

# ADJUSTING ANALOGY SOFTWARE EFFORT ESTIMATION BASED ON FUZZY LOGIC

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**Keywords:** Analogy Software Effort Estimation, Fuzzy Logic, Software Project Similarity Measurement.

**Abstract:** Analogy estimation is a well known approach for software effort estimation. The underlying assumption of this approach is the more similar the software project description attributes are, the more similar the software project effort is. One of the difficult activities in analogy estimation is how to derive a new estimate from retrieved solutions. Using retrieved solutions without adjustment to considered problem environment is not often sufficient. Thus, they need some adjustment to minimize variation between current case and retrieved cases. The main objective of the present paper is to investigate the applicability of fuzzy logic based software projects similarity measure to adjust analogy estimation and derive a new estimate. We proposed adaptation techniques which take into account the similarity between two software projects in terms of each feature. In earlier work, a similarity measure between software projects based on fuzzy C-means has been proposed and validated theoretically against some well known axioms such as: Normality, Symmetry, transitivity, etc. This similarity measure will be guided towards deriving a new estimate.

## 1 INTRODUCTION

Although much research has been carried out in the context of software cost estimation (Kirsopp and Shepperd, 2002), none of the existent models has consistently proved to produce credible estimate than others (Menzies, Chen, Hihn and Lum, 2006). Amongst them, estimation by analogy (EA) has been achieved a considerable interest of many researchers (Mendes and Mosley, 2002). In one sense, it is formal estimation with expert judgement which can be viewed as a systematic development of the expert opinion through experience learning and exposure to analogue case studies (Shepperd and Schofield, 1997) (Mendes and Mosley, 2002). It is based on underlying assumption: *the more similar the software project description attributes are, the more similar the software project cost is* (Mendes, Mosley and Counsell, 2003). Therefore, the similarity measurement between two software projects is the key accuracy of software prediction because it attempts to retrieve the most similar historical project to a new project. But, in many circumstances the use of retrieved projects without adapting them

to considered environment leads to potential overestimation or underestimation problems. The most difficult activity in analogy estimation is how to derive a new estimate from retrieved cases. Thus, it fits the case in hand and minimizes the variation between current case and retrieved case.

In this paper, we proposed two adaptation rules to derive new estimate from retrieved cases using our fuzzy logic based software projects similarity measurement (Azzeh, Neagu, Cowling, 2008). The first Adaptation Rule (AR1) attempts to adapt the retrieved analogies according to their similarity measurement with estimated project in each feature dimension, then the new estimate is aggregated based on one of these operators (minimum, maximum, and mean). The second Adaptation Rule (AR2) is to adapt each analogy individually according to its similarity with estimated one in terms of each feature dimension.

The remainder of the paper is organised as follows: Section 2 discusses related works about EA and adaptation rules. Section 3 introduces Fuzzy Logic. Section 4 presents in more details our

proposed analogy estimation with adaptation rules and fuzzy logic based software projects similarity measurement. Section 5 introduces evaluation criteria. Section 6 compares the efficiency of adaptation rules in analogy effort estimation. Finally, section 7 summarizes our work and outlines the future studies.

## 2 RELATED WORKS

The accuracy EA has been confirmed and evaluated in previous researches such as those were undertaken by (Shepperd and Schofield, 1997), (Mendes and Mosley, 2002), (Kirsopp and Shepperd, 2002) and (Briand, Langley and Wiczorek, 2000), (Myrtveit and Stensrud, 1999) and (Mendes, Mosley and Counsell, 2003).

Chiu et. al. (Chiu and Huang, 2007) reported that EA always needs more sensed similarity methods. They investigated the use of Genetic Algorithms (GA) based project distance to adjust retrieved effort. The results showed that using adjusted similarity mechanism gave better accuracy than using traditional similarity distance. Jorgensen et. al. (Jorgensen, Indahl and Sjoberg, 2003) investigated the use of regression towards the mean (RTM) method to adjust the analogy estimation. They indicated that the adjusted estimation using RTM method was significantly more accurate than EA without adjustment.

Idri et al. (Idri, Abran and Khoshgoftaar, 2001) proposed alternative approach for Analogy software cost estimation based on fuzzy logic and linguistic quantifiers. They tried to adjust analogy estimation based on fuzzy similarity between two software projects that are described as linguistic quantifiers. In some sense, this approach does not have learning ability (Auer, 2004) and the results are not promising.

## 3 FUZZY LOGIC

Fuzzy logic as introduced by Zadeh (Zadeh, 1997) provides a representation scheme and mathematical operations for dealing with uncertain, imprecise and vague concepts. Fuzzy logic is a combination of set of logical expressions with fuzzy sets. Each fuzzy set is described by membership function such as Triangle, Trapezoidal, Gaussian, etc., which assigns a membership value between 0 and 1 for each real point on universe of discourse. This membership value represents how much a particular point does

belong to that fuzzy set. Software estimation is generally complex and vague with some uncertainties in attribute measurement. The most common problem in software estimation arises from using categorical data (nominal or ordinal scale). Fuzzy logic provides a way to map between input and output space with clear natural expressions of fuzzy rules (Bezdek, J.C, 1981) (Zadeh, 1997) (Xu and Khoshgoftaar, 2004).

**Property 1.** Fuzzy set  $A$  is called normal fuzzy set if it has at least one element  $x$  in the universe of discourse whose membership value is unity or height of  $A=1$ . A fuzzy subset that is not normal is called subnormal (Ross, 2004).

## 4 ESTIMATION BY ANALOGY

EA requires identification of a list of main software project attributes the effort estimation will be based upon. Then similar but completed projects are found, for which the cost is known. The estimation is later based on these effort values. In this paper we will use fuzzy logic based software projects similarity to adjust analogy estimation and derive new estimate. In next subsection we will give more details about proposed similarity measure and adaptation rules.

### 4.1 Similarity Measurement

In earlier work, we have proposed similarity measurement approach based on fuzzy C-means and theoretically validated against some well known axioms such as: Normality, Symmetry, transitivity, etc. (Azzeh, Neagu, Cowling, 2008). The similarity measure is described as follows:

Let  $p_x, p_y$  be two software projects described by  $M$  features  $F_j (j=1...M)$ , for each feature (linguistic variable) there are several normal fuzzy sets  $A_k^j$  obtained by FCM and fuzzy identification, where  $k$  represents number of clusters. Particularly, we impose our approach to use Gaussian membership function. The similarity measure is explained in the following steps:

1. For each linguistic variable, find fuzzy set  $A_x^j$  that represents maximum membership value of  $F_j(p_x)$  and fuzzy set  $A_y^j$  that contains maximum membership value of  $F_j(p_y)$  by using maximum operators.

$$\mu_{C_i}(p) = \max\{\mu_{C_1}(p), \mu_{C_2}(p), \dots, \mu_{C_c}(p)\} \quad (1)$$

2. For each linguistic variable, find  $SM_j (A_x^j, A_y^j)$  using *approaching degree* (Azzeh, Neagu, Cowling, 2008). In terms of one feature,  $SM_j(F_j(p_x), F_j(p_y))$  is intuitively identical to  $SM_j (A_x^j, A_y^j)$ .

$$SM_j(F_j(p_x), F_j(p_y)) = \min\left(e^{-\frac{(x-y)^2}{(\sigma_x + \sigma_y)^2}}, 1\right) \quad (2)$$

where  $x, y$  are the mean values and  $\sigma_x, \sigma_y$  are the standard deviation for Gaussian membership functions  $A_x^j$  and  $A_y^j$  respectively.

3. Find overall similarity between two software projects as shown in equation 3. Consequentially, the closest analogue to a particular project is the project with maximum similarity.

$$SM(p_x, p_y) = \text{avg}_{j=1}^m (SM_j(F_j(p_x), F_j(p_y))) \quad (3)$$

## 4.2 Adaptation Strategy

Adaptation is mechanism used to derive a new estimate; thus, to minimize the differences between retrieved case and current case (Sankar, Simon and Shiu, 2004). It is important step in estimation by analogy because it reflects structure of problem case on retrieved case. In this step we have to decide how many analogies should be employed to derive new estimate by adaptation. As yet, there are two main approaches used in EA model (Shepperd and Schofield, 1997). First approach is concerned with taking all software projects that fall in a particular distance of new project. This approach could lose some valuable project when distance between selected and unselected projects is notably very small (i.e. few fractions). Second, is to use fix number of analogies. This approach has been followed by many researchers such as (Briand, Langley and Wiczorek, 2000) and (Mendes, Mosley and Counsell, 2003). The second approach has been followed in this research where number of analogies is limited to 3, which we believe is sufficient to drive new estimate. Several analogy adaptation rules have been used in software engineering literature. Mendes et. al. (Mendes, Mosley and Counsell, 2003) used Linear Size Adjustment to adapt individual project. This approach takes the effect of each feature value on the final estimate. (Idri, Abran and Khoshgoftaar, 2001) used linear distance adjustment where the distance between two

software project in each features is used to adapt new estimate.

In this work we proposed a set of candidate adaptation rules. The first adaptation rule (AR1) calculates the aggregated effort estimate based on the similarity between estimated project and other closest analogies in each feature dimension. The underlying mechanism of AR1 is to adapt the retrieved efforts according to the similarity in each feature, then the final estimated effort is aggregated based on one of these operators (minimum, maximum, or mean).

$$E_s = AR1_{j=1}^M \left[ \frac{\sum_{i=1}^N SIM_j(p_i, p_s) * E_i}{\sum_{i=1}^N SIM_j(p_i, p_s)} \right] \quad (4)$$

Where:

$M$ : number of features,  $N$ : number of analogies.

$ARI$ : is an effort aggregation operator which might be (max, min or average).

The second adaptation rule (AR2) is to adapt each analogy individually according to its feature similarity with estimated one as shown in equation 5. Then adaption cases such as: (mean of closes analogies and inverse ranked weight mean) are used to derive the final estimate. The inverse ranked weight mean takes the influence of each case into account where the higher closes cases takes the high weight than lower cases. For example, in our case we have three analogies so the estimation by inverse ranked would be calculated as (3\*closes case + 2\*second closest + third closes/6)

$$E_{s_i} = \sum_{j=1}^M \left[ \frac{SM_j(p_i, p_s) * E_i}{\sum_{j=1}^M SM_j(p_i, p_s)} \right] \quad (5)$$

The comparison between two adaptation rules is that the AR1 adapts all retrieved efforts together in each feature then aggregates all adapted efforts to derive a new estimate. While in AR2, each retrieved effort is adapted individually in terms of feature similarity.

## 5 EVALUATION CRITERIA

Many prediction evaluation criteria have been proposed in literature, among them Magnitude Relative Error MRE and mean of magnitude relative error MMRE have achieved a considerable interest from researchers. Previous research has criticised that MMRE does not identify the best estimation model and is unbalanced in many validation circumstances which leads to overestimation more than underestimation (Shepperd and Schofield, 1997) (Tron, Stensrud, Kitchenham and Myrvtveit, 2003). Rather, we used MMRER and Pred(0.25). MER Computes the degree of estimating error in an individual estimate and should be less than 25% to be acceptable. Pred(0.25) is proportion of prediction within 25% of actual value for all predictions. It should be larger than 75% to be acceptable.

$$MMER = \frac{1}{n} \sum_{i=1}^n \frac{|actual_i - estimated_i|}{estimated_i} \quad (6)$$

$$Pred(e) = \frac{\# projects with MER \leq e}{\# projects} \quad (7)$$

## 6 EVALUATION OF FUZZY LOGIC ADJUSTMENT

In this section we evaluate the efficacy of fuzzy logic based software projects similarity measurement and proposed adaptation rules to derive more credible estimate. We used Jack Knifing validation (also known as Leave one-out cross validation) approach because it mimics the real world estimation. The data used in this paper come from (ISBSG, 2007), (Sentas and Angelis, 2006), and Desharnais datasets (Boetticher, Menzies and Ostrand, 2007) as shown in Table 1.

Table 1: Data set Characteristics.

Characteristics	ISBSG	Desharnais
No. of features	15.73%	82.0%
No. of projects	15.724%	82.0%

Table 2: Legend for empirical validation.

CC1NA	One analogy without adaptation rule
CC2NA	Mean of 2 analogies without adaptation rule
CC3NA	Mean of 3 analogies without adaptation rule
INV2NA	Inverse ranked for 2 analogies without adaptation rule

Table 2: Legend for empirical validation (cont.).

INV3NA	Inverse ranked for 3 analogies without adaptation rule
MD3NA	Median of 3 analogies without adaptation rule
MAX_AR1	AR1 with MAX operator (3 analogies)
MIN_AR1	AR1 with MIN operator (3 analogies)
MEAN_AR1	AR1 with MEAN operator (3 analogies)
CC1WAR2	One analogy with AR2
CC2WAR2	Mean of 2 analogies with AR2
CC3WAR2	Mean of 3 analogies with AR2
INV2WAR2	Inverse ranked for 2 analogies with AR2
INV3WAR2	Inverse ranked for 3 analogies with AR2
MD3WAR2	Median of 3 analogies with AR2

### 6.1 ISBSG Dataset

Table 3 shows the estimation results of ISBSG dataset. These results have been obtained by considering two new adaptation techniques based on fuzzy logic based software projects similarity. By comparing these different adaptation rules based on lower MMER, and higher Pred(0.25), we can observe that models without adaptation (i.e. only case adaptations) and those using adaptation rule 1 (AR1) produced significantly better results than AR2. Only closest case with AR2 obtained reasonable accuracy while other case adaptations with AR2 did not contribute to credible estimate. This was arose a question about what are the reasons behind this variation between two adaptation rules AR1 and AR2. This may be related to variation in similarity between estimated project and other closest projects, and to the range of data. The results obtained by AR2 corroborated the results obtained by (Mendes, Mosley and Counsell, 2003) that showed using adaptation rules does not often improve estimation accuracy.

Table 4 shows that there is no significant difference between aggregation operators for AR1. Minimum, maximum and average aggregation operators have approximately the same influence on the adjustment because the closest projects are often fall in the same fuzzy set in most features. This make similarity between new project and closest projects is slightly different. We also observed that when using AR1 did not have as many best predictions as it did with CC3NA and INV3NA.

Figure 1 shows Boxplots of estimation results in MER. The Boxplots illustrates inter-quartile rage that contains 50% of projects, median and outlier projects in terms of estimation results as measured by the MER. The upper and lower tails indicate the

distribution of the observations. The Boxplots shows that CC3NA, IN3NA, MINAR1, MAXAR1 are statistically significant than others because they present a low dispersion of the MER values and small median than others. This revealed that AR1 is significantly better than AR2 for ISBSG. Furthermore, the smaller range of upper and lower tails suggests the MAX\_AR1 is statistically the most significant adjustment among the others.

Table 3: Results for ISBSG with case adaptations and AR2.

Case adaptation	Without adaptation rules		With AR2	
	MMER	Pred	MMER	Pred
CC1	17.2%	76%	15.9%	80.0%
CC2	15.4%	80%	33.0%	44.0%
INV2	15.3%	78%	25.4%	50.0%
CC3	14.3%	86%	49.8%	30.0%
MD3	15.0%	76%	49.4%	27.0%
INV3	14.6%	84%	39.9%	42.0%

Table 4: Results for ISBSG with AR1.

AR1	MMER	Pred)
MIN-adaptation	15.73%	82.0%
MAX-adaptation	15.724%	82.0%
MEAN-adaptation	15.6%	82.0%

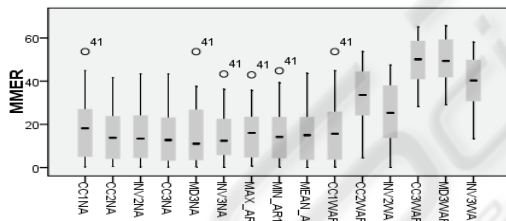


Figure 1: MER Boxplots for ISBSG dataset.

### 6.2 Desharnais Dataset

Tables 5 and 6 present the estimation results and corresponding accuracy for Desharnais dataset. The first observation is that the accuracy obtained by different adaptation did not reach target of acceptable accuracy which is less or equal 25% for MMER and more than 75% for Pred (0.25). This may be related to dataset size and range of values. It seems there is strong linear relationship between effort and other features caused this problem. Adjusted analogy estimation with Adaptation rule AR1 and AR2 contribute to better estimation results than others without adaptation. From table 4 we can

notice that the value of MMER was decreased for all case adaptations except CC3.

Table 6 suggests that using MIN operator for AR1 has significantly given a slight better result than MAX and MEAN operators. On the other hand, adjusted analogy models with AR2 gave better accuracy than analogy models with AR1. The best result obtained with AR2 was by CC2.

Figure 2 suggests that using fuzzy adjustment exhibits a smaller range of upper and lower tails of the MER values than other without adaptation. Furthermore, the adjusted models with AR1 showed small standard deviation than others. It also showed that adjusted analogy models with AR1 and AR2 are marginally more accurate than others without adjustment. The overall results show the adequacy of AR1 for both datasets, whilst AR2 performed better in Desharnais dataset.

Table 5: Results for Desharnais with case adaptations and AR2.

Case Adaptation	Without adaptation rules		With AR2	
	MMER	Pred	MMER	Pred
CC1	50.4%	26.0%	43.7%	32.0%
CC2	44.5%	38.0%	38.5%	38.0%
INV2	48.4%	32.0%	39.4%	36.0%
CC3	42.7%	32.0%	45.7%	22.0%
MD3	48.1%	40.0%	45.0%	30.0%
INV3	43.8%	30.0%	39.7%	36.0%

Table 6: Results for ISBSG with AR1.

AR1	MMER	Pred
MIN-adaptation	40.44%	36.0%
MAX-adaptation	45.6%	30.0%
MEAN-adaptation	42.5%	32.0%

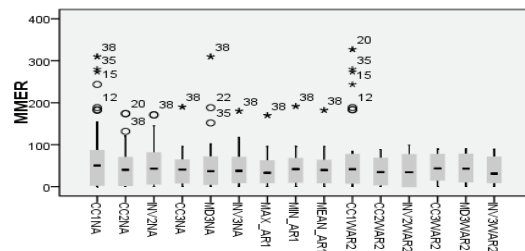


Figure 2: MER Boxplots for Desharnais dataset.

## 7 CONCLUSIONS

In this paper we have proposed two adaptation rules using fuzzy logic based on software project

similarity measurement. We have compared the use of Adaptation rules AR1 and AR2 with non adjustment analogy models. The results showed that adjusted analogy model with AR1 has significantly improved the analogy estimation in both datasets, while AR2 performed better only for Desharnais dataset. The reasons behind that arose from number of features, relevancy of features, range of data values, and number of cases. Future extension of the proposed model is planned to consider the effect of feature subset selection.

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