DISCRETE GENETIC ALGORITHM AND REAL ANT COLONY OPTIMIZATION FOR THE UNIT COMMITMENT PROBLEM

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Keywords: Metaheuristics, unit commitment, ant colony, genetic algorithm, scheduling.

Abstract: In this paper, a cooperative metaheuristic for the solution of the Unit Commitment problem is presented. This problem is known to be a large scale, mixed integer problem. Due to combinatorial complexity, the exact solution is often intractable. Thus, a metaheuristic based method has to be used to compute a near optimal solution with low computation times. A new approach is presented here. The main idea is to couple a genetic algorithm to compute binary variables (on/off status of units), and an ant colony based algorithm to compute real variables (produced powers). Finally, results show that the cooperative method leads to the tractable computation of a satisfying solution for medium scale Unit Commitment problems.

1 INTRODUCTION

The Unit Commitment problem is a mixed integer problem, referring to the optimal scheduling of several production units, satisfying consumer's demand and technical constraints. Integer variables are the on/off status of production units, and real variables are produced powers. Numerous methods have been applied; see (Sen and Kothari, 1998).

The first idea is to use an exact solution method: exhaustive enumeration, "Branch and Bound" (Chen and Wang, 1993), dynamic programming (Ouyang and Shahidehpour, 1991). Due to temporal coupling of constraints (time up / time down constraints), a large temporal horizon is required, leading to a large number of binary variables: exact methods suffer from combinatorial complexity. Approximated methods are required for tractable results.

Deterministic approximated methods have been tested: priority lists in (Senjyu, et al., 2004) or expert systems. Due to numerous constraints, this kind of methods are often strongly suboptimal. Constraints are considered by the Lagrangian relaxation method, see (Zhai and Guan, 2002). Multi unit coupling constraints are relaxed. As a result, the unit Commitment problem is divided into several smaller optimization problems. However, due to the non convexity of the objective function, no guarantee can be given on the duality gap and the actual optimality of the solution. Further, an iterative procedure has to be used: solution of the optimization problems with fixed Lagrange multipliers, updates of these multipliers, and so on. This update can be performed with genetic algorithms as in (Cheng, et al., 2000) or by subgradient methods (Dotzauer, et al., 1999).

Stochastic approximated algorithms, called metaheuristics are potentially interesting methods for Unit Commitment as they are able to compute near optimal solutions with low computation times. A simulated annealing approach is used in (Yin Wa Wong, 1998), tabu search is used in (Rajan and Mohan, 2004) and genetic algorithms are used in (Kasarlis, *et al.*, 1996). Cooperative algorithms have been developed to couple the advantages of several optimization methods: genetic algorithms and simulated annealing are used in (Cheng, et al., 2002); simulated annealing and local search in (Purushothama and Jenkins, 2003).

In (Serban and Sandou, 2007), a mixed ant colony method has been proposed. The approach is interesting, but, due to the positive feedback of ant colony, may quickly converge to local minima. To circumvent this problem, a new cooperative strategy is defined in this paper. The idea is to use a knowledge based genetic algorithm for binary variables to achieve a deep exploration of the search space, and simultaneously an ant colony based algorithm for real variables.

The paper is organized as follows. In section 2, the Unit Commitment problem is briefly called up.

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Sandou G. (2007). DISCRETE GENETIC ALGORITHM AND REAL ANT COLONY OPTIMIZATION FOR THE UNIT COMMITMENT PROBLEM. In Proceedings of the Fourth International Conference on Informatics in Control, Automation and Robotics, pages 256-261 DOI: 10.5220/0001641602560261 Copyright © SciTePress

The cooperative metaheuristic ant colony/genetic algorithm method is depicted in section 3. Both algorithms are described, together with the definition of a criterion guaranteeing feasibility of the solution. Numerical results are given in section 4. Finally, concluding remarks are drawn in section 5.

2 UNIT COMMITMENT PROBLEM

The Unit Commitment problem is a classical large scale mixed integer optimization problem. Following notations are used throughout the paper:

- *N*: length of time horizon,
- *n*: (subscript) : time interval number *n*,
- *K*: number of production unit,
- *k* (superscript): production unit number *k*,
- u_n^k : on/off status of production unit k during time interval n (binary variable),
- Q_n^k : power produced by production unit k during time interval n (real variable).

2.1 Cost Function

The objective function is the sum of production, start-up, and shut-down costs for all time intervals and all units:

$$\min_{\substack{\{\mu_n^k, \mathcal{Q}_n^k\}\\n=1}} \sum_{n=1}^N \left(\sum_{k=1}^K \left(c_{prod}^k \left(\mathcal{Q}_n^k, u_n^k \right) + c_{on/off}^k \left(u_n^k, u_{n-1}^k \right) \right) \right), \quad (1)$$

where production cost of unit *k* can be expressed by: $c_{prod}^{k}(Q_{n}^{k}, u_{n}^{k}) = \alpha_{2}^{k}(Q_{n}^{k})^{2} + \alpha_{1}^{k}Q_{n}^{k} + \alpha_{0}^{k}u_{n}^{k},$ (2)

start-up cost and shut-down costs are: $c_{on/off}^{k}(u_{n}^{k}, u_{n-1}^{k}) =$

$$c_{on/off}^{k} (u_{n}^{k}, u_{n-1}^{k}) = c_{on}^{k} u_{n}^{k} (1 - u_{n-1}^{k}) + c_{off}^{k} u_{n-1}^{k} (1 - u_{n}^{k}),$$
(3)

and α_2^k , α_1^k , α_0^k , c_{on}^k and c_{off}^k are technical data of production unit *k*.

2.2 Constraints

Constraints are:

Capacity constraints

$$Q_{\min}^k u_n^k \le Q_n^k \le Q_{\max}^k u_n^k \tag{4}$$

Consumers' demand satisfaction

$$\sum_{k=1}^{K} \mathcal{Q}_{n}^{k} \ge \mathcal{Q}_{n}^{dem} \tag{5}$$

• Time up and time down constraints

$$(u_{n-1}^{k} = 0, u_{n}^{k} = 1)$$

$$\Rightarrow \left(u_{n+1}^{k} = 1, u_{n+2}^{k} = 1, \cdots, u_{n+T_{up}^{k}-1}^{k} = 1\right)$$

$$(u_{n-1}^{k} = 1, u_{n}^{k} = 0)$$

$$\Rightarrow \left(u_{n+1}^{k} = 0, u_{n+2}^{k} = 0, \cdots, u_{n+T_{down}^{k}-1}^{k} = 0\right)$$
(6)

Such constraints are temporally coupling constraints which express dynamics on production units. Q_{\min}^k , Q_{\max}^k , T_{up}^k and T_{down}^k are technical data.

3 COOPERATIVE METAHEURISTIC SOLUTION

3.1 Algorithm Principles

As already mentionned, Unit Commitment is a large scale mixed integer programming problem. Genetic algorithm is a well known algorithm for combinatorial optimization problems. In this study, a specific criterion is defined (see section 3.2), based on particular penalty functions to guarantee the solution feasibility. Genetic algorithm is used to compute binary variables and is depicted in section 3.3. Further, a stochastic algorithm is simultaneously used to compute real variables, based on ant colony optimization. It is presented in section 3.4.

3.2 Optimization Criterion

3.2.1 Criterion Expression

Consider that a feasible solution is known with a cost c^{f} . The following optimization criterion is defined:

$$\min_{\substack{=(u_n^k, Q_n^k)\\ i=1, \cdots, N\\k=1, \dots, K}} \left(\sum_{n=1}^N \sum_{k=1}^K \left(c_{prod}^k (Q_n^k, u_n^k) + c_{on/off}^k (u_n^k, u_{n-1}^k) \right) + ((1+\varepsilon) c^f + h(y)).B(y) + \right),$$
(7)

where:

• ε is a small positive real,

h(y) is a penalty function for non feasible solutions,

B(y) is a boolean function (1 for non feasible solutions and 0 for feasible ones).

With this criterion, any unfeasible solution has a higher cost than the feasible known solution: any unconstrained optimization algorithm can solve the problem. Thus, an elitist genetic algorithm can be used. The definition of criterion (7) only supposed that a feasible solution is known. It can be easily computed using a simple priority list. This is a very suboptimal solution, but the quality of this first feasible solution is not crucial, as the criterion can be updated when new feasible solutions are known.

3.2.2 Penalty Expression

The following variables are added:

$$\delta_n^k = u_n^k (1 - u_{n-1}^k)$$

$$\varepsilon_n^k = u_{n-1}^k (1 - u_n^k)$$
(8)

With these variables, time-up and time-down constraints are expressed by linear expressions:

$$\delta_n^k = 1 \Longrightarrow (u_{n+1}^k = 1, \dots, u_{n+T_{up}^k-1}^k = 1)$$

$$\Leftrightarrow \sum_{j=0}^{T_k^{up}-1} u_{n+j}^k \ge T_{up}^k \delta_n^k$$
(9)

$$\varepsilon_n^k = 1 \Longrightarrow (u_{n+1}^k = 0, \dots, u_{n+T_{down}^k}^k = 0)$$

$$\Leftrightarrow \sum_{i=0}^{T_k^{down} - 1} (1 - u_{n+j}^k) \ge T_{down}^k \varepsilon_n^k$$
(10)

Capacity constraints and consumers' demands satisfaction are linear. All constraints can be expressed by a linear equation, $A_c x \le B_c$, where x is $(u_n^k, Q_n^k, \delta_n^k, \varepsilon_n^k; n = 1, ..., N; k = 1, ..., K)^T$, leading to a high tractability of the boolean and the penalty functions computation.

3.3 Genetic Algorithm for on/off Variables

3.3.1 Algorithm Principles

Genetic algorithm is a well known optimization method. Fig. 1 and 2 represent classical cross-over and mutation operators for Unit Commitment problem.

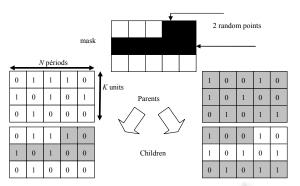


Figure 1: Classical crossing over operator.



Figure 2: Classical mutation operator.

Individuals are in a matrix form. Crossover operator create 2 potentially low cost children from 2 parents by merging their variables (or genes). The mutation operator allows the introduction of new genes in the population by randomly changing one of the variables. Finally, the selection operator is performed with a classical biased roulette method.

3.3.2 Knowledge Based Operators

It has been observed that the genetic algorithm can be more efficient by using some knowledge based operators. New genetic operators are added, considering properties of the problem. The first operator is a "selective mutation operator". Consider unit scheduling of fig. 3. Due to time-up and timedown constraints, a classical mutation leads very often to an infeasible solution. To increase the probability of reaching a new feasible point, a "selective mutation operator" is introduced: this operator detects switching times and allows a random mutation only for these genes.

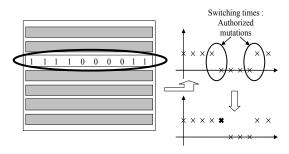


Figure 3: Selective mutation operator.

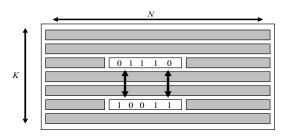


Figure 4: Exchange operator.

The second operator is an exchange operator, introduced by (Kasarlis, et al., 1996). Some production units are profitable or have larger capacities. It may be interesting to exchange a part of the planning of two production units (see fig. 4).

Finally, all-on and all-off operator are introduced. Consider fig. 5. If the unit has a time down constraints of two hours, it may be difficult to go from feasible point a) to feasible point b). The all-on (resp. all-off) operator randomly select two time intervals and a production unit and switch on (resp. switch off) the production unit between these time intervals: the idea is to increase the probability of "crossing the infeasible space".

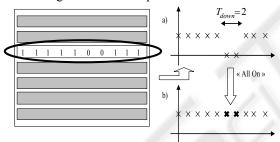


Figure 5: All-on operator.

3.4 Continuous Ant Colony Optimization for Produced Powers

Ant colony optimization was firstly introduced by Marco Dorigo. Ants' behaviour has been used as a metaphor to design algorithms for combinatorial optimization problems such as the Travelling Salesman Problem (Dorigo, et al. 1997). Extensions for continuous search spaces have been proposed by (Socha and Dorigo, 2006) and have been used in (Serban and Sandou, 2007) in a pure ant colony solution of Unit Commitment. Results are here called up. For each binary solution, $U = (u_n^k; n = 1, ..., N; k = 1, ..., K)$, real values Q = $(Q_n^k; n = 1, ..., N; k = 1, ..., K) = (x^1, ..., x^{KN})$ have to be associated. To compute these real variables, a

matrix **T** of *s* real solutions, called "archive matrix of solutions", is stored:

$$\mathbf{T} = \begin{bmatrix} x_1^1 & x_1^2 & \dots & x_1^i & \dots & x_1^{KN} \\ x_2^1 & x_2^2 & \dots & x_2^i & \dots & x_2^{KN} \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ x_j^1 & x_j^2 & \dots & x_j^i & \dots & x_j^{KN} \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ x_s^1 & x_s^2 & \dots & x_s^i & \dots & x_s^{KN} \end{bmatrix}.$$
(11)

These solutions are evaluated with respect to the objective function (1). Costs are stored in **H**:

$$\mathbf{H} = \begin{bmatrix} f_1 & f_2 & \dots & f_j & \dots & f_s \end{bmatrix}^T \text{, with}$$

$$f_j = f(U_j, Q_j) = \sum_{n=1}^N \left(\sum_{k=1}^K \begin{pmatrix} c_{prod}^k(Q_n^k, u_n^k) + \\ c_{on/off}^k(u_n^k, u_{n-1}^k) \end{pmatrix} \right).$$
(12)

The solutions are sorted according to their costs. From these costs, weights are defined according to the ranks of the solutions in the matrix. For the solution with rank r, the weight is defined by:

$$\omega_r = \frac{1}{qs\sqrt{2\pi}} e^{-\frac{(r-1)^2}{2q^2s^2}}.$$
 (13)

Finally, a discrete probability distribution is defined from these weights:

$$\omega_r = \omega_r / \sum_{j=1}^{s} \omega_j \tag{14}$$

q is a tuning parameter of the algorithm. To compute a new real solution, the following procedure is performed:

- a "model ant", say *l*, is chosen, according to this discrete probability distribution (14).
- Each real variable x_{new}^i , i = 1,...,KN, is chosen with a Gaussian probability whose mean and standard deviation is computed by:

$$\mu_{new}^{i} = x_{l}^{i}$$

$$\sigma_{new}^{i} = \frac{\xi}{s-1} \sum_{m=1}^{s} |x_{m}^{i} - x_{l}^{i}|.$$
(15)

 ξ is also a tuning parameter of the algorithm. When real variables have been chosen, consumer's demands (5) may not be fulfilled. Furthermore, the selection of produced powers may lead to overproduction. To get rid of these problems, the following improvement procedure is used:

- Select Q_n^k with the previous algorithm.
- If $\sum_{k=1}^{K} Q_n^k u_n^k > Q_n^{dem}$ (resp. <), then randomly choose, if possible, one of switched on units, and decrease (resp. increase) the corresponding produced power until

 $\sum_{k=1}^{K} Q_n^k u_n^k = Q_n^{dem}$. If it is not sufficient,

choose several production units, if possible.

When all new solutions have been computed, the best new solutions are stored in matrix \mathbf{T} , replacing solutions whose costs were too high. This is an analogy with physical evaporation of pheromone.

4 NUMERICAL RESULTS

4.1 Algorithm Implementation

The proposed cooperative method has been tested with Matlab 6.5 with a Pentium IV 2.5 GHz. When the stochastic cooperative algorithm is completed, a final local search is performed: binary values are set to their final values, and a real optimization based on Semi Definite Programming is performed to solve this particular economic dispatch problem. As stochastic algorithms are considered, 70 tests are performed, and statistical data about the results are given. Optimization horizon is 24 hours with a sampling time of one hour.

4.2 "4 unit" Academic Example

A 4 unit case is considered (see table 1).

	$\begin{array}{c} Q_{\min} \\ (MW) \end{array}$	$Q_{\rm max}$ (MW)	α₀ (€)	α_1	C_{on} (€)	c_{off} (€)	T_{down} (h)	T_{up} (h)
1	10	40	25	2.6	10	2	2	4
2	10	40	25	7.9	10	2	2	4
3	10	40	25	13.1	10	2	3	3
4	10	40	25	18.3	10	2	3	3

Table 1: Characteristics for the "4 unit case".

At time 0, all units are switched off and can be switched on. Note that linear costs have been chosen $(\alpha_2 = 0)$. For this relative small scale cases, and for linear costs, an exact solution has been computed by "Branch and Bound". Consumer's demand is depicted in fig. 6. This demand can be fulfilled by 2 production units (see 2 units limit in fig. 6), except for hour number 9. Because of time up constraints this unit will be switched on for 3 hours. The optimal solution is given in fig. 7.

The corresponding optimization problem is made of 96 binary variables (24 hours and 4 units) and 96 real variables. Table 2 shows results of optimization. Statistical results are given: best case, mean, number of success (a test is successful if the best solution is found).

The following parameters were used:

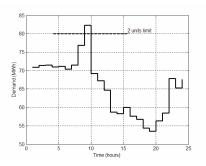


Figure 6: Consumer's demand.

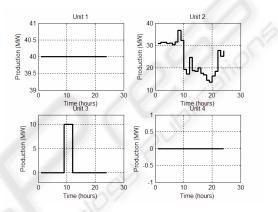


Figure 7: Optimal solution for "4 unit case".

- Genetic population size: 50,
- Cross-over rate: 70%,
- Mutation rate: 5%,
- Knowledge based operators rate: 10%,
- Archive matrix size: s = 20,
- Tuning parameters $q = 1; \xi = 0.8$.

Results show that interesesting solutions can be computed with relatively low computation times.

Case	Best	Mean	Nb.	Time
			Success	
100 iter.	8778€	9449€	8/70	22 s
	(+0%)	(+7.6%)		
200 iter.	8778€	9004 €	32/70	45 s
	(+0%)	(+2.6%)		
500 iter.	8778€	8922€	45/70	115 s
	(+0%)	(+1.6%)		

4.3 Medium Scale Case

A "10 unit" case is now considered (see table 3). This a medium scale case. Low start up and start down costs have been considered, leading to the possibility of guessing the optimal solution. The corresponding optimal cost is $29795 \in$. For a 24 hour optimization, this problem is made of 240 binary

optimization variables and 240 real variables. Results for the cooperative method are given in table 4. As in previous examples, 70 tests are performed and statistical results are given (best case, mean). The same values were used for parameters.

	Q_{\min}	Q_{\max}	α_0	α_1	C_{on}	C_{off}	T_{dow}	T_{up}
	MW	MW	€		€	€	"h	h
1	10	40	25	2.6	10	2	2	4
2	10	40	25	5.2	10	2	2	4
3	10	40	25	7.9	10	2	3	6
4	10	40	25	10.5	10	2	3	6
5	10	40	25	13.1	10	2	3	4
6	10	40	25	15.7	10	2	3	4
7	10	40	25	18.3	10	2	3	4
8	10	40	25	21.0	10	2	3	4
9	10	40	25	23.6	10	2	3	4
10	10	40	25	26.2	10	2	3	4

Table 3: Characteristics for the "10 unit case".

Results show the viability of the cooperative method to solve mixed integer optimization problems. Low computation times are observed, even for this medium scale case.

Table 4: Optimization results "10 unit case".

	Best	Mean	Time
500 iter.	30210€	32695€	275 s
	(+1.4%)	(+9.7%)	
1000 iter.	29851€	32138€	550 s
	(+0.2%)	(+7.8%)	

5 CONCLUSION

In this paper, a cooperative method ant colony/genetic algorithm for Unit Commitment solution has been proposed. The main idea is to use a genetic algorithm with knowledge based operators to compute binary variables and a real ant colony algorithm to compute real variables. To guarantee the feasibility of the final solution, a criterion has also been defined. Finally, the proposed method leads to near optimal solutions, with guarantees of feasibility and with low computation times.

Some dedicated methods are able to find better solutions than the proposed cooperative algorithm, and can consider larger scale cases. However, this cooperative method seems to be promising and the study has proven its viability.

Forthcoming works deal with the use of such a cooperative metaheuristic method to solve generic non linear mixed integer optimization problems, as the use of the method does not require any structural property of the problem.

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