# A FUZZY-BASED DISTANCE TO IMPROVE EMPIRICAL METHODS FOR MENU CLUSTERING

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Keywords: Menu Design, Human Factors, Design Methodology.

Abstract: An effective menu organization is fundamental to obtain usable applications. A common practice to achieve this is to adopt empirical methods in the menu design phase, by requesting a number of intended final users to provide their ideal tasks arrangements. However, to improve the effectiveness of this approach, it is necessary to filter results, by identifying and discarding data coming from subjects whose mental models are too weak on the considered domain. To this aim, in the paper, we propose a formal tool suited to support menu designers, which is based on a fuzzy-based distance we defined. This measure can be easily calculated on the empirical datasets, thanks to a specifically conceived supporting application we developed. As a result, by exploiting the proposed solution, menu designers can rely on a formal tool to evaluate significance of empirical data, thus leading towards more effective menu clustering.

## **1** INTRODUCTION

In the literature it is widely proved that an intuitive menu organization, corresponding to user's expectations, can lead to many benefits, since it improves the overall usability of the system (for instance (Norman, 1991), or (Schneiderman, 1998)). Moreover, in some domains, menu intuitiveness can eventually affect safety of human beings. For instance, in automotive info-telematics systems the end-user is normally busy in the mission-critical task of driving, and menu clustering has deep impact on the safety, since it influences the amount of time the driver spends with glances out of the road, searching for a specific system feature (Di Martino, 2005).

The effectiveness of a menu-based system is strongly dependent on the organization of its items, which should both be congruent to the operator's mental organization of the task domain, both closely match his/her conceptual relationships between system features (Wickens, 1984). This is particularly true for ubiquitous information systems, such as cell phones, MP3 players, automotive information systems, etc... where very often the point-and-click paradigm cannot be applied, and the interaction is achieved exclusively by means of menus. For standard desktop applications, the menu design is a widely covered issue by the literature, where it is possible to find lots of guidelines and different approaches, such as (Sears and Shneiderman, 1994). Many menu organizations have been suggested in

literature, such as alphabetical, categorical, or frequency-based (Norman, 1991). In particular, the frequency-based sorting is achieved by placing the most frequently used item at the top of the menu, and it turns out to be very adequate (other than widely adopted) for the previously described mobile systems. In fact, it allows users for a faster selection of frequently used features, with an overall reduction of interaction efforts. To apply this approach, User Interface (UI) designers must own knowledge about the selection frequencies of the considered tasks. This job is straightforward in well-established domains, since these data are either usually available or easilv collectable by logging subjects' interactions in pilot experiments. But when dealing with novel application domains, these data are often not available. Thus, since it is not possible to rely only on domain experts knowledge (Toms et al., 2001), there is the necessity to gain data from empirical methods, involving external subjects to capture the diverse organizational structures that exist within the user population (Shneiderman, 1998). This is especially true when the intended user population is highly diverse on factors such as age, system expertise, and technical background, which is a common case for mobile systems (Toms et al., 2001). About the empirical approaches, many researches in the literature suggest to analyze data with methods such as the Cluster Analysis Technique or Multi-dimensional Scaling. However, their applicability to dual task environments, such as the ubiquitous ones, is not clear (Toms et al., 2001). Indeed, we adopted the cluster analysis technique in the context of automotive info-telematics systems, but the data we gathered leaded us to initial inaccurate results. In particular, we recruited a set of 14 intended end-users to define a meaningful menu arrangement for the navigator, phone, SMS and entertainment sections of a next-generation telematics system. We noticed that some subjects do not own a significant mental model on the specific features, thus distorting the results in the gathered empirical data.

Starting from this experience, we felt the need for a formal tool able to support the menu designer in identifying the outliers, i.e. the subjects with a mental model too weak for significant results in these experiments. To address this issue, in this paper we introduce a notion of *distance*, to measure how far is the mental model of a subject with respect of all others, when dealing with frequency-based menu organizations. In particular, we propose a "fuzzy-based" distance function, aimed at measuring the closeness between different arrangements of menu items proposed by the subjects. This measure allows menu designers to define a threshold to clearly identify the outliers. The threshold can be easily calculated by using a tool (freely downloadable) we developed, which is able to highlight subjects' data too far from the others. So. the defined distance allows menu designers to filter empirical data on the basis of a formal tool rather than on his/her sensibility, which can be highly subjective. Thus, higher quality and repeatable results can be obtained from the datasets, leading towards menu clustering less biased by outliers.

The remainder of the paper is structured as follows. In section 2 we describe the experiment we conducted, and the related contrasting results, which motivated us in working for the definition of a distance. In section 3 we present the fuzzy-based distance function, and how to calculate it, while in section 4 we report on the application of this distance on our dataset, also by exploiting a tool we specifically developed to assist menu designer. Finally, a discussion on final remarks and future work will conclude the paper.

# 2 THE EXPERIMENT

In 2004 we were involved in the definition of the UI for a next-generation automotive telematics system, together with the research centre of a well-known automotive car manufacturer. We had about 90 system features to arrange within menus. Accordingly to the standard literature guidelines (for

instance (Lee, MacGregor, 1985)) we adopted the following methodology to arrange these items:

- 1. cluster together items sharing some inherent relationships, and
- 2. within each cluster, sort items basing on selection frequency, placing most frequently used on top of hierarchy.

Since we were dealing with many novel features, such as remote diagnosis, or interaction with PAN wireless devices, we had no previous data about their frequency of use. To define an organizational menu structure reflecting a "typical" end-user mental model, many previous researches (such as (Toms et al., 2001)) suggest to use empirical methods involving a number of intended users, external from the development team. Following these suggestions, we recruited for the experiment a total of 14 participants, 9 males and 5 females. Their age ranged form 23 to 59, with a mean of 31. To gain insight about their backgrounds, we collected information about their experiences on Personal Computers, Cell Phones, Car Stereo and Mobile Navigators. Moreover, we asked subjects if they own a Car Stereo and/or a Car Navigator. The results were that all subjects but one reported to be familiar with personal computers and phone cells. All the 14 subjects stated to have experience with a car stereo, and only three of them do not own it. Finally, 8 subjects reported some previous experiences with car navigators, and only 3 have a telematics system in their vehicles. Thus, almost half of the samples does not have familiarity with advanced automotive infotainment applications.

The stimuli for the analysis consisted of 90 strips of paper (8 x 2.5 cm), each of them with a system feature description, corresponding to a generic task that one might perform when using a next generation telematics system. Slips were subdivided according to six modules of the system, namely the Navigator, Audio – OFF, Audio – Tuner, Audio – CD Changer, Cell Phone and Short Message System (SMS).

Obviously, careful consideration was given wording of each task description, to allow subjects to base their assessments more on the semantic rather than the syntactic attributes of the task. Some examples of these strips are provided in Table 1.

Each strip was accompanied by a number (not shown to subjects), used by the team for task identification. Subjects were asked to:

- 1. Sort slips, placing at the top positions the feature they suppose to be the most frequently selected, according to their mental model.
- 2. Arrange slips into stacks of related functions, based on their own criteria for similarity. They could make as many separate stacks as they cared to, as long as each stack contained at most four task items.

Activate Remote Diagnosis						
Play a specific track of the CD						
Write a SMS						
Insert a Destination in the navigator						

In the remainder of the paper, we will use indifferently the terms *permutation*, *arrangement*, *list* and *sequence*, to refer to the ordered list of menu items produced by a subject in step 1, to represent his/her mental model of selection frequency.

In order to obtain the tree-like structure of menu items (named also *dendritic* representations, or *dendograms*), we adopted the Agglomerative Clustering Procedure (Toms et al., 2001), starting from a situation in which every item is in its own cluster and then, in succeeding steps, merging the closest clusters on the basis of their similarity. Within each of these clusters, items are sorted consequently to the sequences proposed by subjects. In particular, the final permutation is obtained by applying the statistical *mode* function on all the gathered lists.

#### 2.1 Results

Some of the empirical data we gained from subjects are shown in Table 2 (results for the SMS module) and Table 3 (results for the navigator module). The strings S1...S14 in first column identify the considered subjects, while the numbers on the table headers represent the positions in the items sorting. The digits in table cells represent the numbers used for the identification of each menu item, ordered by the subject's supposed frequency of usage.

Table 2: Gathered data about SMS.

	1	2	3	4	5	6	7	8	A 3
S1	79	80	81	77	86	82	78	83	<i>(</i>
S2	83	79	90	86	80	88	89	81	
S3	83	80	78	87	79	77	90	82	
S4	83	87	79	88	78	80	77	89	
S5	83	80	82	79	87	77	78	90	
S6	83	80	87	78	82	79	88	90	
S7	83	80	79	82	87	77	88	78	
S8	83	82	90	87	79	80	84	86	
S9	80	83	87	79	78	90	82	88	
S10	83	80	79	87	78	88	82	86	
S11	77	80	83	78	86	87	82	79	
S12	83	80	78	89	77	87	88	79	
S13	83	80	78	87	79	82	90	77	
S14	83	78	80	87	90	82	88	79	

For instance, in Table 2 the number 79 in position 1 for the subject S1 means that subject S1 expects that feature  $n^{\circ}$  79 might be his/her most frequently used one, the 80 the second one, and so on.

By analyzing these data, we can gain insight on the subjects' mental models, depending on the different domains. In particular, we found that for well-established applications, such as Cell-Phone or SMS, subjects have comparable conceptual organizations. Indeed, let us observe that items in Table 2 were arranged by the various subjects in a very similar fashion. For instance, notice that features numbered 83 and 80 were placed at the beginning of the lists by almost all the subjects, since they suppose these features might be the most frequently used. Similarly, functions 79 and 87 appeared frequently in the 3<sup>rd</sup> and/or in the 4<sup>th</sup> positions, and so on.

Table 3: Gathered data about NAV.

	1	2	3	4	5	6	7	8	
S1	9	6	8	1	17	16	13	7	
S2	5	4	10	1	16	17	11	12	
S3	16	11	17	4	10	14	15	13	//
S4	3	11	16	4	12	13	14	15	\
S5	12	11	17	16	4	13	2	8	
S6	14	15	13	17	4	16	10	2	
S7	11	16	8	10	2	17	4	13	
S8	11	16	2	8	17	10	4	15	
S9	4	12	13	15	14	11	17	1	
S10	4	13	2	17	12	11	16	10	
S11	4	6	15	17	1	7	2	14	
S12	4	13	12	2	14	10	16	6	
S13	17	1	3	14	15	12	16	11	
S14	17	14	4	3	1	15	12	7	

On the other hand, when dealing with novel services, such as the services provided by a nextgeneration navigator, user's mental models and conceptual relationships between menu items are dissimilar, even when they received detailed task explanations prior to the test. By looking at items in Table 3, it is more difficult to find similarities in the arrangements proposed by the different subjects. Moreover, some subjects, such as S1 and S2, provided arrangements very far from the others, biasing the result of the mode and aggregative procedures. It is worth pointing out that these outliers are far from trivial to perceive, especially in large datasets, limiting the meaningfulness of the empirical data.

In order to provide UI designers with a formal tool to identify subjects that can disrupt the validity of the collected data, we are going to define, in the next section, a specific "distance" among subjects' arrangements, satisfying several peculiarities related to the problem we are dealing with.

## **3** AN EVALUATION FUNCTION

We are interested in "measuring" the "distances" between the collected permutations, i.e. to understand if a sequence is on the average very different from the others, implying that the corresponding subject cannot be considered affordable for that specific domain.

In order to define this measure, we have to clarify which relations among the elements in these permutations have to be considered relevant. When dealing with binary strings, the Hamming distance is the most natural and utilized one. Instead, for general permutations, in the literature there are many different interpretations of distance, according to the kind of problem they represent (Moraglio et al., 2004). For example, in some domains, the relevant information is the adjacency relation among the elements of a permutation; in others, the most significant factor is the position in which the elements of a permutation lie; in further contexts, permutations provide priority lists, and so the relevant information is the order of the elements of the permutations. An interesting survey of metrics on permutations is provided by (Huang, 1997). But, at best of our knowledge, none of the above described interpretations fits well our problem.

## **3.1 The Underlying Approach**

In our case, we have to give prominence to two factors:

- 1. the relative positions of the items in the same permutation, and
- 2. the distance between the position of an item in the  $i^{th}$  permutation and the position of the same item in the  $j^{th}$  one.

To clarify factor 1, let us recall that, in frequency-based menu organization, we are mainly interested in the items placed at the top of the sequence, which should be the most frequently used. For example, let us consider the following sequences:

Table 4: Example 1.

	1	2		n-1	n
S1	A				
S2	<		А	1	
S3				0	Α
-			.1		0

In agreement with the selection-frequency approach, the sequences provided by S1 and S2 are semantically much more "far" than the two sequences provided by S2 and S3, since the foremost positions in the menu, corresponding to the mostly used tasks, are much more relevant than the outermost ones. Factor 2 concerns the comparison of the positions where the same items are placed in the different permutations. Thus, in order to define a suitable distance between the permutations, we combine, in a single formula, the following aspects:

to make the foremost menu positions more relevant, we assign them *weights*, between 1 and 0, in a decreasing and non-linear way;

- to satisfy factor 2, we define a distance reporting the number of steps needed to go from the position of an item in a permutation, to the position of the same item in the other permutation we are examining;
- finally, in order to normalize the distance function to take values between 0 and 1, independently from the length of permutations, we multiply the result by a suitable factor. This allows us to compare sequences of different subsystems, independently of the number of menu items.

In the following we will describe these steps in a more formal way.

## 3.2 Weight and Distance Functions

To satisfy the requirement that the foremost positions have much more importance than the others, we consider the monotone decreasing function *rel* from the set of the positions  $P=\{1,...,N\}$  to the interval [0,1]:

$$el: k \in P \to 1/k \in [0, 1].$$
(1)

This function is a *fuzzy subset* (Zadeh, 1965) and we interpret the membership degree rel(k) of the element k as the "degree of relevancy" of the position k; we call *rel* the *fuzzy subset of relevant positions*. The function *rel* is suitable for our situation because it well represents the decreasing importance of the positions, in a non-linear trend.

In order to compare the positions corresponding to equal items in different permutations, we consider a distance between the position of an item in a sequence and the position of the same item in another sequence. Given an item, we denote by dthis distance and we define it, as

d

$$(k,h) = |k-h| \tag{2}$$

for every  $k, h \in P$ , where  $| \cdot |$  denotes the absolute value. In other words, the value d(k, h) indicates how many steps we have to do from the position k of an item in a permutation, to the position h, in which the same item is placed in the other permutation we are examining. Let us observe that, since we have a set of N positions, the maximum possible distance between two positions is N-1.

To clarify these concepts, let us consider the following example of a dataset:

Table 5: Example 2.

	1	2	 9	10
Si	А	В	 С	D
Sj	В	С	 А	D

We have a set of 10 items A, B,... to be arranged by subjects Si .. Sj. If we consider the item A, we observe that it is in position 1 in the sequence arranged by subject Si and in position 9 in the sequence arranged by subject S<sub>j</sub>. So we can evaluate the distance between these two permutations for the item A as d(1, 9) = |1-9|.

Now we have to combine the considered functions, in order to give a suitable expression for the distance between permutations.

## **3.3 The Resulting Fuzzy-based Distance**

Before proceeding, let us introduce some notations. Let us suppose that each module of the system for which we are defining the menu clustering has N menu items. We denote by I this set. The  $i^{th}$  subject arranges the items in a particular sequence, which can be viewed as a function from the set of the positions  $P=\{1,...,N\}$ , to the set of the items I:

$$s_i: k \in \{1, \dots, N\} \to s_i(k) \in I.$$
(3)

In other words, we identify the permutation produced by the subject Si with the function  $s_i$ .

By  $s_i(k)$  we indicate the item placed in the  $k^{th}$  position by the  $i^{th}$  subject. Let us underline that, since  $s_i$  is bijective, we can always consider the inverse image of an item  $s_i(k)$ . In this case, we have that  $s_i^{-1}(s_i(k))$  gives the position k in which the item  $s_i(k)$  is placed in the  $i^{th}$  sequence.

In the example we are considering (Table 4),  $s_i(1) = A$  and  $s_i^{-1}(s_i(9)) = s_i^{-1}(C) = 9$ .

Let us remark that we can move from the  $i^{th}$  permutation to the  $j^{th}$  one simply by the composition of  $s_j$  and the inverse of  $s_i$ . More precisely,  $s_i^{-1}(s_j(k))$  furnishes the position in the  $i^{th}$  sequence of the item  $s_j(k)$ , which is placed in the position k in the  $j^{th}$  sequence.

Now we can define, for every pair of permutations  $(s_i, s_j)$ , the distance

$$\frac{1}{2(N-1)\sum_{k=1}^{N} rel(k)} \sum_{k=1}^{N} rel(k) \left[d(k, s_{j}^{-1}(s_{i}(k))) + d(k, s_{i}^{-1}(s_{j}(k)))\right].$$
(4)

Let us also observe that in this expression, we consider both the distance  $d(k, s_j^{-1}(s_i(k)))$  between the positions k and  $s_j^{-1}(s_i(k))$  of the same item in the sequence  $s_i$  and in the sequence  $s_j$ , respectively, and the distance  $d(k, s_i^{-1}(s_j(k)))$  between the positions k and  $s_i^{-1}(s_j(k))$  of the same item in the sequence  $s_j$  and in the sequence  $s_i$ , respectively. Then, in order to make symmetric the distance D, we sum these two distances. As an example, in calculating the distance between  $s_i$  and  $s_j$  in Table 4, for the position 1, first we consider the distance d(1, 9) = |1-9|. Then, since  $s_j$ , we consider also the distance d(1, 2) = |1-2|.

Let us stress that if an item is fixed, i.e. if it lies in the same position k in both the permutations we are comparing, the  $k^{th}$  term in the sum vanishes, obviously. So *D* results reflexive, trivially.

Then we multiply each term of the sum of the distances d by the degree of relevancy of the position we are examining.

Finally, in order to normalize on the length of permutations, we multiply the result of the total sum by the factor  $\frac{1}{2(N-1)\sum_{k=1}^{N} rel(k)}$ . So the distance

takes always values between 0 and 1, obtaining just 0 for equal sequences. In this way we can compare sequences, independently of their length.

Again referring to the simple example of Table 4, let us evaluate the final distance D between the two sequences  $s_i$ , and  $s_j$ . We have to repeat for every position each step we examined and then to sum all the results. Finally we have to multiply by the factor

$$\frac{1}{2*9}*\frac{1}{\sum_{k=1}^{10}\frac{1}{k}}$$
 to normalize. At the end, we have  

$$D(s_i, s_j) = \frac{1}{2*9}*\frac{1}{2.93}[1(|1-9|+|1-2|) + \frac{1}{2}(|2-1|+|2-9|) + \frac{1}{2}(|2-1|+|2-9|) + \frac{1}{9}(|9-2|+|9-1|) + \frac{1}{10}(|10-10| + |10-10|)].$$
(5)

### 4 APPLYING THE FORMULA

In order to identify the outliers, the designer needs to calculate, for each permutation, its distance on the average from all the other ones. Then, (s)he may choose a threshold, depending on the considered context, to filter data. An example applied on our data is provided in the following. We applied the proposed distance on the data gathered by the empirical studies described in Section 2. In Table 6 we provide the mean distances among the permutations. As expected, it resulted that for well known domains, such as the SMS or the CD modules, the permutations provided by the different subjects were very close (mean 0.286 and 0.237 respectively). On the other hand, the mean distance for the navigator is 0.446, which is almost the double of the other modules. Moreover, the distance allowed us to discern the outlier subjects. For instance, we choose a threshold value of 0.3 for Audio and SMS modules and 0.5 for the navigator one. Consequently subjects s1 and s2 were discarded both for NAV and SMS data, having high mean distances. S11 was not considered for the SMS,

while S4 and S13 were discarded in the Audio module.

	Audio - CD	SMS	NAV
S1	0.4	0.446	0.623
S2	0.226	0.322	0.525
S3	0.220	0.169	0.370
S4	0.336	0.256	0.479
S5	0.219	0.177	0.419
S6	0.223	0.179	0.419
S7	0.219	0.172	0.433
S8	0.234	0.279	0.431
S9	0.208	0.204	0.394
S10	0.263	0.182	0.384
S11	0.250	0.325	0.444
S12	0.234	0.224	0.417
S13	0.751	0.167	0.477
S14	0.225	0.211	0.427
Mean	0.286	0.237	0.446

Table 6: Results on the gathered data.

## 4.1 A Supporting Tool

To simplify the evaluation of these distances, we developed a specific tool, named *Distance-o-Meter*, quite trivial to use.



Figure 1: A screenshot of the developed tool.

Starting from a CSV file, storing the dataset of the permutation, the designer can either calculate the distance of a specific subject from all others, or let the tool calculate all the distances among subjects. Moreover, it allows the designer to specify a limit to filter subjects, which can be easily adjusted through a slider. Figure 1 shows the tool's UI (left) and how the tool highlights the subjects within the threshold of 0.5 (right). The tool can be freely downloaded at http://193.205.186.31/DataAnalysis.

# 5 CONCLUSIONS AND FUTURE WORK

To define a significant menu clustering it is a common practice to involve a number of final users in the menu design process. However, in novel application domains this approach can sometimes provide imprecise results if some subjects have weak mental models about the considered tasks. In this paper we presented a formal tool to support the menu designers in identifying the validity of subjects' conceptual models. To address this issue, we defined a "fuzzy-based" distance function between the different arrangements of the tasks, empirically produced by the different subjects. In particular, since we are considering a frequencybased menu organization, the proposed distance takes into account the fact that the foremost positions in an arrangement are more "important" than the others. Indeed, we used a function that assigns a decreasing "relevance" to the positions in an arrangement.

Thanks to this defined measure, a UI designer can compare the different menu items arrangements provided by the subjects. If a distance is over a selected threshold, then the relative subject can be considered an outlier. Such a filtering can be easily calculated by using a tool (freely downloadable) we developed, which is able to analyze a dataset containing subjects' answers, and to highlight abnormal situations.

We successfully applied this distance to discern significant subjects' trials when defining a nextgeneration automotive telematics system. About future work, we are currently devoting efforts at defining a distance on the dendograms obtained by agglomerative psychological clustering procedures.

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