

# Modeling Multi-agent Logistic Process System using Hybrid Automata

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**Abstract.** Multi-agent systems are a widely accepted solution to handle complex problems. One application of multi-agent system is autonomous logistics. In autonomous logistic processes, potentially every element in a logistic supply chain is modeled as cooperating software agent. Thus, there exist modeling languages that are used to model such multi-agent systems. However, these modeling languages do not allow verifying the properties of systems. Hybrid automata can be used to model hybrid systems by capturing both discrete and continuous changes of a system. Fortunately, hybrid automata are equipped with formal semantics that make formal methods possible to apply to them in order to prove certain properties of the specified systems. In this paper, we model multi-agent system behaviors in autonomous logistic processes using the concept of hybrid automata. With the help of model checking techniques, we can prove some properties of a modeled system before involving in the implementation of a system.

## 1 Introduction

Software agents and multi-agent systems (MAS) are an approach to implementing autonomous and interacting software systems. An agent is an autonomous decision maker on behalf of some real world entity. Generally, agents are able to perceive from their environment with sensors, and to act with actuators. The agents choose their action as because of a reasoning process. In particular, agents in multi-agent system are able to communicate and coordinate with each other to fulfill tasks in cooperation or competition depending on their respective goals and abilities. This enables them to solve complex problems and tasks in a distributed way [9].

There are several approaches for modeling multi-agent system like [11], [12]. Among of them, Agent UML [1] is one of the widely accepted languages for modeling multi-agent system. This language is chosen by FIPA<sup>1</sup> association as an acceptable language to model interactions among agents. Unfortunately, although most multi-agent system modeling languages are clear to understand, they are not able to verify some properties of the modeled system, because there is no formal semantics of agent decision making.

One important aspect of multi-agent systems is that the agents interact with a physical environment. Such interactions typically consist of continuous changes of behaviors of an agent (e.g. a movement of an agent in logistic transportation, or an agent waiting for some events), as well as discrete changes of the behaviors. The previous scenario

<sup>1</sup> [www.fipa.org](http://www.fipa.org)

can be captured using hybrid automata [7]. In hybrid automata, the discrete changes are modeled using state chart, while the continuous changes are modeled using differential equations. Fortunately, hybrid automata are equipped with formal semantics that make them accessible to formal validation of modeled behaviors. Thus, it becomes possible to prove desirable features as well as to prove absence of unwanted properties for the modeled behavior automatically with the help of model checking methods.

To this end, the aim of this paper is to model a multi-agent system scenario in autonomous logistic processes using hybrid automata and by using model-checking techniques [2], we can prove certain properties of the modeled system. Each agent in the involved scenario is described using Hybrid automaton and the communication between agents is represented using shared variables and synchronization labels. However, before we begin describing the subsequent sections, we will use the term Automaton and Agent synonymously. The remainder of this paper is divided as follows. Section 2 shows the concept of hybrid automata. In section 3, we will discuss autonomous logistic process and our proposed model scenario. Section 4 comes with verifying some properties of the modeled scenario. Finally, section 5 concludes the paper.

## 2 Hybrid Automata

A hybrid system is a system with a phased evolution. Within each phase, the system evolves continuously according to a dynamic law. When an event occurs, the system makes a discrete transition from one phase to the next. A non-deterministic automaton can be used to describe the discrete behavior, and the continuous behavior within each phase can be described by a differential equation. This leads to the notion of hybrid automaton. Hybrid automata have been introduced as a formal model for hybrid systems that combine discrete control graphs, usually called finite state automata, with continuously evolving variables. The syntax of hybrid automata is defined as follows, and for more detail, you can see [7].

### 2.1 Formal Definition

A hybrid automaton  $A$  is a tuple  $(X, V, F, I, Init, E, Jump, \Sigma, Syn)$  where:

- $X$  is a finite set of  $n$  real-valued variables. For example, the variable  $Tdistance$ , in the automaton truck Fig. 1, represents the speed of a truck inside the automaton.
- $V$  is a finite set of locations. For example, the automaton Fig.2 has locations, named,  $Begin, Goodcondition, Badcondition,$  and  $Finish$ .
- $F$  is the flow function which maps set of locations  $V$  to predicate over  $X \cup \dot{X}$ , where  $\dot{X}$  is the set of differential equations of the set of variables  $X$ . When the control of a hybrid automaton  $A$  is at location  $v \in V$ , the variables evolve according to differentiable functions, which satisfy the flow conditions  $F$  at this location. For example, location  $GoodCondition$ , in Fig.2, has a flow condition denoted as  $F : envTime=1$ . A flow may be omitted if nothing changes continuously.
- $I$  is the invariant that is a mapping from the set of locations  $V$  to the predicate over the variables in  $X$ .  $I : v$  means the invariant condition at location  $v$ , and it permits

- that the control will be at location  $v$ , whenever the condition is true. For instance, the location `GoodCondition` Fig.2 has invariant  $I : envTime \leq gtime$ , which means that the control will be at this location until the condition is violated. The invariant  $I : True$  means that the invariant is always achievable at the respective location.
- *Init* Is a mapping from the set of locations  $V$  to the predicate over  $X$  that represents the initial condition at each location.  $Init(v)$  is called the initial condition of location  $v$ . Initial conditions, graphically, are expressed as incoming arrow marked with condition in an automaton. For example, `envTime=0` represents the initial condition at location `GoodCondition` Fig.2.
  - $E$  is a finite set of edges, called transition. A transition  $e=(v,v')$  is a directed edge between a source location  $v \in V$  and target location  $v' \in V$ .
  - *Jump* is a mapping, which assigns to each edge  $e \in E$  a jump condition. If the jump condition a transition  $e \in E$  holds, the transition  $e$  can take place and may change the values of the variables  $X$  by executing a specific action (assignment). For instance, the transition between `GoodCondition` and `BadCondition` (Fig.2) has a jump condition `envTime=gtime`, and when it holds it updates the value of the variable `envTime` to the value 0 using `envTime:=0`.
  - $\Sigma$  is a finite set of synchronization labels and a labeling function  $Syn$  that assigns each transition  $e \in E$  a synchronization label from  $\Sigma$ . The synchronization labels are used to define the parallel composition of two automata. If both automata share the same synchronization label  $s \in \Sigma$ , then each  $s$ -transition of one automaton must be accompanied by  $s$ -transition of the other automata. For example, both truck and environment automaton (see Fig.1 and Fig. 2) share the same synchronization labels `ToBad`, `Done`, and `ToGood`.

## 2.2 Parallel Composition

Parallel composition of hybrid automata can be used for specifying larger systems. A hybrid automaton is given for each part of the system, and communication between the different parts may occur via shared variables and synchronization labels. Technically, the parallel composition of hybrid automata is obtained from the different parts using a product construction. The transitions from the different automata are interleaved, unless they share the same synchronization label. In this case, they are synchronized the execution simultaneously. In our scenario, the system is built using the parallel composition of four automata, two trucks, environment, and cargo automaton, as we will show in the next sections.

## 3 Autonomous Logistic Processes

Getting the right goods to the right place at the right time are the requirements on logistics. Nevertheless, with highly dynamic markets and increasingly complex logistic networks it is becoming more and more difficult to meet these standards with conventional methods of planning and control. In the future, aspects such as flexibility, adaptability and reactivity will be of primary importance. The paradigm of autonomous

logistic processes [10] addresses these aspects by decentralizing logistic control to single logistic entities (e.g. freight items, transport containers, means of transport, or storage facilities). Therefore, autonomous logistic processes aim at managing logistics in a highly distributed way by transferring decision-making competencies to the logistic entities. MAS is an adequate and promising technique to implement the autonomous logistic process [5]. Logistic entities as well as secondary logistic services (e.g. traffic information, route planning, and service brokerage) are represented by software agents interacting with each other to coordinate the logistic process. Agent communication and coordination follows standards defined by FIPA association, i.e., using Agent Communication Language (ACL) and interaction protocols for specific agent conversations. In the next subsections, we will describe a multi-agent system in logistic scenario and show how this can be modeled with hybrid automata.

### 3.1 Case Study: Logistic Process Scenario

Our multi-agent scenario constitutes four agents: cargo, environment, and two trucks. The cargo has the objective to be transported to some destination city. The trucks may offer transportation service. Additionally, the environment agent represents an external disturbance to the transportation process. In the following, we will discuss the scenario in more details.

Initially, the cargo tries to contact the two different trucks for requesting the transportation service. The two trucks are located in two different cities. When the cargo calls for a proposal, it sends information, including destination point of the shipment, as well as its due time (deadline), to trucks. As soon as each truck receives the call for proposal, it evaluates and estimates this request according to decision criteria (e.g. its speed limit, transport distance, deadline for transportation). The reason behind the estimation and evaluation processes is that the truck has to check if it may perform the transportation due to some constraints like (the delivery not after deadline). If it can offer transportation, it accepts the proposal and proposes its desired price. On the other hand, if the cargo received multiple proposals, it can pick up the one, which has the lowest price.

Once a selected truck begins the process of transportation, it may be exposed to some environment condition (un-anticipated environmental interactions e.g. traffic or bad weather, etc.). For simplicity, we will use two different environment conditions; named bad and good conditions. These conditions influence the speed of the truck according to their state (i.e. bad or good). The truck slows down its speed to its minimum limit, whenever it is subjected to a bad condition received from the environment, whereas it accelerates to its maximum limit, whenever environment conditions are good. The influence of the environment is of course seriously limited in this way. In reality, these conditions are more complex than our scenario. In a more realistic model of the environment, a stochastic characterization of disturbances would be used. Stochastic models, however, go beyond the expressiveness of hybrid automata. At the end of the transportation process, the truck reports its delivery time with comparison to the due time. Therefore, if the truck delivered the shipment after the deadline, it informs the cargo with failure in the transportation otherwise, it informs the cargo that the transport was successful.

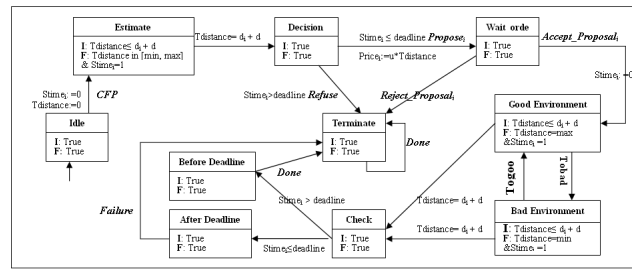


Fig. 1. Truck Automaton.

Surely, the previous scenario can be modeled using FIPA contract net protocol [3]. As we mentioned before, FIPA specification gains widely acceptance in modeling multi-agent system especially for representing the interactions among the agents. It lacks, however, from proving certain properties to the modeled multi-agent system. Therefore, we intend in the next sections to model the previous scenario using hybrid automata, and with the help of model checking we check desirable features.

### 3.2 The Model

As stated earlier, hybrid automata allow to model systems as a set of concurrent processes. We model the logistic scenario described in the previous section as a concurrent hybrid automata. Each automaton represents an agent in the modeled scenario. Truck automaton, cargo automaton, and environment disturbance automaton will be described in the following subsections in more details.

**Truck Automaton.** Figure 1 depicts the automaton(agent) truck. In our scenario, we have two trucks with the same behaviors, but with different capabilities (e.g. speed, price, total distance the truck will pass). Each truck has desired price to perform the transportation, and has different speed capability.

Initially, the behavior of a truck control starts at location *Idle*, and waits for incoming proposal from the cargo. The proposal is represented by the synchronization label *CFP*. Once a truck receives a *CFP* message, the control goes to location *Estimate*. At the later location, the truck estimates, according to its minimum and maximum speed limit, as well as, the expected time it will take to perform the transportation process. Once the estimation process terminates, the control goes to location *Decision*. From this location, the control goes to either location *Terminate* or *Wait-order*. The former location is chosen whenever the expected estimation time exceeds the deadline for transporting the shipment. However, if it goes to *Wait-order*, the truck proposes to perform the transportation as well as the intended price. From location *Wait-order*, the control goes to either location *GoodEnvironment* or *Terminate*. This is depending on the received message from the cargo. The control goes to location *Terminate*; when the truck receives proposal rejection from the Cargo (which is represented by synchronization label *Reject\_proposal* in Fig. 1). However, when the truck receives accept proposal (indicated in Fig.1 as *Accept\_proposal*), the control goes to location *GoodEnvironment* and the control mutually changed between *GoodEnvironment* and *BadEnvironment* according to the influence of the environment to the truck. The truck

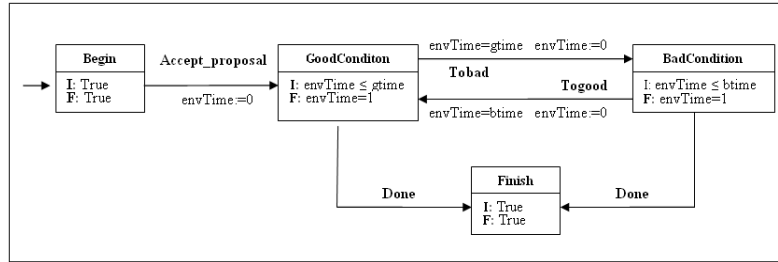


Fig. 2. Environment Automaton.

receives disturbance from the automaton environment using the synchronization labels *Togood* and *Tobad*. At both locations, the truck either speeds up to its maximum or slows down to its minimum speed. After certain time passes, the control goes to location *Check*, which assure that the truck reaches to the required destination point. In such a case, a truck arrives either before deadline or after deadline. In both cases, the truck has to inform the cargo wither with failure or with done, when it arrives after or before deadline respectively.

**Environment Automaton.** Figure 2 models an environment that generates disturbance during transportation process. This disturbance could be due to traffics, or a change in weather. The Environment automaton is augmented with the variable *envtime* that calculates the elapsed time at both location *GoodCondition* and *BadCondition*. The behavior of the environment automaton mutually oscillates between these two locations. The control waits for *gtime* units at the location *GoodCondition*, while it waits for *btime* time units at *BadCondition* location. Both *gtime* and *btime* represent the time that environment takes at both locations.

**Cargo Automaton.** The automaton cargo is shown in Fig.3. The control of the cargo begins at location *Start*. Then, it requests proposals from the participating trucks and the control goes to location *Wait-proposals*. At this location, the cargo reports the received messages that are coming from the different trucks (the messages are represented either by *Refuse<sub>i</sub>* or *Propose<sub>i</sub>* synchronization labels and  $i=\{1,2\}$ ). After all trucks send their desired proposals, the control goes to location *Evaluate-propos*. From this location, the control may go to one of the location *Terminate*, *SelectAgent*, or *Bid*. The choice among these locations is depending on how many trucks propose to perform the transportation. For example, if no truck proposes a proposal, the control goes to location *Terminate* that means there is no truck agreed to perform the transportation. If there is only one truck proposes a proposal, the control goes to location *Bid*. While, if more than trucks propose proposal, the control goes to location *SelectAgent*. At this latter location, the cargo selects a truck that provides a minimum price, and then the control goes to location *Bid*. At location *Bid*, the cargo informs a selected truck with acceptance of the proposal. In addition, the cargo will exclude the remaining truck using synchronization label *Reject-proposal*. After that, the control goes to location *Wait-arrived* and the cargo at this location waits for an incoming report from a truck that is responsible for the transportation process. Whenever the cargo receives *Failure* message, the control goes to location *Unsafe* then goes to location *Terminate*.



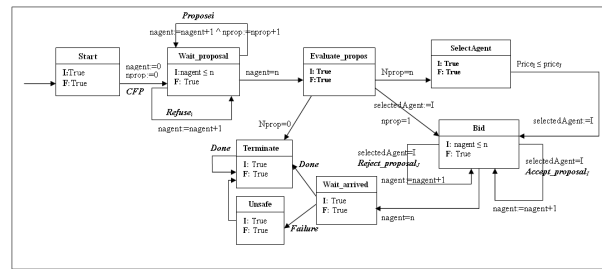


Fig. 3. Cargo Automaton.

### 3.3 Entire Automaton

The previous multi-agent scenario typically consists of several agents that operate concurrently and communicate with each other. We described each agent as a hybrid automaton component. Component automata coordinate through shared data variables and synchronization labels. Nevertheless, the hybrid automaton that models the entire system should be constructed to analyze behaviors of the modeled system. However, when numbers of automata and numbers of states in each automata increase, it will be difficult to understand the behavior of the entire system. This is because the entire automaton is constructed from a product operation of the all participant automata. Fortunately, there are model-checking tools that automatically construct the entire automaton and make it accessible for formal verification (as we will see in the next section). Therefore, this gives us the ability to concentrate on each automaton separately, and then input these automata in a proper format to a model-checking tool, which in turn constructs the entire automaton and performs some verification experiments.

## 4 Model Checking

Generally, a formal verification is a process in which mathematical techniques are used to guarantee the correctness of a dosing with respect some behavior. A formal model of a system allows its verification before it is built in order to determine design problem, or it can be used to improve an existing one. Currently, the most successful approach to the verification of formal models against formally expresses requirements is that of model checking [2]. Generally, Model checking techniques allow verifying formally and automatically if some properties of a system are satisfied in all possible system evolutions. The process of model checking includes modeling, specification, and verification. In modeling, a design is converted to a formalism accepted by a model checker (in our case study we use hybrid automata). The specification process asserts the properties, described in temporal logic, that the model has to satisfy. The verification process asserts that the model meets the specification. Ideally, the verification using model checking is completely automatic.

There are several existing model checker tools that are used to verify the properties of the hybrid automata. Among of them are Hytech [8], and PHAVER [4]. We implement our model using Hytech. Hytech takes a textual representation of hybrid automata as input and performs reachability analysis by exploring the entire state space of the

system. For more details about Hytech syntax, see [6]. Hytech computes the reachability of the entire state space by computing the set of all states reachable from the initial state, and then performs checking for needed properties using the resulting set. Moreover, Hytech provides a way that aids in design and debugging a system. For example, if a system description contains design parameters, whose values are not specified, then Hytech computes the necessary and sufficient constraints on the parameter values that guarantee correctness. In addition, if a system fails to satisfy a correctness requirement, then Hytech generates an error trajectory, which contains a time-stamped sequence of events that leads to a violation of the requirement.

In the rest of this section, we present some model checking experiments on our scenario. We have proved various properties, depending on different values of the involved variables in our model. Here, we will spot on some of them.

**DEADLOCK OCCURRENCE:** One system property, that is of general interest, is the absence of deadlocks in the modeled system. This means that there is no configuration that prevents one of the component automata from reaching its final location (in our model, location `Terminate` in both cargo and truck is the final location). Using Hytech, we showed that our model is indeed free of deadlocks by asking if the formula  $f: location[Truck1]=terminate \ \& \ location[Truck2]=terminate \ \& \ location[Cargo]=terminate$  is reached.

**IS THERE A TRUCK THAT CAN PERFORM THE TRANSPORTATION?** In our scenario, there are two trucks involved in the process of transportation. We ensure that only one truck will be responsible for performing the transportation by checking the reachability of the formula  $f: location[Cargo]=selectAgent$  is reached. Moreover, this truck always provides the minimum price.

**DEADLINES:** One of the most important topics in the logistics domain is the question whether a deadline can be met or not. Clearly, the question if a truck will arrive before or after a given deadline depends on a number of factors like the environmental conditions during the transport, the transport distance, and of course the deadline itself. Using Hytech we did some experiments to answer this question for various values of the deadline, as well as, the times  $gtime$  and  $btime$  of the environment. The speed of the trucks in our experiments lies between 60 and 90, and the total distance that the trucks had to travel, was 1100 and 1150. With  $btime=0$  and  $gtime=5$  several values for the deadline were investigated. It turned out that the truck could always reach its destination on time if the deadline was 17 time units, while a deadline of 12 time units was impossible to meet. In order to determine the closest deadline for which the truck was guaranteed to be on the due time, we use parametric analysis provided by Hytech. This yielded 15.55 time units as the closest deadline that could always be met.

Similarly, some experiments were done to investigate the influence of the environment during the transport. For a given  $deadline=17$  and  $btime=5$ , Hytech's analysis has shown, that  $gtime = 0.888$  time units is enough to ensure that the truck will always arrive on time. If, on the other hand,  $gtime=2$ , then  $deadline=17$  can only be met if  $btime \leq 14.33$ . It is easy to see that the knowledge of boundaries and dependencies between certain values as we presented above will help both the transport agent and the customer to negotiate a contract that suits both parties.



## 5 Conclusions

Currently, most of multi-agent systems modeling languages are not able to verify some properties of the modeled system. Therefore, we demonstrated, in this paper, how to model a multi-agent system using the formalism of hybrid automata. This is because hybrid automata are equipped with formal semantics that make them accessible to formal validation of modeled behaviors using model-checking techniques. The context in which we modeled our multi-agent system is taken from logistics process. This scenario is mainly depending on FIPA contract net protocol. However, FIPA protocols are not able to verify the properties of modeled multi-agent systems. Therefore, we modeled the multi-agent system scenario using hybrid automata and with the help of HyTech model checker; we verified certain properties of this scenario. Reachability analysis, which is provided by model checking, helps us for finding out the possible paths, which could help in the pre-computation of multi-agent system implementations. This point will be subject of future work. Further, we intend to integrate a knowledge base with hybrid automaton to reasoning about the dynamic behaviors of Multiagent system specially in the logistic domain.

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