APPLICATION OF NEURAL NETWORKS IN AID FOR DIAGNOSIS FOR PATIENTS WITH GLAUCOMA

Dário A. B. Oliveira, Marley M. B. R. Vellasco

Electrical Engineering Department, Pontifical Catholic University of Rio de Janeiro - Rio de Janeiro, RJ, Brazil

Mariana M. B. Oliveira, Riuitiro Yamane

Medical Sciences Faculty, Department of Opthtalmology, Rio de Janeiro State University - Rio de Janeiro, RJ, Brazil

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Abstract: Glaucoma is an ophthalmologic disease very difficult to diagnose in the earlier phase. Additionally, exams and methods used to give reliable information for correct diagnosis are usually very expensive. Therefore, other methods less expensive and also reliable must be proposed as an auxiliary tool to Glaucoma diagnosis. This paper analyzes the performance of neural networks as an auxiliary tool for the diagnosis of patients with glaucoma, avoiding the use of data only available in expensive exams. The analysis considers two different kinds of neural networks (Multi-Layer Perceptron (MLP) and Probabilistic Neural Networks (PNN)) and two different methods variable selection: a random and iterative method; and the Least Square Extrapolation (LSE) method. The paper also evaluates the benefits of applying principal components analysis (PCA) to the database. The results obtained were very good, attaining an accuracy of more than 90% of correct classification of all cases present in our database. It confirms the real possibility of using neural networks as an auxiliary and inexpensive tool to help in Glaucoma diagnosis.

1 INTRODUCTION

Advances in medicine increase daily the volume of data to be analyzed by experts. This large amount of data often makes it harder the definition of a profile of diagnosis using all available information and based only on past experience. Computational intelligence methods may be used in this context, since they are able to acquire knowledge through historical data, obtained from patient examinations and diagnose, and provide a decision support system to help in the glaucoma diagnosis.

The human visual system is extremely complex and functional loss of vision, as in glaucoma, affects in a significant way the quality of life. Glaucoma is a disease of the optic nerve and is the leading cause of irreversible blindness and the second leading cause of low vision in the world, affecting about 67 million people. It usually has a slow progression, and can lead to blindness in 27% of cases.

More than half of people with glaucoma is not diagnosed, since ill patients are rarely symptomatic before submitting an advanced degree of injury of ganglion cells and, consequently, changes in the visual field (Quigley, 1996; Hattenhauer et al, 1998). The presence of changes in visual field represents an injury of 30%-50% of ganglion cells, which represents an advanced injury (Kerrigan-Baumring et al. 2000). The irreversible nature of injuries makes the diagnosis and early treatment essential.

An analysis of extreme importance in the diagnosis of glaucoma is the assessment of nerve fibre layer (NFL) of the retina, which is composed of ganglion cells axons, among other cells (Hoyt et al, 1972). Various methods are available to assess the NFL. One example is the direct ophthalmoscopy or red-free photographs, allowing a qualitative and semi-quantitative analysis. However, photographs of good quality depend on the patient level of cooperation, maximum pupil dilation, trained photographer and other factors, such as pigmentation of the retinal pigmented epithelium, which can difficult the nerve fibres identification as it changes the nerve fibres reflection. Therefore, it is a subjective analysis, since it depends on the examiner experience (Quigley et al, 1993).

The HRT (Heidelberg Retina Tomograph), a confocal laser scanning ophthalmoscope, is another technique for easy operation, rapid acquisition and useful to obtain images without dilation of the pupil, but it is not able to measure the layer of nerve fibres directly. It calculates the NFL from a plan of reference, based on studies of histological NFL in monkeys. If used with diagnostic purposes, there is a degree of overlap between the patients with and without glaucoma.

One of the most currently used methods, due to its high precision, is optical coherence tomography (OCT). The OCT is a method capable of providing images of the retina nerve fibres layer through transverse sections with high resolution (8-10 μ m), described by Huang et al in 1991, in vivo or in vitro. This technique is based on the principle of low coherence interferometry, creating two-dimensional images with information of distance and thickness of retinal structures.

The final image provided by OCT is produced based on code of colors, processed by a computer, as shown in Figure 1. Figure 1-a illustrates the eye background image and the retina nerve fibres layer. Bright gray indicates greater concentration of nerve endings. Figure 1-b shows the thickness of retinal NFL distributed spatially into four different regions: superior, temporal, inferior and nasal. The graph shows the spatial distribution of the retinal NFL thickness in black, and a benchmark in gray levels, where the region in dark gray indicates healthy patient, the region in white in between the two gray regions indicates a patient with a possible presence of dysfunction, and the light gray region indicates the presence of dysfunction.



Figure 1: Image of the retina with information obtained by the OCT.

Although this examination provides very precise information about the retinal NFL, which is used in

glaucoma diagnosis, it is important to stress that it is an expensive examination. Therefore, this work intends to propose a much cheaper alternative that still can obtain satisfactory results in the identification of retinal dysfunction in NFL. The proposed method only uses variables that can be obtained through cheaper examinations, and it is based on neural networks.

Artificial neural networks are systems inspired on biological neurons and on the ability of the brain to process information in a massively parallel way. These systems are able to acquire knowledge experimentally and to properly respond to new cases.

A neural network is represented by weighted interconnections between processing elements (PEs). These weights are the parameters that actually define the non-linear function performed by the neural The process of determining such network. parameters is called training or learning, relying on the presentation of many training patterns. Thus, neural networks are inherently adaptive, conforming to the imprecise, ambiguous and faulty nature of real-world data. Learning procedures can be either supervised or unsupervised. In supervised learning, a training pair, consisting of an input pattern and the target output, is submitted to the network. The network usually adjusts the weights based upon the error value between the target and the network output. Unsupervised learning procedures, on the other hand, classify input patterns without requiring information on target output. In such procedures, the network must detect the patterns' regularities, classifying them into disjoint groups according to their feature similarities.

This paper assesses the ability of neural networks (Haykin, 1994), based on supervised learning, to properly classify patients with dysfunction in retinal NFL, an indication of the presence of glaucoma, based on variables obtained in simpler and cheaper exams than OCT.

It compares the performance of two neural network models: Multi-Layer Perceptron (MLP) (Rumelhart et al, 1986), and probability neural networks (PNN) (Wasserman et al, 1993). For both MLP and PNN models, two different methods of selection of variables were tested: a random and repetitive, and another that uses least square extrapolation (LSE) (Roxana et al, 2005) (Chung, 2000).

The database was also decomposed into its principal components (PCA) (Krzanowski, 1988), in order to assess the importance of this transformation

in increasing the neural network rate of proper identification for this application.

The article has three additional sections, which explain in more details, the proposed study. Section 2 describes in details the database obtained and the neural networks modeling. Section 3 shows the results obtained and section 4 presents the main conclusions that this work has generated.

2 GLAUCOMA DIAGNOSIS THROUGH NEURAL NETWORKS

2.1 Medical Database

The input database used to classify patients was generated from results obtained with the Optical Coherence Tomography of Stratus OCT 3.0 (Carl Zeiss Meditec) and consists of 256 samples. Values of 14 different input variables were catalogued, as well as the status of the dysfunction in retinal NFL. This dysfunction indicates the presence of glaucoma.

The input variables are:

- 1. Age
- 2. Sex
- 3. Rim Area
- 4. Average width of nerve
- 5. Diameter of Disk
- 6. Diameter of Excavation
- 7. Width of Rim
- The proportion of excavation area and disk area
 The proportion of excavation horizontal diameter
- and disk horizontal diameter 10. The proportion of excavation vertical diameter
- and disk vertical diameter
- 11. Thickness of the superior region of retinal NFL
- 12. Thickness of the nasal region of retinal NFL
- 13. Thickness of the inferior region of retinal NFL
- 14. Thickness of the temporal region of retinal NFL

Among the input variables, age is an important risk factor associated with glaucoma. The rim, or neuroretinal ring, can be considered as an equivalent intrapapillary NFL of the retina, and measures about width, diameter and values of areas are physical measurements of the human eye. In normal individuals, the inferior neural rim is usually thicker, followed by the superior, nasal and temporal. In glaucoma, there is mainly loss of rim nerve in superior and inferior poles. Variables 11 to 14 represent the thickness of retinal NFL, for each region, in micrometers (μ m). The classification of the dysfunction is obtained with the commercial software that comes with OCT. In the process, the values of variables 11, 12, 13 and 14 of each patient are submitted to a specific function, whose expression is not provided by the software, and that determines whether or not the patient has some dysfunction in retinal NFL. These four variables can be obtained only using this specific exam, and neural networks will be used to identify the same dysfunction using other variables, that can be obtained through cheaper exams.

2.2 Neural Network Modeling

All numerical variables (1, 3 to 14) were normalized according to their range, in order to remain in the interval [0, 1]. The following normalization equation was used:

$$x_i = \frac{x_i - x_{\min}}{x_{\max} - x_{\min}} \tag{1}$$

The variable sex was codified in binary (0 for female and 1 for male).

The class output was also coded in binary form, 0 being the code of patients whose configuration of retinal NFL indicates a healthy patient and 1 the code for patients whose configuration is pathological. The specification in the database of the presence or absence of dysfunction in retinal NFL was obtained by examination of the OCT response (see Figure 1).

As already mentioned, two different neural network models were evaluated: Multi-Layer Perceptron (MLP) and Probabilistic Neural Network (PNN). The structure of the MLP networks was composed of a single intermediate or hidden layer in all performed experiments. The number of neurons (processing elements) varied according to the experiment, as discussed on the next section.

Due to the binary definition of the output codification, the MLP neural networks output consists of a single node, whose real value between 0 and 1 indicates the likelihood of NFL retinal dysfunction, given a particular individual in the entry. It was assumed that a value greater than 0.5 indicates dysfunction and a value lower than 0.5 indicates a healthy patient.

The structure of PNN networks is defined according to the number of patterns in the training group, and the output layer is treated exactly like the output layer of MLP networks.

The cross-validation method (Kohavi, 1995) was used for training the MLP networks, with 50% of the

population for training, 25% for validation and 25% for testing. In PNN networks, the proportion was 75% of the population for training, and 25% for testing. The samples were distributed in a balanced way between sets, that is, both sets of patients with pathological and healthy profiles were divided using similar proportions.

It is important to mention that the set of validation was used to determine the optimal configuration of the network, in terms of number of processors in the hidden layer and to avoid over training. The same set of test was used through all networks configurations. The results presented in the next section are related only to the test set, which means that the sets of training and validation were not used for the generation of results.

3 RESULTS

The first experiment was performed using only the variables that bring information from the thickness of the NFL (11, 12, 13 and 14), which evaluates the performance of the proposed neural networks models for the classification of patients when these four variables are available. As these variables are used by the OCT to define which patients are healthy and which are not, the task of the neural network is only to model the function inside the unit.

The second experiment, on the other hand, is to assess the performance of the proposed models without using these four variables. The purpose of this experiment is to provide a cheaper alternative to raise the profile of pathological NFL patients, regardless of OCT.

3.1 Experiment 1: Classification using only Measures of Retinal NFL Thickness

The best configuration of MLP networks used four input nodes (one for each of the four input variables), 5 neurons in the hidden layer and one node in the output layer, as explained in section 2.

The results obtained by the two networks are shown in Table 1. This table shows the results for 64 samples of patients from the test set, 19 regarding patients with dysfunction and 45 regarding healthy patients. As shown in Table 1, both networks had an excellent performance, resulting in 100% of success. This result was already expected, since we used exactly the same input variables that are needed by the unit to define the outcome of the examination.

| 4-Variables (fixed) | Ν | MLP | PNN | | | |
|------------------------|----|-----|------|----|--|--|
| Hit rate | 10 | 0% | 100% | | | |
| Confusion Matrix | 45 | 0 | 45 | 0 | | |
| | 0 | 19 | 0 | 19 | | |

Table 1: results of MLP and PNN neural networks for experiment 1.

3.2 Experiment 2: Classification without Measures of Retinal NFL Thickness

The second experiment had the intention to evaluate the performance of neural networks in the classification of patients using the other variables, excluding the four input variables corresponding to the retinal NFL thickness, as mentioned above.

This decision was taken for two reasons. First to evaluate the performance of the network using other variables whose direct involvement in defining the profile of disease for the patient was not pre-known. The second reason is the fact that the variables regarding the thickness of the nerve fibres can only be obtained through the OCT, which is a very expensive exam, while the other variables can be obtained in other exams. It is therefore interesting to know if these other variables can be used to detect the presence of retinal NFL dysfunction, or at least simulate the result of the indication of dysfunction proposed by OCT.

The structures of MPL and PNN networks in this experiment are exactly to the same as the structures of networks in experiment 1, except for the number of variables in the entry that varied from 3 to 10.

These N input variables, where N ranges from 3 to 10, were selected in accordance with 4 different criteria for selection, in both types of neural networks (MLP and PNN):

a) Selection of N variables set randomly;

b) Selection of N most important variables defined by the LSE method;

c) Selection of N first major components identified by the PCA;

d) Selection of N most important variables defined by the LSE method with data transformed into its principal components using PCA.

The results obtained by the various configurations of networks are presented in Tables 2 and 3, using only the test set. Table 2 presents the results for MLP networks and table 3 for PNN networks.

| Number of input | Multilayer Perceptron | | | | | | | | | | | |
|-----------------|-----------------------|---------------------|-------|-------------|---------------------|-------|-------------|---------------------|-------|-------------|---------------------|----|
| | Random | | | LSE | | | РСА | | | PCA/LSE | | |
| variables | Hit rate | Confusion Matrix | | Hit rate | Confusion Matrix | | Hit rate | Confusion Matrix | | Hit rate | Confusion Matrix | |
| 3 5 | 56.25 | 21 | 24 | 79,69 | 38 | 7 | 87,50 | 43 | 2 | 85,94 | 41 | 4 |
| | 50,25 | 4 | 15 | | 6 | 13 | | 6 | 13 | | 5 | 14 |
| 4 90 | 90.63 | 42 | 3 | 89,06 | 42 | 3 | 79,69 | 37 | 8 | 81,25 | 38 | 7 |
| | 90,05 | 3 | 16 | | 4 | 15 | | 5 | 14 | | 5 | 14 |
| 5 89 | 89.06 | 42 | 3 | 90,63 | 42 | 3 | 84,38 | 40 | 5 | 87,50 | 42 | 3 |
| | 87,00 | 4 | 15 | | 3 | 16 | | 5 | 14 | | 5 | 14 |
| 6 89,06 | 89.06 42 | 3 | 80.06 | 41 | 4 | 85.04 | 41 | 4 | 80.06 | 42 | 3 | |
| | 89,00 | 4 | 15 | 89,00 | 3 | 16 | 63,94 | 5 | 14 | 89,00 | 4 | 15 |
| 7 82,8 | 02 01 | 82.81 36 | 9 | 87,50 | 41 | 4 | 82,81 | 37 | 8 | 92,19 | 44 | 1 |
| | 02,01 | 2 | 17 | | 4 | 15 | | 3 | 16 | | 4 | 15 |
| 8 85 | 95.04 | 40 | 5 | 89,06 | 41 | 4 | 87,50 | 40 | 5 | 87,50 | 41 | 4 |
| | 85,94 | 4 | 15 | | 3 | 16 | | 3 | 16 | | 4 | 15 |
| 9 | 89,06 | 41 | 4 | 87,50 | 41 | 4 | 85,94 | 41 | 4 | 89,06 | 41 | 4 |
| | | 3 | 16 | | 4 | 15 | | 5 | 14 | | 3 | 16 |
| 10 | 82,81 | 38 | 7 | 87,50 | 41 | 4 | 65,63 | 25 | 20 | 87,50 | 40 | 5 |
| | | 4 | 15 | | 4 | 15 | | 2 | 17 | | 3 | 16 |

Table 2: Results from MLP networks using different number of input variables and different methods of variables selection.

Table 3: Results from PNN networks using different number of input variables and different methods of variables selection.

| Number of input | Probabilistic Neural Networks (PNN) | | | | | | | | | | | |
|-----------------|-------------------------------------|---------------------|-------|-------------|---------------------|-------|-------------|---------------------|-------|-------------|---------------------|----|
| | Random | | | LSE | | | РСА | | | PCA/LSE | | |
| variables | Hit rate | Confusion Matrix | | Hit rate | Confusion Matrix | | Hit rate | Confusion Matrix | | Hit rate | Confusion Matrix | |
| 3 8 | 07.50 | 42 | 3 | 84,38 | 44 | 1 | 82,81 | 41 | 4 | 81,25 | 40 | 5 |
| | 87,50 | 5 | 14 | | 9 | 10 | | 7 | 12 | | 7 | 12 |
| 4 85,9 | 85.04 | 41 | 4 | 84,38 | 44 | 1 | 84,38 | 41 | 4 | 87,50 | 45 | 0 |
| | 03,94 | 5 | 14 | | 9 | 10 | | 6 | 13 | | 8 | 11 |
| 5 84,3 | 8/ 38 | 84 38 40 | 5 | 87,50 | 44 | 1 | 84,38 | 42 | 3 | 84,38 | 43 | 2 |
| | 04,50 | 5 | 14 | | 7 | 12 | | 7 | 12 | | 8 | 11 |
| 6 82,8 | 82.81 | 82,81 39 5 | 6 | 81,25 | 42 | 3 | 82,81 | 41 | 4 | 78,13 | 40 | 5 |
| | 02,01 | | 14 | | 9 | 10 | | 7 | 12 | | 9 | 10 |
| 7 85,94 | 85 94 | 42 | 3 | 81.25 | 42 | 3 | 85.04 | 44 | 1 | 78.13 | 40 | 5 |
| | 6 | 13 | 01,25 | 9 | 10 | 05,74 | 8 | 11 | 70,15 | 9 | 10 | |
| 8 85,94 | 85 94 | 42 | 3 | 70.60 | 40 | 5 | 85.04 | 44 | 1 | 70.60 | 41 | 4 |
| | 6 | 13 | 79,09 | 8 | 11 | 05,94 | 8 | 11 | ,,,0) | 9 | 10 | |
| 9 85,94 | 85.94 | 43 | 2 | 84,38 | 44 | 1 | 85,94 | 44 | 1 | 85,94 | 44 | 1 |
| | 05,74 | 7 | 12 | | 9 | 10 | | 8 | 11 | | 8 | 11 |
| 10 85,94 | 85.94 | 44 | 1 | 85,94 | 44 | 1 | 85,94 | 44 | 1 | 85,94 | 44 | 1 |
| | 05,74 | 8 | 11 | | 8 | 10 | | 8 | 11 | | 8 | 11 |

The performance of a given network setting was measured using two consecutive criteria. The first welcomes the network that obtained the highest hit rate of patients with retinal NFL dysfunction, since the main goal is the correct classification of patients with an indication of glaucoma. The second criterion is the highest hit rate of the overall, healthy or pathological patients, among the best networks obtained by the first criterion.

The best overall hit rate was 92.19% and it was obtained with a MLP network with 7 entries, the data decomposed into its principal components, and the variables selected by the LSE method. High performance (90.63%) was also achieved with MLP neural networks and the variables selected by the LSE method. The transformation of the database into its principal components seems not to have substantially improved the performance of networks.

Various configurations of networks have hit rates above 84% in patients with an indication of glaucoma, correctly classifying 16 patients in a total of 19. All networks that have this kind of performance were MLP, and therefore one can say that generally the performance of networks MLP was higher than of PNN networks in this application.

The LSE method has proved to be very consistent, making explicit that from 10 variables, not considering the ones related to retinal NFL thickness, 4 have much relevance and allow classification with a hit rate of over 89%: rim width, excavation diameter, disk diameter and average width of nerve. The result of the networks shows that there is a clear link between these 4 variables and an amendment of retinal NFL that may suggest the presence of glaucoma, according to the pattern of this amendment.

According to the specialist, these results are very interesting. In glaucoma, there is really a loss of preferential rim nerve in superior and inferior poles, and so it is consistent the involvement of these variables in the definition of retinal NFL dysfunction.

4 CONCLUSIONS

In ophthalmologic exams, the detection of optic nerve damage by glaucoma involves morphological characteristics, like size and shape of rim and the excavation of the disk, which were pointed out as an important feature in the results. It is known that these characteristics vary with the size of the disk (Hoffman et al, 2007). Moreover, the measure of the disk size varies with the technique used, among populations. Often it is easier to detect suggestive changes of glaucomatous damaged nerves with a larger size compared to the small disks. This characteristic affects the likelihood of a doctor to make the diagnosis, being a major factor of bias, which characterizes the complexity of the process involved.

According to most specialists, it is not possible to make the diagnosis of glaucoma without characteristics changes in the visual field, which represents a significant loss of neural tissue, in which functional injuries are most often irreversible.

Therefore, researchers have pursued ways to find the changes that precede these symptoms for a diagnosis and early treatment of glaucoma. Such searches are based, most of them, on morphological changes of the optical disk and the layer of nerve fibres, as detected by the OCT.

The neural network can help the doctor in the diagnosis since these physical measures of disk are mathematically related, so it is possible to correlate them and generate an output profile of the pathology. In this study, through the use of neural networks, there was a significant hit rate of this pathological profile characterized by changes in retinal NFL, which suggests presence of glaucoma.

As discussed in the previous section, it was expected that the variable width of rim, excavation diameter, disk diameter and average width of nerve were relevant to the indication of glaucoma. However, other studies are still needed to understand the complex relationship between size of disk, neural tissue, demographic factors and the development of glaucoma.

The suppression of the 4 input variables related to NFL thickness in the second experiment did not prevent the high performance of networks using the other variables. The hit rates in patients with dysfunction in retinal NFL were still satisfactory.

Therefore, this work provided an important result as it proved that it is possible to detect the presence of retinal NFL dysfunction, or at least simulate the result of the statement obtained on OCT, using neural networks fed by variables that can be obtained by different and cheaper exams.

Other classification methods besides ANN could be tested with the available database, such as support vector machines (Cristianini, 2000) (Haykin, 1999) and hybrid neuro-fuzzy models (Gonçalves et al, 2006) (Vellasco et al 2007) (which would also allow one to extract fuzzy rules that could generate linguistic rules over the classification problem). However, in this work we chose the ANN models to classify our data, because they fit well the desired automatic, accurate and cheap method profile. It is known that ANN have an excellent performance in classification problems due to their universal approximation characteristics, and they are also recommended in problems where the formulation is not easily defined, such in this application.

Despite this work achieved success in identifying patients with retinal dysfunction of CFN, it only suggests the presence of glaucoma, and consequently further steps can be suggested.

One of them would be to better evaluate the performance of the networks obtained, using a new database where the patients would have a clinical diagnosis of glaucoma. It would be good to assess the direct relationship between the variables of entry and the final diagnosis of glaucoma. This study could be important because it would indicate how important the retinal NFL is in the diagnosis of glaucoma.

Another step would be to include data from clinical diagnosis such as visual field and campimetry. Using these data it would be possible to quantify the importance of each of these exams in the final diagnosis of glaucoma, and possibly find a good set of examinations for aid in the diagnosis of glaucoma through the use of neural networks.

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