# MULTIDIRECTIONAL FACE TRACKING WITH 3D FACE MODEL AND LEARNING HALF-FACE TEMPLATE

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Abstract: In this paper, we present an algorithm to detect and track both frontal and side faces in video clips. By means of both learning Haar-Like features of human faces and boosting the learning accuracy with InfoBoost algorithm, our algorithm can detect frontal faces in video clips. We map these Haar-Like features to a 3D model to create the classifier that can detect both frontal and side faces. Since it is costly to detect and track faces using the 3D model, we project Haar-Like features from the 3D model to a 2D space in order to generate various face orientations. By using them, we can detect even side faces in real time without learning frontal faces and side faces separately.

### **1 INTRODUCTION**

In recent years there has been a great deal of interests in detection and tracking of human faces in video clips. To recognize people in a video clip, we must locate their faces. For example, to design a robot capable of interacting with humans, it is required that the robot can detect human faces within its sight and recognize the one it is interacting with. In this case, the speed of face detection is most important. On the other hand, when face detection is used in surveillance systems, the speed of face detection is also important. However it is most important that the system can detect all faces in the video clips.

Recently, Viola et al. proposed a very fast approach for multiple face detection (Viola and Jones, 2001), which uses AdaBoost algorithm (Freund and Schapire, 1996). This algorithm learns a fast strong classifier by applying AdaBoost to a weak learner. Then the classifier is applied to sub-images of the target image, and the sub-images classified into a face class are detected as faces in the target image. This approach has two problems:

First, AdaBoost has some problem to use human face detection. AdaBoost does not consider the reliability of the classification result of each sample with each weak classifier. Furthermore, AdaBoost is based on decision-theoretic approach, which does not take the reason of misclassified samples. Therefore, this algorithm cannot distinguish between misclassified faces and misclassified non-faces. We will discuss these problems finely in section 3.

Second, this algorithm can only detect frontal faces. However the number of frontal faces in video clips is less than the number of side faces. Additionally, some algorithms have problems in the initialization process. Gross et al. (Gross et al., 2004) use mesh structure to represent a human face, and detect and/or track the face with template matching. In the initialization process, all mesh vertices must be marked in every training sample manually. Pradeep et al. (Pradeep and Whelan, 2002) represent a face as a triangle, whose vertices are the eyes and the mouth, and track the face with template matching. In the initialization process, they need to manually initialize the parameters of the triangle in the first frame. Ross et al. (Ross et al., 2004) use eigenbasis to track faces and update the eigenbasis to account for the intrinsic (e.g. facial expression and pose) and extrinsic variation (e.g. lighting) of the target face. In the initialization process, they need to decide the initial location of the face in the first frame manually. Zhu et al. (Zhu and Ji, 2004) use face detection algorithm in the first frame to initialize the face position. Thereby, they do not need manual initialization process. However, the face detection algorithm can detect only a frontal face.

In this paper, we propose an algorithm, which classifies sub-images to face class or non-face class by using classifiers. This algorithm does not require manual initialization process. We substitute Info-Boost algorithm (Aslam, 2000), which is based on information-theoretic approach, for AdaBoost algorithm, which is based on decision-theoretic approach. The reason is to solve the first problem and to improve the precision by using the additional information (hypothesis with reliability), which is ignored in AdaBoost. Additionally, our algorithm does not learn the whole human face but half of it and maps these half-face templates to a 3D model. Then the algorithm reproduces the whole-face template from the 3D model with some angle around the vertical axis. As a result, we can detect faces, which are even rotated around the vertical axis, by using the reproduced whole-face templates.

### **2 HAAR-LIKE FEATURES**

In this paper, Haar-Like features are used to classify images into a face class or a non-face class. Some samples of Haar-Like features are shown in Figure 1. Basically, the brightness pattern of the eyes distinguishes the face from the background. (a) is an original facial image. (b) measures the difference in brightness between the region of the eyes and the region under them. As is shown in (b), the brightness of the eyes is usually darker than the skin under them. (c) measures the difference in brightness between the region of the eyes and the region between them. As is shown in (c), the eyes are usually darker than the regions between them Thus, an image can be classified as a facial or a non-facial class based on the brightness pattern described above. These features are generated from feature prototypes (Figure 2) by scaling these prototypes vertically and horizontally.

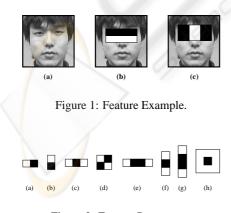


Figure 2: Feature Prototypes.

We calculate the average brightness  $B_b$ ,  $B_w$  in the black region and the white region of the features, and use their difference  $(F = B_b - B_w)$  as a feature

value. Then we use these feature values as parameters to classify images into a face class or a non-face class. For example, when a feature of Figure 1(b) is applied to a true human face, F is too large. Accordingly, we decide the threshold of the classification and classify images according to the feature value F, if it is larger or smaller than the threshold. If F is larger than the threshold, the image is classified into a face class. If F is smaller than the threshold the image is not a human face.

Viola et al. use feature prototype (a)-(d) shown in Figure 2. We use four additional prototypes (e)-(h). Prototype (e) will measure the difference in brightness between the region of the mouth and its both ends. The black region of prototype (e) will match the region of the mouth, and the white regions will match both ends of the mouth. The black region of prototype (f), (g) will match the region of the mouth (the eyes), and the white regions will match the top and bottom of the region of the mouth (the eyes). The black region of prototype (h) will match the region of the eye (the nose or the mouth), and the white region will match the region around the eye (the nose or the mouth). Therefore, these feature prototypes will be effective to classify images to face and non-face classes.

If we add these effective feature prototypes like (e)-(h), the learning time will be somewhat increased, while the speed of classification will be improved. If we add some compound feature prototypes, the time of classification will be decreased. For example, feature prototype (e) can be considered as the prototype, which is made by combining the prototype (a) twice. In the region where the feature prototype (e) can be used, we need to calculate twice for the value of the feature generated from prototype (a). But now we need only one calculation for the value of the feature generated from the prototype (e). So the time complexity is decreased for these regions, and the detection time can be reduced. In this case, if we need tseconds to face detection with prototype (a), we only need  $\frac{1}{2}t$  second to face detection with prototype (e).

### **3** APPLYING INFOBOOST

Classification with Haar-Like features is fast, but it is too simple and its precision is not very impressive. Hence, we apply a boosting algorithm to generate a fast strong classifier. AdaBoost is a most popular boosting algorithm.

#### 3.1 AdaBoost

AdaBoost assigns the same weight to all training samples and repeats learning by weak learners while updating the weights of the training samples. If the weak classifier generated by the weak learner classifies a training sample correctly, the weight of the sample increases. If the weak classifier misclassifies a training sample, the weight of the sample decreases. By this repetition, the weak learner becomes more focused on the sample, which is difficult to classify. At last, by combining these weak classifiers with the voting process, AdaBoost generates one strong classifier and calculates the final hypothesis for each sample. The voting process evaluates results of weak classifiers by majority decision and decides the final classification result. Nevertheless, we use InfoBoost to increase the precision of the classifier because there are two problems in AdaBoost.

Weak classifiers generated in the AdaBoost process do not consider the reliability of the classification result for each sample. Hence, the classifiers which classify the sample with high reliability and those which classify the sample with low reliability are combined without any consideration of their reliabilities.

For example, assume that nine weak classifiers are generated in the AdaBoost process. If four of them classify a sample into a face class with 95% accuracy, and five of them classify the same sample into a non-face class with 55% accuracy, the image will be classified into a non-face class. If we introduce the reliabilities of these classifications, the sample should have been classified into a face class.

Another problem is that AdaBoost is based on decision-theoretic approach. AdaBoost algorithm only deals with two cases, whether the classification is true or false, when the weights are updated. But actually there are the following four cases to be considered.

- A face image classified into a face class.
- A non-face image classified into face class.
- A face image classified into a non-face class.
- A non-face image classified into a non-face classD

The incidences of these classifications are not always the same. For example, in a certain round of AdaBoost, if the number of misclassified face images and the number of misclassified non-face images are nearly equal, all we are required to do is to decrease the weights of correctly classified samples and to increase the weights of incorrectly classified samples. In contrast, if the number of misclassified non-face images is larger than the number of misclassified face images, the misclassified non-face images will be classified correctly in the next round or later, although the misclassified face images may not be correctly classified. The reason is that AdaBoost does not take care of the difference of two misclassification cases. Therefore, we should not depend only on the classification result (true or false) for weight updating, but we must also consider the correct classes (positive or negative). When we update the weight of each sample image we must consider these four cases separately.

### **3.2 InfoBoost**

In this paper, we consider the two problems of AdaBoost and use InfoBoost algorithm, which is a modification of AdaBoost. We propose three points where InfoBoost and AdaBoost differ:

First, InfoBoost repeats the round T times  $(t = 1, \dots, T)$  in the learning process. In round t, weak hypothesis  $h_t$  is shown by  $h_t : X \to \mathbb{R}$ . The hypothesis represents not only the classification result but also the reliability of the classification result. In order to make it easy to handle, we restrict the region of hypothesis  $h_t$  to [-1, +1]. The sign of  $h_t$  represents the class of prediction (-1 or +1), and the absolute value of  $h_t$  represents the magnitude of reliability. For example, if  $h_1(x_1) = -0.8$ ,  $h_1$  classifies the sample  $x_1$  into the class -1 with the reliability value 0.8.

Second, the accuracy of negative prediction  $\alpha_t[-1]$ and the accuracy of positive prediction  $\alpha_t[+1]$  are calculated. These values are calculated using equation (1), (2).

$$\alpha[-1] = \frac{1}{2} \ln \left( \frac{1+r[-1]}{1-r[-1]} \right)$$
(1)

$$\alpha[+1] = \frac{1}{2} \ln \left( \frac{1+r[+1]}{1-r[+1]} \right)$$
(2)

$$\cdot [-1] = \frac{\sum_{i:h(x_i) < 0} D_t(i) y_i h_t(x_i)}{\sum_{i:h(x_i) < 0} D(i)}$$
(3)

$$r[+1] = \frac{\sum_{i:h(x_i) \ge 0} D_t(i) y_i h_t(x_i)}{\sum_{i:h(x_i) \ge 0} D(i)}$$
(4)

 $y_i$  is the correct class of the sample  $x_i$ , and  $D_t(i)$  is the weight of the sample  $x_i$  in round t.  $\alpha_t[-1]$  and  $\alpha_t[+1]$  reflect the magnitude of reliability and the precision of classification for each sample. If hypothesis  $h_t$  classifies  $x_i$  into the class -1,  $\alpha_t(h_t(x_i))$  is  $\alpha_t[-1]$ . If hypothesis  $h_t$  classifies  $x_i$  into the class +1,  $\alpha_t(h_t(x_i))$  is  $\alpha_t[+1]$ .

Third, the weight  $D_t$  is updated according to equation (5)

$$D_{t+1}(i) = \frac{D_t(i)\exp(-\alpha_t(h_t(x))y_ih_t(x_i))}{Z_t}$$
 (5)

 $Z_t$  is a normalization factor. It is chosen in a way that  $\sum_i D_{t+1}(i) = 1$ . By executing this operation, the weight of the sample classified correctly with hypothesis  $h_t(x_i)$  is decreased, while the weight of the sample classified incorrectly with hypothesis  $h_t(x_i)$ is increased. We repeat these processes T times, and calculate the final hypothesis H with the T weak hypotheses. Then we take a weighted vote among hypotheses using  $\alpha_t(h_t(x_i))$  as weight. If the result of voting is a negative value, we output -1 as the final hypothesis, and if the result of voting is a positive value, we output +1 as the final hypothesis.

When we apply InfoBoost to weak learners, it is necessary to show how correct the classification results of training samples are. We calculate the feature value for each training sample, the difference d of the feature value f, and the threshold t (d = f - t). The sign of difference f represents the classification result. If the absolute value of d is too small, the feature value f is near the threshold d. The sample classified +1 might be classified -1, so it is not trusty. Conversely, if the absolute value of d is too large, the classification result is trusty. Obtaining the difference between feature value and threshold, we can express the classification result and its reliability for each sample. Therefore, we use the difference between the feature value and the threshold as the classification result with evaluation of reliability.

Because InfoBoost is based on informationtheoretic approach, it does not only have the benefit of the improvement of the classification's precision, but also it can provide some flexibility for the classifier. For instance, in surveillance systems, we must detect all human faces while it is allowed to mis-detect few non-faces as faces. On the other hand, if a surveillance system of a building cannot detect some faces and those people commit a crime in the building, we cannot place their faces on the wanted list. Thus the surveillance system which cannot detect some human faces is not useful.

By increasing the weight of face samples classified into non-face class, the learning process focuses more on the misclassified face image and the final classifier will be able to detect almost all human faces more accuratly. Hence, we can adapt classifiers for surveillance systems by adjustment of weights of samples. InfoBoost can bias the classification basis based on the importance according to the four cases (face classified into face, face classified into non-face, non-face classified into face, and non-face classified into nonface) by biased the rules of updating weight.

# 4 3D MODEL AND LEARNING HALF-FACE TEMPLATE

In video clips, the probability of having complete frontal faces is not high. Most of them are side faces. Consequently, we map the classifier learned from facial features to a 3D model (Figure 3(a)(b)). The 3D model consists of three areas (r), (c), (l) (in Fig-

ure 3(b)). (r) is the right part of the 3D model, (c) is the center part of the 3D model, and (l) is the left part of the 3D model. These parts of the 3D model are plane faces, and their joint angles are  $\frac{\pi}{4}$  in Figure 3(b). By using this 3D template, the classifier will be able to detect not only frontal faces but also side shots of faces.

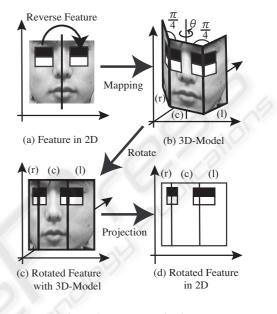


Figure 3: Feature Projection.

If we use 3D model in face detection, time complexity is increased and detection speed is decreased, because the calculation of 3D model is time consuming. Therefore, we create a new classifier by rotating the 3D model around the vertical axis and by projecting the 3D model classifier back to 2D again (Figure 3(c)(d)). By using these classifiers, we do not need calculation of 3D model in the detection process, so the time complexity does not increase much.

If the rotation angle is  $\theta$  (positive for clockwise rotation), the width  $w_r$  of area (r) is modified to  $\frac{\cos(\theta - \frac{\pi}{4})}{\cos \frac{\pi}{4}}w_r$ , the width  $w_c$  of area (c) is modified to  $\cos(\theta)w_c$ , and the width  $w_l$  of area (l) is modified to  $\frac{\cos(\theta + \frac{\pi}{4})}{\cos \frac{\pi}{4}}w_l$ . We execute these processes in every 30 degrees of rotation angle and use these classifiers in parallel to prevent the increase of time complexity.

But, there is a self-occlusion problem. When the 3D model is rotated enough, (r) or (l) of the 3D model is occluded by (c), and some feature rectangles in 3D model may be hidden and we cannot use these features. If the 3D model in Figure 3 is rotated in clockwise direction enough, the part of the feature at the right eye in (r) will be hidden and we cannot use this feature. Hence, we do not use whole faces but use half-faces as learning samples.

Furthermore, because of the face symmetry, we express the whole face by combining reversed facial features with the original ones (Figure 3(a)). Therefore, even if the 3D model is rotated, we can use all features of either the right half or the left half of the face.

Additionally, because of learning half-faces, we can be free from the different illumination states between left and right faces. We use the right side and reversed left side of whole face samples as the halfface samples, thus the half-face classifier is robust to the difference between the left and the right of the faces.

The classifier generated from the boosting algorithm is a set of weak classifiers using Haar-Like features. Each weak classifier consists of the following elements: coordinates of the reference points, width and height of the white and black rectangles of Haar-Like feature, and the threshold of Haar-Like feature. In Figure 4,  $P_w$  is the reference point of the white rectangle of Haar-Like feature, and  $P_b$  is the reference point of the black rectangle of Haar-Like feature. The coordinates of these rectangles are shown as  $X_w$ ,  $X_b$ ,  $Y_w$ ,  $Y_b$ , and widths and heights of these rectangles are shown as  $W_w$ ,  $W_b$ ,  $H_w$ ,  $H_b$ .

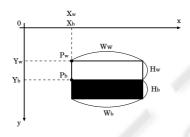


Figure 4: Parameter of Haar-Like Feature Rectangle.

Therefore, the features are easily mapped to the 3D model shown in Figure 3(b). Then, we confine that 3D model can only be rotated around the vertical axis, as a result feature rectangles are scaled only in horizontal axis (see Figure 3(a) and (d)). Therefore, the weak classifier generated by projecting the features from 3D model to 2D can be transformed by moving, expanding and/or shrinking the Haar-Like feature rectangles of the original weak classifier horizontally.

## 5 EXTENSION OF CASCADING

Cascading is the algorithm to reduce the time complexity of classification. Cascading algorithm generates the cascade of small classifiers by dividing the set of weak classifiers into some subsets. The first classifier of the cascade classifies all samples. The samples classified into negative samples are not passed to the following classifiers. By doing this, cascading algorithm reduces the number of samples to be evaluated and the time complexity of classification. To generate each weak classifier, the learning process is executed with a constrained condition (TP > minTP) while FP < maxFP. True positive rate TP and false positive rate FP are calculated as follows:

$$TP = \frac{\text{number of correctly classified faces}}{\text{total number of faces}} (6)$$
$$FP = \frac{\text{number of misclassified non-faces}}{\text{total number of non-faces}} (7)$$

minTP and maxFP are parameters of the learning process. We execute learning process with minTP = 0.999 and maxFP = 0.4.

We extend boosting and cascading process in the following three points to reduce the time complexity of face detection and learning time.

- The configuration of the cascading.
- The termination condition of the learning process.
- The number of samples used in AdaBoost process.

First, when we use half-face templates, we must evaluate them separately and aggregate these evaluation results. As is shown in Figure 5, the classifier consists of two cascades. In this case, both of the calculations of these cascades are executed every time. However, when the target sample is rejected in an early stage in one of these cascades, the calculation of another cascade makes no sense. Therefore we combine these cascades as shown in Figure 6 to reduce the unnecessary process. By using this new cascade, the unnecessary process is avoided. If the target sample is rejected in an early stage on one of the cascades, the calculation on another cascade is stopped immediately.

Second, when we use half-faces as learning samples, characteristic features of a face are much fewer than those of whole face samples. If we use whole faces as learning samples, we can use all features learned from the whole face. However we cannot use some of these features (for example, the feature in Fig 1(b), (c)), because we use half-faces as learning samples. Thereby, we will use some new features that can be applied to half-faces to substitute for the features that we cannot use here. These new features are more delicate, hence their number is larger than that of the features that can only be applied to the whole faces. As the tradeoff, the speed of face detection will be decreased, because a simple feature based on the whole face is replaced by several small features based on the half-face. Accordingly, in the learning process, if precision of the classifiers is enough to detect faces, we finish the learning process. As the learning process makes progress, the face detection rate will hit a peak. Simultaneously, the number of features which are necessary to classify both positive and negative

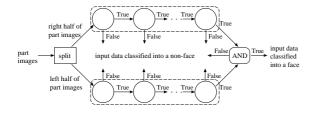


Figure 5: Two Classifier Cascades.

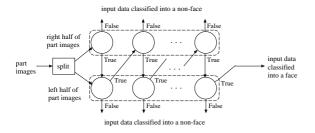


Figure 6: Combining Two Classifier Cascades.

samples will become larger. For this reason, we stop the process when both the precision and the recall are larger than 0.95.

Third, in learning process, we must use many sample images to detect almost all faces. However, when we use many sample images, the time complexity of the learning process is very huge. Therefore, we use a subset of all samples to generate each small classifier. These samples are selected by random sampling.

Random sampling is a sampling algorithm which pick out some samples from all samples randomly without overlapping. Random sampling is used where we cannot evaluate all samples (for example, marketing). The probability of each sample to be picked out is same. Therefore, the selected samples are miniature versions of all samples, and the learning result with selected samples will be similar to that with all samples.

We must decide the total number of selected samples. We decide the number based on "Chernoff bound" (Chernoff, 1952). The number of selected samples n are defined by inequality (8).

$$n > \frac{1}{2\epsilon^2} \ln\left(\frac{2}{\delta}\right) \tag{8}$$

According to "Chernoff bound", if the above inequality is satisfied for any  $\epsilon$  ( $0 < \epsilon < 1$ ) and any  $\delta$ ( $0 < \delta < 1$ ), the number of sample *n* is enough for classification. We use this inequality as  $\epsilon = 0.05$ ,  $\delta = 0.01$ , and get the minimum n = 1060. Thus we select 530 positive samples and 530 negative samples in each stage to generate small classifiers.

#### **6 EXPERIMENTS**

We performed five experiments. We use a window to extract sub-images from the original image. Minimum size of the window is 38x38 pixels, translation factor is 0.5 \* window size and scale factor is 1.2.

First, we compare the precision of the classifier generated by InfoBoost with that of AdaBoost. We use Yale Face Database B (Georghiades et al., 2001) as positive samples. We use half of them as training set, and the rest as test set. We use our own negative sample images in the learning process. We generate more negative samples by clipping and scaling these original ones . The total number of negative samples is 7933744, and we use half of these samples as a training samples, and the rest as a test set.

The result of our experiment is shown in Figure 7. The horizontal axis shows false positive rate and the vertical axis shows true positive rate. The horizontal axis is a logarithmic axis to show the difference of the graphs more clearly.

This graph shows that the precision of InfoBoost is higher than that of AdaBoost. The true positive rate of AdaBoost impatiently decreases when the false positive rate is small. When the false positive rate is small, there are less misclassified non-face samples than misclassified face samples. InfoBoost can focus on both misclassified non-face and face samples separately, thus InfoBoost can reduce false positive rate with reduction of true positive rate. In contrast, AdaBoost cannot focus on the misclassified non-face samples and but can focus on the misclassified face samples. That is because AdaBoost does not use the true classes of samples and cannot discriminate between misclassified face samples and misclassified non-face samples. AdaBoost cannot distinguish between misclassified faces and misclassified non-faces, and cannot focus on misclassified non-faces, thus AdaBoost reduce true positive rate without reduction of false positive rate, and the precision of AdaBoost impatiently decreases.

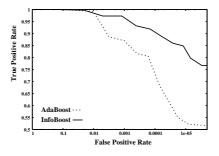


Figure 7: Precision of Classifier.

Second, we perform the experiment of face tracking with 3D model, and examine the accuracy of the classifier for each angle (-60, -30, 0, 30, 60 degrees). The training set this time will consist of the training, and the test sets will in the first experiment. We use Head Pose Image Database of Pointing'04 (N. Gourier, 2004) as test set. This data set contain multidirectional face images (vertical angle= $\{-90, -60, -30, -15, 0, +15, +30, +60, +90\}$ , and horizontal angle= $\{-90, -75, -60, -45, -30, -15, 0, +15, +30, +45, +60, +75, +90\}$ ). We use a part of these samples, whose vertical angles are 0, and horizontal angles are  $\{-75, -60, -45, -30, -15, 0, +15, +30, +45, +60, +75\}$ . There are 30 sample images for each degree, basically the maximum number of detected faces is 30. Besides, the number of evaluated sub-images is about 4800000. Thus the maximum number of detected negative samples is about 4800000.

We show two figures indicating the accuracy of classifiers in Figure 8 and Figure 9. We represent the classifier aiming at detecting faces rotated with  $\theta$  degrees as Classifier[ $\theta$ ], and samples rotated with  $\theta$  degrees as Samples[ $\theta$ ]. Most classifiers can detect faces rotated with an angle close to that of the classifier, and the number of mis-detected non-faces is not many. For example, Classifier[0] classifies Sample[0] correctly with high precision. However, there are two exceptions.

One of them is that Classifier[-30] and Classifier[+30] have the highest detection rate on Samples[-15] and Samples[+15]. The reason of angle mismatch is as follows: The structure of 3D face model is too simple to represent human faces correctly. Additionally, the test samples are taken by only one camera, and faces are turned toward a sign on the wall that indicates the direction. When the samples were being taken, some people of the test sample only focused their eyes on the sign instead of rotating their heads, thus their face direction is not turned toward the sign.

The other exception is that Classifier[-60] and Classifier[+60] have the highest detection rate on Samples[0]. For this case, we consider the reason is self-occlusion of 3D model. If the angle is -60 or 60 degrees, self-occlusion of 3D model emerges and we cannot use left or right half-face detectors. Accordingly, the Classifier[-60] and the Classifier[+60] detects half of the whole face, thus the number of detected faces in Samples[0] is increased.

Third, we compare the detection speed between the classifiers using the new cascading structure (Figure 5) and the classifiers using old one (Figure 6) on all the samples used in the second experiment. If we use the new cascading structure, we can detect faces in an image whose size is 320x240 pixels, in about 0.036 seconds on 3.2GHz Pentium 4. If we do not use the new cascading structure, the calculation time is about 0.043 seconds. Hence, our new structure of cascading is effective for reduction of time complexity.

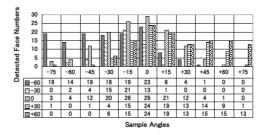


Figure 8: Number of Detected Faces for Each Direction.

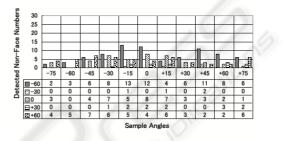


Figure 9: Number of Detected Non-Faces for Each Direction.

Fourth, we execute the learning process with random sampling, and evaluate it. We extracted training sets from the same data set, which is used as the training set in the second experiment. The learning time with random sampling is about 2.5 hours, and that without random sampling is about 2 days. Additionally, the result of face detection with random sampling is shown in Table 1. The numbers of detected faces and non-faces for each direction are reduced compared to the detection result without random sampling. Accordingly, precision is reduced and recall is improved. Total accuracy is not reduced. In conclusion, random sampling reduces the time complexity of learning without reducing the accuracy of the face detector.

Table 1: Number of Detected Faces/Non-Faces for Each Direction With Random Sampling.

	-60	-30	0	+30	+60
-75	23 / 10	0 / 0	1/0	0 / 0	0/14
-60	17/6	0 / 0	2/0	0/0	0/9
-45	11/9	1/0	2/0	0/0	0/6
-30	9 / 10	7 / 0	12 / 1	0 / 0	1/3
-15	8 / 11	14 / 0	20 / 0	3/0	5/1
0	6/5	13/0	25 / 0	17/0	11/3
+15	3 / 2	2/0	14 / 1	17 / 1	15 / 1
+30	1/2	1/0	5/0	7 / 0	5/3
+45	0 / 10	0 / 0	0 / 1	5/0	6/2
+60	0 / 10	0 / 0	0 / 1	2/0	12/4
+75	0/7	0 / 0	0 / 0	0/0	11/8

Fifth, we increase the weight of misclassified face samples in the learning process. The way we extracted training sets is the same as that in the fourth experiment. After updating the weights of samples, we double the weights of misclassified face samples. The result of face detection is shown in Table 2. Looking at the result of Classifier[-30], Classifier[0]and Classifier[+30], we see the number of detected faces is not increased and the number of detected nonfaces is decreased. The reason of this is that we use parameters maxFP and minTP to repeat and finish the learning process. These parameters are stronger than modification of weights. Hence, the modification of weights cannot increase the precision of face detector. However, it can reduce its time complexity, because the learning process focuses more on the misclassified faces and converges faster. In this case, we can detect faces in an image whose size is 320 by 240 pixels, in about 0.023 seconds on 3.2GHz Pentium 4, which is faster than that without modifying the weights.

Table 2: Number of Detected Faces/Non-Faces for Each Direction With Random Sampling and biased InfoBoost.

	-60	-30	0	+30	+60
-75	26 / 1	0/0	0 / 0	0 / 0	0 / 15
-60	22 / 2	0/0	0/0	0/0	0 / 10
-45	18/3	1/0	0/0	0/0	0/11
-30	13 / 8	1/0	4 / 0	0 / 0	9/2
-15	10 / 10	2/0	12/0	0 / 0	9/2
0	7/8	0/0	20/0	10/0	17/2
+15	3/6	1/0	9/0	8 / 0	14/9
+30	2 / 10	0 / 0	1/0	2/0	11/5
+45	0 / 10	0/0	0/0	0/0	12/8
+60	0 / 14	0 / 0	0 / 0	1/0	17/2
+75	0 / 11	0 / 0	0 / 0	0 / 0	18/5

## 7 CONCLUSIONS AND FUTURE WORK

In this paper, we tried to improve the precision of a classifier by using InfoBoost algorithm and tried to detect not only frontal faces but also side faces by using 3D model and half-face templates. Additionally we extend the classifier cascade, and reduce the time complexity of learning and face detection.

However, we cannot detect faces rotated around the horizontal axis, or the axis vertical to the image. If we rotate the 3D model around these axes and project the features from 3D model to 2D space, these Haar-Like feature rectangles are deformed. In our algorithm, we can only calculate upright rectangles. Thus, we must think about a fast algorithm to calculate these feature values.

Furthermore, with the extensions in this paper, the time complexity of face detection is increased. We must reduce the time complexity by reducing the images evaluated with face detector or some other method. In the process of extracting sub-images from the target image, if we use skin colors to detect face candidate regions, the number of evaluated sub-images are reduced. Therefore, the precision of classifier may be improved and time complexity may be reduced.

Likewise, we must perform more experiments with different training and test samples. When we perform experiments with only one training set and one test set, the result depends only on these samples. Consequently, if these samples are not trusty, the experiment result is not trusty either.

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