio properties.

Main findings are that the approximation quality is within reasonable boundaries given in the MDS literature, and that cost estimation can indeed benefit substantially from MDS—specific benefits include better transparency of the analogy-based approach, a better understanding of a portfolio's data properties, thus, easier assessment of the validity of analogy-based approaches in specific circumstances, easier data handling and project selection, and finally, higher confidence in estimates.

However, many aspects have to be refined and will be addressed in future research efforts. First, weighting portfolio data dimensions using brute force could be extended from the current appoach to fine-grained weight levels. Second, user interface issues will be addressed to facilitate cluster analysis, for example, providing easy access to project cluster mean and variance values. Finally, quantitative measures for estimation confidence will be defined to assess the value of the visualization for the estimators, for instance, by weighting estimates' accuracies (post-project) with the estimators' corresponding confidence values in these estimates (pre-project).

To sum up, this and future research aims at supporting decision makers in the crucial task of cost estimation, by providing transparent and intuitive means to analyze portfolio data and assess estimates' plausibility.

REFERENCES

- Agarwal, R., Kumar, M., Yogesh, Mallick, S., Bharadwaj, R. M., and Anantwar, D. (2001). Estimating software projects. *Software Engineering Notes*, 26(4):60–7.
- Albrecht, A. J. and Gaffney, S. H. (1983). Software function, source lines of code and development effort prediction: A software science validation. *IEEE Transactions of Software Engineering*, 9(6):639–48.
- Auer, M., Graser, B., and Biffl, S. (2003). An approach to visualizing empirical software project portfolio data using multidimensional scaling. In *Proceedings of the IEEE International Conference on Information Reuse* and Integration Paper Notification (IRI 2003).
- Boehm, B. W. (1981). Software Engineering Economics. Prentice Hall.
- Boetticher, G. D. (2001). Using machine learning to predict project effort: Empirical case studies in data-starved domains. In *Proceedings of the Model Based Requirements Workshop*, pages 17–24.
- Borg, I. and Groenen, P. (1996). *Modern Multidimensional Scaling: Theory and Applications*. Springer.
- Briand, L. C., Langley, T., and Wieczorek, I. (2000). A replicated assessment and comparison of common software cost modeling techniques. In *Proceedings* of the 22nd International Conference on Software Engineering (ICSE'00), pages 4–11, Limerick, Ireland.
- Clouse, D. and Cottrell, G. (1996). Discrete multidimensional scaling. In Cottrell, G., editor, *Proceedings of the 18th Annual Conference of the Cognitive Science Society (COGSCI'96)*, pages 290–4.
- Conte, S. D., Dunsmore, H. E., and Shen, V. Y. (1986). Software Engineering Metrics and Models. Benjamin/Cummings.
- Coxon, A. and Davies, P. (1982). Key Texts in Multidimensional Scaling. Heinemann.
- Desharnais, J. M. (1989). Analyse statistique de la productivitie des projets informatique a partie de la technique des point des fonction. Master's thesis, Univ. of Montreal.
- Goodhill, G., Simmen, M., and Willshaw, D. (1995). An evaluation of the use of multidimensional scaling for understanding brain connectivity. *Philosophical Transactions of the Royal Society*, B 348:265–80.
- Hihn, J. and Habib-Agahi, H. (1991). Cost estimation of software intensive projects: A survey of current practices. In *Proceedings of the 13th International Conference on Software Engineering (ICSE'91)*, pages 276– 87.
- Jones, C. (1998). Estimating Software Costs. McGraw-Hill.
- Kemerer, C. (1987). An empirical validation of software cost estimation models. *Communications of the ACM* (*May*), pages 416–29.
- Kruskal, J. B. (1964a). Multidimensional scaling by optimizing goodness of fit to a nonmetric hypothesis. *Psychometrika*, 29(1):1–27.

- Kruskal, J. B. (1964b). Nonmetric multidimensional scaling: A numerical method. *Psychometrika*, 29(2):115– 29.
- Kruskal, J. B. and Wish, M. (1978). *Multidimensional Scaling*. Sage Publications.
- Larkin, J. and Simon, H. (1987). Why a diagram is (sometimes) worth ten thousand words. *Cognitive Science*, 11:65–99.
- Leeuw, J. D. (2001). Multidimensional scaling. In International Encyclopedia of the Social and Behavioral Sciences. Elsevier.
- Myrtveit, I. and Stensrud, E. (1999). A controlled experiment to assess the benefits of estimating with analogy and regression models. *IEEE Transactions on Software Engineering*, 25(4):510–25.
- Robinson, N. and Shapcott, M. (2002). Data mining information visualisation beyond charts and graphs. In *Proceedings of the Sixth International Conference on Information Visualisation (IV'02)*, pages 577–83.
- Schroeder, L., Sjoquist, D., and Stephan, P. (1986). Regression Analysis: An Introductory Guide. SagePublications.
- Shepperd, M. and Schofield, C. (1997). Estimating software project effort using analogies. *IEEE Transactions on Software Engineering*, 23(12):736–43.
- Stensrud, E. and Myrtveit, I. (1998). Human performance estimating with analogy and regression models: An empirical validation. In *Proceedings of the Fifth International Symposium on Software Metrics (MET-RICS'98)*, pages 205–13.
- Thearling, K. (2001). Visualising data mining models. In Information Visualisation in Data Mining and Knowledge Discovery. Morgan Kaufman.
- Wieczorek, I. and Ruhe, M. (2002). How valuable is company-specific data compared to multi-company data for software cost estimation? In *Proceedings of the Eighth International Symposium on Software Metrics (METRICS'02)*, pages 237–48.



Figure 4: 2D MDS visualization of Desharnais 2 data



Figure 5: Shepard diagram of Desharnais 2 data set



Figure 6: 2D MDS visualization of Desharnais 3 data



Figure 7: Shepard diagram of Desharnais 3 data set