

# Combining Selective-Presentation and Selective-Learning-Rate Approaches for Neural Network Forecasting of Stock Markets

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**Abstract.** We have investigated selective learning techniques for improving the ability of back-propagation neural networks to predict large changes. We previously proposed the *selective-presentation* approach, in which the training data corresponding to large changes in the prediction-target time series are presented more often, and *selective-learning-rate* approach, in which the learning rate for training data corresponding to small changes is reduced. This paper proposes combining these two approaches to achieve fine-tuned and step-by-step selective learning of neural networks according to the degree of change. Daily stock prices are predicted as a noisy real-world problem. Combining these two approaches further improved the performance.

## 1 Introduction

Prediction using back-propagation neural networks has been extensively investigated (e.g., [1-5]), and various attempts have been made to apply neural networks to financial market prediction (e.g., [6-16]), electricity load forecasting (e.g., [17]) and other areas. In the usual approach, all training data are equally presented to a neural network (i.e., presented in each cycle) and the learning rates are equal for all the training data independently of the size of the changes in the prediction-target time series. Also, network learning is usually stopped at the point of minimal mean squared error between the network's outputs and the desired outputs.

Generally, the ability to predict large changes is more important than the ability to predict small changes, as we mentioned in the previous paper [12]. When all training data are presented equally with an equal learning rate, the BPNN will learn the small and large changes equally well, so it cannot learn the large changes more effectively. We have investigated selective learning techniques for improving the ability of neural networks to predict large changes. We previously proposed the *selective-presentation* and *selective-learning-rate* approaches and applied them into stock market prediction [12-14]. In the *selective-presentation* approach, the training data corresponding to large changes in the prediction-target time series are presented more often. In the *selective-learning-rate* approach, the learning rate for training data corresponding to small changes is reduced. The previous paper [12] also investigated another stopping criterion for financial predictions. Network learning is stopped at the point having the

maximum profit through experimental stock-trading.

This paper proposes combining the *selective-presentation* and *selective-learning-rate* approaches. By combining these two approaches, we can easily achieve fine-tuned and step-by-step selective learning of neural networks according to the degree of change. Daily stock prices are predicted as a noisy real-world problem.

## 2 Combining Selective-Presentation and Selective-Learning-Rate Approaches

To allow neural networks to learn about large changes in prediction-target time series more effectively, we separate the training data into large-change data (L-data) and small-change data (S-data). L-data (S-data) have next-day changes that are larger (smaller) than a preset value.

In the *selective-presentation* approach, the L-data are presented to neural networks more often than S-data. For example, all training data are presented every fifth learning cycle, while the L-data are presented every cycle. In the *selective-learning-rate* approach, all training data are presented in every cycle; however, the learning rate of the back-propagation training algorithm for S-data is reduced compared with that for L-data. These two approaches are outlined as follows.

### ***Selective-Presentation Approach***

1. Separate the training data into L-data and S-data.
2. Train back-propagation networks with more presentations of L-data than of S-data.
3. Stop network learning at the point satisfying a certain stopping criterion (e.g., stop at the point having the maximum profit).

### ***Selective-Learning-Rate Approach***

1. Separate the training data into L-data and S-data.
2. Train back-propagation networks with a lower learning rate for the S-data than for the L-data.
3. Stop network learning at the point satisfying a certain stopping criterion (e.g., stop at the point having the maximum profit).

We combine these two approaches to achieve fine-tuned and step-by-step learning of neural networks according to the degree of change. The outline is as follows.

### **Combining *Selective-Presentation* and *Selective-Learning-Rate* Approaches**

1. Separate the training data into L-data and S-data.
2. Separate L-data into two subsets: L1-data and L2-data, where changes in L2- data are larger than those in L1-data.
3. Separate S-data into two subsets: S1-data and S2-data, where changes in S2-data are larger than those in S1-data.
4. Train back-propagation networks with more presentations of L1- and L2-data than of S1- and S2-data, and with a lower learning rate for L1- and S1-data than for L2 and S2-data.
5. Stop network learning at the point satisfying a certain stopping criterion (e.g., stop

at the point having the maximum profit).

In general, we can separate the training data into  $N$  subsets ( $N \geq 2$ ):  $D_1$ -,  $D_2$ -, ..., and  $D_N$ -data, where changes in  $D_i$ -data are larger than those in  $D_{i-1}$ -data, and give "selective intensities"  $I$  (number of presentations times learning rate) to  $D_1$ -,  $D_2$ -, ..., and  $D_N$ -data as  $I_1 < I_2 < I_3 < \dots < I_N$ .

### 3 Evaluation through Experimental Stock-Price Prediction

We considered the following types of knowledge for predicting Tokyo stock prices. These types of knowledge involve numerical economic indicators [12-14].

1. If interest rates decrease, stock prices tend to increase, and vice versa.
2. If the dollar-to-yen exchange rate decreases, stock prices tend to decrease, and vice versa.
3. If the price of crude oil increases, stock prices tend to decrease, and vice versa.

We used the following five indicators as inputs to the neural network.

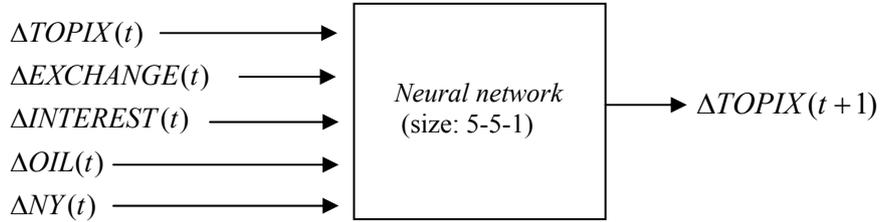
- TOPIX: the chief Tokyo stock exchange price index
- EXCHANGE: the dollar-to-yen exchange rate (yen/dollar)
- INTEREST: an interest rate (3-month CD, new issue, offered rates) (%)
- OIL: the price of crude oil (dollars/barrel)
- NY: New York Dow-Jones average of the closing prices of 30 industrial stocks (dollars)

TOPIX was the prediction target. EXCHANGE, INTEREST and OIL were chosen based on the knowledge of numerical economic indicators. The Dow-Jones average was used because Tokyo stock market prices are often influenced by New York exchange prices. We assume that tomorrow's change in TOPIX is determined by today's changes in the five indicators according to the knowledge. Therefore, the daily changes in these five indicators (e.g.  $\Delta \text{TOPIX}(t) = \text{TOPIX}(t) - \text{TOPIX}(t-1)$ ) were input into neural networks, and the next-day's change in TOPIX was presented to the neural network as the desired output (Figure 1). The back-propagation algorithm was used to train the network. All the data of the daily changes were scaled to the interval [0.1, 0.9]. A 5-5-1 multi-layered neural network was used (five neurons in the input layer, five in the hidden layer, and one in the output layer).

#### 3.1 Experiments

We used data from a total of 409 days (from August 1, 1989 to March 31, 1991): 300 days for training, 30 days for validation (making decisions on stopping the network learning), and 79 days for making predictions. In Experiment 1, all training data were presented in each cycle with an equal learning rate ( $\varepsilon = 0.7$ ). In Experiment 2, L-data were presented five times as often as S-data. Here, the large-change threshold was 14.78 points (about US\$ 1.40), which was the median of absolute value of TOPIX

daily changes in the training data. In Experiment 3, the learning rate for the S-data was reduced up to 20% (i.e.,  $\varepsilon = 0.7$  for the L-data and  $\varepsilon = 0.14$  for the S-data). Experimental conditions in Experiments 1, 2, and 3 are shown in Table 1, 2, and 3.



**Fig. 1.** Neural prediction model.

**Table 1.** Experimental conditions in Experiment 1: conventional technique.

	S-data	L-data
Range of absolute value of $\Delta$ TOPIX(t)	0 to 50%	50 to 100%
Number of data	150	150
Relative number of presentations ( $P$ )	1	1
Learning rate ( $\varepsilon$ )	0.7	0.7
$P$ times $\varepsilon$ (relative value)	0.7 (1)	0.7 (1)

**Table 2.** Experimental conditions in Experiment 2: selective presentation.

	S-data	L-data
Range of absolute value of $\Delta$ TOPIX(t)	0 to 50%	50 to 100%
Number of data	150	150
Relative number of presentations ( $P$ )	1	5
Learning rate ( $\varepsilon$ )	0.7	0.7
$P$ times $\varepsilon$ (relative value)	0.7 (1)	3.5 (5)

**Table 3.** Experimental conditions in Experiment 3: selective-learning-rate.

	S-data	L-data
Range of absolute value of $\Delta$ TOPIX(t)	0 to 50%	50 to 100%
Number of data	150	150
Relative number of presentations ( $P$ )	1	1
Learning rate ( $\varepsilon$ )	0.14	0.7
$P$ times $\varepsilon$ (relative value)	0.14 (1)	0.7 (5)

Experimental conditions in Experiment 4 are shown in Table 4. S-data were separated into S1- and S2-data, where changes in S2-data were larger than those in S1-data. Here, the boundary between S1- and S2-data was at the 25% point. (The 25% point means that 25% of the data is between the minimum data and the 25% point data. The 50% point corresponds to the “median.”) L-data were separated into L1- and L2-data, where changes in L2-data were larger than those in L1-data. Here, the boundary between L1- and L2-data was the 75% point. The 25%, 50%, and 75% points were 5.36 (about US\$ 0.51), 14.78 (US\$ 1.40) and 31.04 points (US\$ 2.94), respectively. L1-, L2-, S1-, and S2-data each had 75 data. In Experiment 4, L1- and L2-data were presented five times as often as S1- and S2-data. In Experiment 4, the learning rate for L1- and S1-data was reduced to 50% (i.e.,  $\varepsilon = 0.7$  for L2- and S2-data, and  $\varepsilon = 0.35$  for L1- and S1-data). Relative *selective intensities* (number of presentations times learning rate) for S1-, S2-, L1-, and L2-data were 1, 2, 5, and 10, respectively.

**Table 4.** Experimental conditions in Experiment 4: the hybrid technique.

	S1-data	S2-data	L1-data	L2-data
Range of absolute value of $\Delta \text{TOPIX}(t)$	0 to 25%	25 to 50%	50 to 75%	75 to 100%
Number of data	75	75	75	75
Relative number of presentations ( $P$ )	1	1	5	5
Learning rate ( $\varepsilon$ )	0.35	0.7	0.35	0.7
$P$ times $\varepsilon$ (relative value)	0.35 (1)	0.7 (2)	1.75 (5)	3.5 (10)

In each experiment, network learning was stopped at the point having the maximum profit (the learning was stopped at the point having the maximum profit for the validation data during 8000 learning cycles). The prediction error and profit were monitored after every hundred learning cycles.

When a large change in TOPIX was predicted, we tried to calculate “Profit” as follows: when the predicted direction was the same as the actual direction, the daily change in TOPIX was earned, and when it was different, the daily change in TOPIX was lost. This calculation of profit corresponds to the following experimental TOPIX trading system. A buy (sell) order is issued when the predicted next-day's up (down) in TOPIX is larger than a preset value which corresponds to a large change. When a buy (sell) order is issued, the system buys (sells) TOPIX shares at the current price and subsequently sells (buys) them back at the next-day price. Transaction costs on the trades were ignored in calculating the profit. The more accurately a large change is predicted, the larger the profit is.

In each experiment, the momentum parameter  $\alpha$  was 0.7. All the weights and biases in the neural network were initialized randomly between -0.3 and 0.3. In each experiment the neural network was run four times for the same training data with different initial weights and the average was taken.

### 3.2 Results

The experimental results are shown in Table 5. Multiple regression analysis (MR) was also used in the experiments. The “prediction error on large-change test data” is the mean absolute value of the prediction error for the test L-data.

Applying our *selective-presentation* approach (Experiment 2) reduced the prediction error for test L-data and improved profits: the prediction-error on L-data was reduced by 7% (1- (21.3/22.9)) and the network’s ability to make profits through experimental TOPIX-trading was improved by 30% (550/422) compared with the results obtained with the usual presentation approach (Experiment 1).

The prediction error and profits in Experiment 3 (*selective-learning-rate* approach) were comparable to those in Experiment 2 (*selective-presentation* approach). Combining *selective-presentation* with *selective-learning-rate* approaches (Experiment 4) further reduced the prediction error for test L-data and improved profits: the prediction-error was reduced by 10% (1- (20.7/22.9)) and the network’s ability to make profits was improved by 38% (581/422).

**Table 5.** Experimental results.

	MR	Exp. 1	Exp. 2	Exp. 3	Exp. 4
Presentation method	equal	equal	<i>selective</i>	equal	<i>selective</i>
Learning rate		equal	equal	<i>selective</i>	<i>selective</i>
Prediction error for large-change data (relative value)	24.3 (1.06)	<u>22.9</u> (1)	21.3 (0.93)	21.3 (0.93)	<u>20.7</u> (0.90)
Profit on test data (relative value)	265 (0.62)	<u>422</u> (1)	550 (1.30)	563 (1.33)	<u>581</u> (1.38)

## 4 Conclusions

We investigated selective learning techniques for forecasting. In the first approach, training data corresponding to large changes in the prediction-target time series are presented more often, in the second approach, the learning rate for training data corresponding to small changes is reduced, and in the third approach, these two techniques are combined. The results of several experiments on stock-price prediction showed that the performances of *selective-presentation* and *selective-learning-rate* approaches were both better than the usual presentation approach, and combining them further improved the performance. Next, we will apply these techniques today’s stock market and other real-world forecasting problems. We also plan to develop a forecasting method that integrates statistical analysis with neural networks.

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