

# FUZZY CLASSIFICATION BY MULTI-LAYER AVERAGING

## *An Application in Speech Recognition*

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**Abstract:** This paper intends to introduce a simple fast space-efficient linear method for a general pattern recognition problem. The presented algorithm can find the closest match for a given sample within a number of samples which has already been introduced to the system. The fact of using averaging and fuzzy numbers in this method encourages that it may be a noise resistant recognition process. As a test bed, a problem of recognition of spoken words has been set forth to this algorithm. Test data contain clean and noisy samples and results have been compared to that of a widely used speech recognition method, HMM.

## 1 INTRODUCTION

Pattern recognition is one of the oldest challenges of researchers in different areas such as artificial intelligence, interactive graphic computers and computer aided design. Different kinds of recognition can also be generalized as a pattern recognition problem. A *pattern* is an arrangement of descriptors. Therefore a wide range of problems can easily be seen as a pattern recognition problem. Considering this general view, this paper tries to demonstrate a time and space efficient yet simple approach for a pattern matching problem.

The presented algorithm can compare a given sample to a number of samples in its database and specify the closeness of each sample of database to the given one. This comparison can be served to find the closest match which can be interpreted as a recognition process. The samples used in this algorithm are generally N-dimensional arrays, but since 2D arrays are mostly the case (images, spectrograms and etc.) in pattern recognition processes, the algorithm has been developed based on such structure. The details about this issue have been discussed in next section.

For displaying the effectiveness of presented method and also for demonstrating its ability to solve practical problems, this algorithm has been applied to a speech recognition problem and tested

and compared with one of the best methods of this category, Hidden Markov Model. The flexibility of this method to noise which is one the most important concepts of speech recognition has also been tested.

The next section explains the details of the problem in hand and how the discussed general domain has been mapped to a speech recognition issue. In section 3, the steps of recognition process is explored in which the idea of *Multi-Layer Averaging* (MLA) combined with fuzzy classification is described. The complexity of the algorithm is then calculated and shown in section 4 which shows its time and space efficiency. Finally, the results and comparisons are presented in section 5.

## 2 PROBLEM SPACE

As it was mentioned, a pattern recognition problem can be a general concept. This section tries to limit the definition of the problem although it can easily be extended to more complex forms. First, a general view is established to display how this method can be applied to different areas. Then an application of this definition in recognition of a spoken word signal will be presented.

## 2.1 General View

The idea of MLA can be applied on any arrangement of numeric data with subtle adaptations. The structure used in this paper is a 2-Dimensional matrix of integer numbers. The goal is to find a match for a given sample among a number of samples which has already been introduced and analyzed by the system.

**Definition:** A *Sample* is a matrix of size  $(m \times n)$  of integer numbers.

Different samples do not necessary have the same size. However it is needed for further steps of algorithm to reduce sample data to a specified size for all samples. This reduction is done by quantization process.

Quantization process is a process which takes raw data from input source and converts these data to integer values in the form of a matrix with a predefined size. First part of quantization is converting the numbers to integer values. This can be done by a function to map the input range to a desired range so that a proper distribution of numbers is achieved.

In second part, to resize the dimensions of input data, a grid of specific size is assumed upon current data and the numbers of each block of the grid are averaged and the result will represent the value of that block. The above view has been applied to a specified case of speech recognition which is described in the following sub-section.

## 2.2 Word Recognition Problem

Speech recognition can be divided to smaller problems. The range of these problems can differ from recognition of phoneme to a word then a sentence and ultimately continuous speech. The number of speakers is also an important factor. This paper deals with the recognition of spoken words of a single speaker. The goal is to get a new sample (a spoken word in this case) from a speaker and classify it within a number of existing samples which are already acquired from the same speaker.

There are two technical assumptions considered in implementation of this algorithm. First assumption is that words are pronounced normally i.e. the relative lengths of phonemes of a word are almost equal for different pronunciations of the same

word. Second assumption is that each sample is properly clipped i.e. there are no blank or irrelevant data in the beginning and end of a sample.

Before the recognition process can be applied, it is needed for both train and test data to be converted to the format discussed in previous sub-section. To do so, spectrogram of each sample is calculated. Spectrogram is simply amplitudes of a range of frequencies in small time slices over speech signal time period.

After acquiring spectrograms of each sample, a normalization algorithm makes sure that data are converted to integer and uniformly distributed over the range of [0, 255]. The result is a matrix of integer numbers which its sizes are dependant of both length of time of the word and the size of FFT algorithm (256, 512, etc). Figure 1 shows a spectrogram of a spoken word. The horizontal axis is time and the vertical axis is frequency.

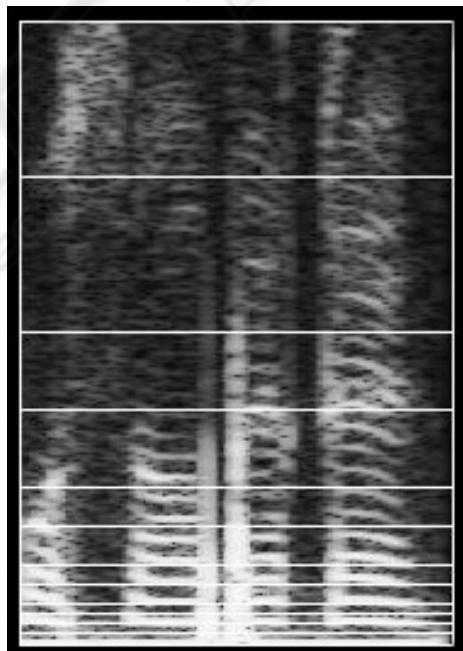


Figure 1: Spectrogram of a word.

The last step of this preprocess is averaging data of spectrograms so that all samples have equal sizes. For this reason, the spectrogram is divided to 12 frequency bands and 32 time bands. It is notable that the number of time bands should be in form of a power of 2. The reason will be explained in next section. The lengths of all time bands are equal. However the length of frequency bands differs.

Because lower frequencies contain more information than higher ones, the length of bands increases for higher frequencies. The horizontal lines displayed in figure 1 separate frequency bands.

Intersection of a frequency band and a time band creates a block. After averaging the data of each block, a matrix of  $(32 \times 12)$  is achieved for each sample. These matrices are fit to be dealt by recognition process. The idea of averaging is used for correcting probable noises and displacements. In the next section, the MLA algorithm is used to recognize test samples which are also converted to matrices of above size and format.

### 3 RECOGNITION PROCESS

The main idea of MLA for matching a sample within a group is to eventually eliminate non-similar samples by giving them a penalty so that the best match which is the most similar sample remains with least penalty. In order to accomplish this goal, the following fact is used: if two series of numbers are almost similar their averages are also similar. In other words, if averages of two series of numbers are not similar, those series are not similar either (however the reverse is not true). Therefore this dissimilarity can be used to eliminate samples.

#### 3.1 Multi-Layer Averaging

Using the idea introduced above, MLA tries to iteratively give penalty points to samples by comparing their averages. The comparison is done in different layers. The following steps explain the algorithms. The sample to be recognized is called

"Test Sample" and the sample from database of system upon which test sample is checked is called "Matching Sample"

Step 1: Choose a matching sample from database. Set its penalty point to zero.

Step 2: Set the number of averages ( $N_a$ ) in first layer to 1. Each of two samples should have C members which should be a power of 2.

Step 3: Define variable M as  $C / N_a$ . Average every M members of both test and matching samples which results in  $N_a$  numbers for each samples. Call them  $A_i$  and  $B_i$  for which  $1 \leq i \leq N_a$ .

Step 4: Compare each average of test sample ( $A_i$ ) to its corresponding average in matching sample ( $B_i$ ). Add a penalty point to the points of matching sample according to comparison method.

Step 5: Multiply  $N_a$  by 2 for next layer. If  $N_a$  is not larger than C go to step 3.

Step 6: If there are any remaining sample in database go to step 1. Otherwise, sort matching samples ascending based on their penalty points. Return first sample in the list as answer.

The penalty point in step 4 can be defined differently to achieve better results. It can simply be average of all of differences of each  $A_i$  and  $B_i$ :

$$\text{Penalty} = \text{Avg}_{i=1}^{N_a} (|A_i - B_i|) = \frac{1}{N_a} \sum_{i=1}^{N_a} (|A_i - B_i|)$$

Test Sample	Layer 1		Layer 2		Layer 3		Penalty
43   17   10   2	18		30   6		43   17   10   2		
Matching Samples	Avg	Diff	Avg	Diff	Avg	Diff	
40   18   11   3	18	0	29   7	1   1	40   18   11   3	3   1   1   1	2.5
15   45   1   11	18	0	30   6	0   0	15   45   1   11	28   28   9   9	18.5
20   30   5   5	15	3	25   5	5   1	20   30   5   5	23   13   5   3	17

Figure 2: MLA algorithm using simple differential penalty point strategy.

Figure 2 shows an illustration of above algorithm with such penalty point strategy for a test sample and 3 matching samples having 4 members which in fact is the number of time bands for speech recognition problem. Only 1 frequency band is considered just for the ease of understanding. This means that our samples in this example are matrices of  $(4 \times 1)$ .

First matching sample in figure 2 is most similar one and gets the least penalty. Although second matching sample gets no penalty in first two layers but it gets largest penalty in last level. It should be mentioned again that differences of each layer are averaged and sum of these averages will be the penalty point. For better understanding, let us review how the penalty of third matching sample is calculated.

In first layer, the average of all members (20, 30, 5, and 5) is 15 and the difference of this value with its correspondence in test sample (18) is equal to 3 which is added to penalty points of this matching sample ( $P = 3$ ). Then in second layer, average of first two members (20 and 30) is 25 and average of second two members (5 and 5) is 5. The differences of these averages with their correspondence (30 and 6) are respectively 5 and 1. The penalty point of this layer is then average of 5 and 1 which is 3 and adds to overall penalty ( $P = 3+3 = 6$ ). In last layer, each member acts as an average and therefore the differences with the corresponding values of test sample are 23, 13, 5 and 3. The penalty point of this layer is average of these values which equals to 11. Finally the overall penalty is  $P = 6 + 11 = 17$ . All of these calculations were based on differential penalty point strategy. A fuzzy penalty point strategy is presented in next sub-section.

### 3.2 Fuzzy Classification

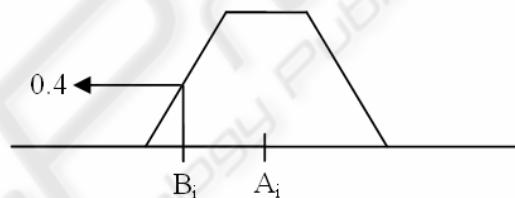
The chosen penalty point strategy in above algorithm is the strategy to eliminate non-similar samples so that the best match gets the least penalty. Therefore, it can be considered as a classifier. One simple method has been introduced in previous sub-section. Another strategy is used in this project which is based on fuzzy numbers.

Instead of calculating the difference between  $A_i$  and  $B_i$ , the averages of test sample ( $A_i$ ) are considered fuzzy numbers. These fuzzy numbers are defined by a symmetrical trapezoidal membership function (the size of this trapezoid depends on the

nature of the problem and will be specified mostly by trial and error to achieve best results). Then, membership values of the corresponding averages of matching sample ( $B_i$ ) are calculated. The overall penalty for all pairs of averages is calculated by:

$$\text{Penalty} = \text{Avg}_{i=1}^{N_a} ((1 - \mu_{\tilde{A}_i}(B_i)) \times 100) \\ = \frac{100}{N_a} \sum_{i=1}^{N_a} (1 - \mu_{\tilde{A}_i}(B_i))$$

If each two averages are close enough, the membership value would be 1 and then the penalty is 0. Otherwise it gets a linear penalty up to 100. Figure 3 shows a fuzzy number ( $A_i$ ) and how a penalty is given to a corresponding average ( $B_i$ ).



$$i^{\text{th}} \text{ Penalty: } (1 - 0.4) \times 100 = 60$$

Figure 3: Fuzzy number and penalty calculation.

In order to apply the MLA algorithm to the presented problem in previous section, a sample is treated like 12 sub-samples for every frequency band and each of these 12 sub-samples are given to the algorithm and a penalty point is gathered for each band and these penalty points are added up to one penalty point for the whole sample.

### 4 COMPLEXITY OF ALGORITHM

It is very easy to show that both space and time complexity of MLA algorithm is  $\Omega(n)$  in which  $n$  is the number of trained samples. The samples which are introduced to the system are usually called trained samples. However it should be considered that there is no training stage in this algorithm. Adding new samples only involves calculating spectrogram with FFT algorithm which can be done very fast, normalizing which is applying a function to each value of spectrogram and finally averaging

spectrogram to acquire a matrix of  $(32 \times 12)$  and saving this matrix for further use.

The memory space needed for this algorithm is  $32 \times 12$  integer numbers for each sample. Considering the range of these integers [0, 255], only 1 byte is needed for each number. Therefore each sample takes 384 bytes and the growth of space is  $384 \times n$  hence  $\Omega(n)$ .

Time complexity for this algorithm can be calculated by considering the comparisons for each sample. The number of layers is always constant (6 layers in this case:  $2^0$  to  $2^5$ ). In presented problem there are 12 frequency bands which are also constant. Therefore number of comparisons for each sample is constant and same for all samples. This shows that the complexity is again  $\Omega(n)$ . However, the sorting step takes about  $O(n \log n)$ . This causes the time complexity to be  $O(n \log n)$  in overall which is still acceptable as a fast algorithm.

The small size of memory needed for each sample and the speed of recognition of a word make this algorithm very suitable for voice commands in mobile devices such as cell phones, PDAs and etc. Since there are only one or two words for each command and considering the results in next section, this simple algorithm seems very efficient and useful for the purpose of voice command.

## 5 RESULTS

The presented algorithm has been implemented and tested for a single speaker with 100 words. The results have been compared to that of a widely used method in speech recognition, HMM. In order to measure flexibility of this algorithm to noise, different kinds of noises are applied to test data. Table 1 shows these results.

For this purpose, a database of samples is generated which contains about 8 different pronunciations of a same word, for 100 words which add up to 800 samples. All samples were introduced to system except one for each word. Then these unused samples were tested by system and asked for recognition. The entry called "Clean" in table 1 refers to these results.

Afterwards, different amounts of two kinds of noises, White Noise and Babble Noise, are added to test data and asked again to be recognized. Other

entries of table 1 show these results. Also, "First Answer" means first recognized answer is the correct answer and "Third Answer" means one of the first three answers is the correct answer. The same data has been tested with HMM approach and its results are also included for comparison.

Table 1: Experimental results.

		HMM	First Answer	Third Answer
Clean		100 %	98 %	99 %
White Noise	20 db	99 %	91 %	96 %
	10 db	74 %	90 %	96 %
	0 db	4 %	84 %	91 %
Babble Noise	20 db	98 %	98 %	99 %
	10 db	92 %	92 %	95 %
	0 db	39 %	44 %	72 %

Table 1 shows that while the efficiency of HMM algorithm drops down sharply with noisy data, the presented algorithm keeps its efficiency even with intensive noise. Also, it can be noted that because of the smoothing property of averaging, this algorithm has a good resistance to white noise and this can be concluded from above results. However, because the babble noise destroys the information of lower frequencies, it can affect the efficiency of this algorithm. Therefore, the first 3 lower frequency bands of spectrograms have been ignored to achieve better results in table 1.

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