Shadow Artifacts Correction on Fine Art Reproductions

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Abstract. The paper under consideration deals with information technology for correction of shadow artifacts on colour digital images obtained by taking photos of paintings with the purpose of their reproduction. Appearance of shadow artefacts is caused by different intensity of picture lighting. The problem of shadow detection and subsequent colour correction in this area is solved.

1 Introduction

Digital images of paintings are used to create the reproductions of pictures, virtual museums, and digital catalogues of paintings preserved in the museums. Usually, they are obtained by one of two ways: either by direct recording into the digital camera, or by scanning the negative images and slides made before. When taking a photo of a picture, the main problem is to provide a uniform intense lighting of the entire picture surface. For this purpose, the painting is lighted from both sides by floodlight projectors. Thereby, due to different remoteness of illuminators, shadow stripes are appearing along the edges of the frame.

Paper [1] deals with the task of removing the shadow using two images of the same subject, one of which has been obtained in the natural environment, and the other by means of additional lighting (i.e., flashlight). The problems of color reproduction and correction of color artifacts on digital images were also solved in papers [2-7], [14].

In these papers, cases of uniform shadowing along the image area were investigated.

In this paper, we consider an information technology for removing the shadow in a situation, when the single unique copy of painting is available, and the shadows are located in some area. The paper deals with correction methods based on applying an algorithm for histogram transformation and identification of formal transformation model of lightness function.

2 **Problem Definition**

The registration of fine art image is suggested to be implemented in such a way, that the axes of coordinates connected with the sides of a rectangular picture frame and digital image are parallel.

For definiteness, let us suppose that a system of coordinates begins at the left lower corner of a rectangular picture frame, the OY-axis is directed upwards, and the OX-axis directed to the right. Axes oy and ox of the rectangular window of registration device are directed accordingly, and deviations of these axes OY, oy and OX, ox from parallelism may be neglected.

In the present paper, we limit our consideration to removing a shadow stripe along the left lateral side of image, so that the left boundary of stripe coincides with the *OY*axis. One can easily note that the algorithms for removing the shadow stripe located along any boundary of image will not change, if system of coordinates will be rotated accordingly.

Usually, the lighting equipment does not cause any perceptible color distortion. That is why in the present paper, to detect and remove the shadow distortion, we only use information about lightness of pixels. It is known [8] that the information is contained in the lightness components of some color spaces. Specifically, the *CIE Lab* color space is used in the present work.

In case when the lighting equipment causes any additional color distortion, correction is also to be performed in channels carrying the information about color. As these distortions are distributed uniformly along the image field, the task can be solved after removing the shadows by methods considered in papers [2-7].

Let us give the definition of a shadow. Let k be a number of row parallel to ox-axis and reckoned in the direction of oy-axis. Consider an interval [0, N] in this row. Let $s^* < N$ be some point within the interval. Assume that for the k-th row of the minimum that is the same matrix of means within the interval.

Let s < N be some point within the interval. Assume that for the k-th row of the uniformly illuminated image, the equality of means within the intervals left and right from this point is valid:

$$\frac{1}{s^{*}}\sum_{i=1}^{s^{*}}L_{k}\left(x_{i}\right) = \frac{1}{N-s^{*}}\sum_{i=s^{*}+1}^{N}L_{k}\left(x_{i}\right)$$
(1)

where $L_k(x_i)$ are values of lightness at the x_i -th points of the k-th image row.

As a shadow on the interval $[0, s^*]$ we shall call a distortion, whereby for any interval $[s^b, s^e] \in [0, s^*]$ holds the following inequality

$$\frac{1}{s^{e} - s^{b}} \left(\sum_{i=s^{b}+1}^{s^{e}} \widehat{L}_{k}(x_{i}) - \sum_{i=s^{b}+1}^{s^{e}} \widecheck{L}_{k}(x_{i}) \right) > d$$
(2)

where *d* is a parameter characterizing the shadow intensity. Here and elsewhere, the values of lightness, in case of the illuminated dots of image, are designated as $\hat{L}_k(x_i)$, and in case of the shaded dots as $\check{L}_k(x_i)$.

Due to the fact that the light source is not a point source, the shadow boundary, as a rule, proves to be fuzzy. In this case, the definition of shadow (1) and (2) still holds, if the diffusion function is smooth and has no ridge point (sign reversals of the derivative). In this case, as a frontier point s^* of shadow field we take a point, where the diffusion function is equal to half-sum of its extreme values. From now on this point will be called middle point of twilight area. Thus, the locus of s^* is a boundary shadowed area. Examples of the s^* locus are shown on fig. 3.

Furthermore, the shadow field for various rows k may differ because of the relief of picture frame. Thus, the shadow field has two regions, the distortion character of which and, consequently, the methods for their correction must differ, and the boundaries of these regions are in general not rectilinear.

Directly to the OY -axis adjoins the (main) area with the uniform shading, the latter being determined by the parameter d. Between this area and illuminated area there is a twilight area, generally more narrow, which shading is decreasing towards the OX -axis. The boundaries of the twilight area separating it from the shaded and illuminated fields are curved. Usually, the X-coordinate of these curves has a slight spread with respect to a straight line parallel to the OY -axis.

Thus, the problem is to determine the boundaries of main and twilight area of shadow and to elaborate the algorithms for color correction in each of these fields taking into account the peculiarities of variations of shadow distortion intensity in each of them. The proposed information technology is oriented at implementation in a distributed computing system.

3 Detecting a Boundary of Shadow Area

The task of detecting the boundaries of shadow area is, in fact, the task of edge detection [13]. The most approximate to it is the task of edge detection in the *CIE Lab* color space considered in [10]. In the said paper, the so called method of active contours [9][11] was employed based on the theory of curve evolution. But in our case, this method can not be used in original form, as the contours of the fields are fuzzy. In the following, we consider the algorithm for detecting the boundaries of shadow area accounting for the mentioned peculiarities of contours.

The problem is solved in two steps. First, we determine a set G of points $(x_k, y_k) \in G$ pertaining to the so called midline of the twilight area oriented along the oy-axis. Then, the entire twilight area is formed in its neighborhood.

Let us consider a lightness component L of a three-component color image. To detect the boundary of shadow area introduce a criterion. For the point s^* , being a boundary of the shadow field determined by Eq. (1) and (2), the so called *contrast indicator* is introduced:

$$f(s) = C_R - C_L \tag{3}$$

where

$$C_{R} = \frac{1}{N - s^{*}} \sum_{i=s^{*}+1}^{N} \breve{L}_{k}(x_{i})$$
$$C_{L} = \frac{1}{s^{*}} \sum_{i=1}^{s^{*}} \widehat{L}_{k}(x_{i})$$

are estimates of the mean value of lightness function within the intervals $[s^* + 1, N]$ and $[1, s^*]$ respectively, and N is a number of lightness values within the investigated image area in the direction of the *ox* - axis.

Thus, it will be sufficient for the point s^* to be the boundary of shadow area at the *k*-th row, if the contrast indicator (3) is distinct from zero and assume the maximum value at this point. Consequently, to detect the boundary of shadow field it is necessary to compute the values of the contrast indicator (3) at every point of the row, to choose the row where it proved to be the maximal one, and to verify that the contrast at this point is perceptible enough. Proximity of contrast parameter values in the neighboring rows can be an additional condition of shadow existence.

We should emphasize once more that in reality the statements (1) and (2) do not hold exactly. But the differences between the means within the intervals are generally much less than the contrast caused by shadow. That is why the procedure described turns out to be effective in a wide range of shading intensity.

The following modification of indicator (3) improves the fidelity of identification in many cases. This modification is based on calculations of two means of two symmetrical intervals of *a* pixels, divided by (2b+1) pixels:

This modification is based on a calculation of mean values on two symmetrical intervals of size a, spaced (2b+1) pixels apart:

$$g(s,a,b) = \frac{1}{a} \sum_{i=s-a-b-1}^{s-b-1} L_k(x_i) - \frac{1}{a} \sum_{i=s+b-1}^{s+a+b+1} L_k(x_i)$$
(4)

here a and b are parameters, requiring additional identification.

Indicator (4) is more localized then (3) and its computation is more robust to behavior of lightness function in twilight area. If distance(2b+1) is greater then width of twilight area, then maximum value of indicator (4) does not depend on lightness function behavior. When b = 0 and a = N the indicator (4) acts like indicator (3), when b = 0 and a = 1 this is like expression for first difference.

The shadow boundary point is defined by:

$$s^*(a,b) = \arg\max g(s,a,b).$$
⁽⁵⁾

Typical values of indicator (4) and s* is shown on figures 1. and 2. On first figure profile of lightness function L for 50-th row of image from fig 3a is shown, also on this figure the line chart of g(s, 20, 15) is presented. On the next figure is shown the graph for s* function for fixed value of b. Presented graphs are typical for most row of investigated image, thus indicator g(s, 20, 15) can be used for shadow boundary detection on this image.



Fig. 1. a) Graphs of the lightness function and of the contrast indicator for the 50-th row for image form fig. 3 b) Graph of s*(b) dependence.

If the values $L_k(x)$ are distorted by the noise (particularly, by the impulse one), the errors of detecting the shadow boundaries in different rows may occur. To maintain the smoothness of shadow field boundaries by the transition from $y = y_{k-1}$ to $y = y_k$, the additional restriction may be imposed:

$$\left|x_{k}-x_{k-1}\right| < \Delta_{dist} \tag{6}$$

Here, x_{k-1} is a point pertaining to the midline of twilight area at $y = y_{k-1}$, Δ_{dist} is a variable defining the maximal admissible jump. If an initial point of midline within the twilight area $(x_0, y_0) \in G$ is specified, subsequent applying the expression (6) allows us to determine the sufficiently smooth shadow border (set *G*).

4 Detecting the Boundaries of a Twilight Area

In the course of correction on the twilight area the fact, that the width of this area is varying at different image areas should be taken into account. This is caused by variances of distance between different parts of the frame and the light-source. In particular, on the edges of the frame which are more distant from the light source, the shadow boundary is moving off from the *oy* -axis and the twilight area is getting wider. In this section, procedure of detecting the boundaries of twilight area with regard for the said peculiarities is considered. It is based on the midline of shadow boundary, and the method for detecting this boundary was described in the previous section.

The idea is to approximate the lightness function within the twilight area specified by the steady increasing function. Actual lightness functions may essentially differ owing to superposition of shadow upon various picture elements in the rows. This is why approximation is implemented with respect to some averaged lightness function values obtained by summing the lightness functions of several neighboring rows.

With this purpose, the values of lightness functions in the rows are taken in such a way that the indications of each row pertaining to the midline of shadow boundary coincide. Let us designate a mean of lightness function values pertaining to the

midline of shadow boundary in the local subset of rows as w(0). Mean value of lightness indications at the distance of one pixel towards the negative values of the *ox*-axis designate as w(-1), and towards the positive values of the *ox*-axis as w(1) etc.

Further on, the values of lightness function for all the rows, assigned numbers of which are equal, are averaged. As a result, for the twilight area, a set of lightness function values averaged within the local set of rows is formed (Fig. 2):

$$w(-n), ..., w(-1), w(0), w(1), ..., w(n)$$
(7)

where *n* is selected in such a way that $S_{\max} < 2n + 1 \le \min D$, where s_{\max} is the maximum possible length of twilight area within a set of all rows of the distinguished subset, *D* is a distance from the point of shadow to the next image boundary.



Fig. 2. Detecting boundaries of the twilight area.. (1) is the initial function, (2) – approximating function, (3) – point of the shadow line, (4) – amended point of the shadow line, (4-5) – boundaries of the twilight area.

To detect the boundaries of twilight area within the allocated local area of rows, we have to solve a problem of approximating the said set of lightness values (7) to a function given by

$$w(x) = \frac{b(x-c)}{1+a|x-c|} + d.$$
 (8)

Parameters c and d are introduced to estimate a shift of shadow boundary midline within the local set of rows. The bias usually occurs due to different lightness of picture elements within the illuminated and shaded fields.

Estimates of the parameters a, b, c, d for each midline of local subset of rows are made applying the least absolute values method. To make the estimates for the next row, the last row is eliminated from the local subset and a new row is added instead. As an initial approximation for subsequent rows, estimates of the parameters obtained in the previous step are used.

As a result, we have a set of parameter estimates of the function (8) for each row (except several rows from the beginning and the end). Using these estimations, the amended mean of lightness function in each row is built. In particular, position of a

point pertaining to the midline of shadow boundary, and the values of approximated lightness function corresponding to the shifted points are amended:

 $x^{*}(i) = x(i) - c, w^{*}(i) = w(i) - d, i = 0, \pm 1, ..., \pm n.$

Using the amended approximated lightness function of twilight area for each middle of local subset of rows, the boundary values of twilight area are defined by

$$x_{bor} = x_0^* \pm \frac{b(1 - \Delta_{bor})}{a\Delta_{bor}},\tag{9}$$

where x_0^* is the amended coordinate of a point pertaining to the midline of shadow boundary, $\Delta_{bor} = \Delta w(x) / w_{max}(x)$, and $\Delta w(x)$ is the given admissible deviation of lightness function from the maximal value of approximating curve at the boundary point of twilight area.

Moreover, for each row in the neighborhood of the amended point pertaining to the midline of shadow boundary there is a set of values of the approximated lightness function which, in fact, are weighting factors characterizing a change of shading intensity in the direction of *ox*-axis.

5 Algorithm for Color Correction

Algorithms for color correction of shadow distortions in uniformly shaded and twilight areas are developed by a different ways. When solving a problem in the *Lab* color space only one of them (i.e., lightness component L) is responsible for a shadow. Thus, for shadow correction it seems reasonable to apply a popular method for correction the lightness of grayscale images, that is, equalisaton of histogram [11].

In the course of testing a method for transformation of histograms on test and real images, the main defect of this approach was revealed, namely, appearance of the posterization effect, i.e. merging of different, but neighboring lightness values as a result of transformation. In this paper, we develop an approach first proposed in [12] and based on solving a problem of identification of formal model for color transformation. Consider peculiarities of its applying for the present case.

Designate the coordinates of two points selected from the shaded and illuminated image areas as (x_i^l, y_i^l) and (x_i^r, y_i^r) respectively. By assumption, at the absence of shading and at uniform picture illumination, the colors of these points are similar:

$$L^*\left(x_i^l, y_j^l\right) \approx L\left(x_i^r, y_j^r\right).$$
⁽¹⁰⁾

In the following, the points meeting the condition (10) will be called *matching points*. It is obvious that for an shadowed image holds the expression:

$$L(x_i^l, y_i^l) < L(x_i^r, y_i^r).$$

Take into consideration the transformation function $\Psi[*]$ establishing a relation between the brightness values of matching points as follows:

$$L(x_i^l, y_i^l) = \Psi \Big[L(x_i^r, y_i^r) \Big].$$
⁽¹¹⁾

Having registered the lightness values for N pairs of matching points from the shaded and illuminated areas, the matrix relation can be written on the basis of Eq. (11) as follows:

$$\mathbf{L}_{\mathbf{L}} = \mathbf{L}_{\mathbf{R}}^{*} \boldsymbol{\Psi} + \boldsymbol{\xi} \tag{12}$$

Components of vector \mathbf{L}_{L} consist of lightness values at the matching points of the illuminated area. Matrix \mathbf{L}_{R}^{*} is composed in assumption that the transformation function (12) is a third-order polynomial. Components of vector $\boldsymbol{\xi}$ are errors of registration, approximating the model etc.

The sought-for estimates of transformation model parameters may be defined using the least-square method:

$$\hat{\boldsymbol{\psi}} = \left[\mathbf{L}_{\mathbf{r}}^{*\mathrm{T}} \mathbf{L}_{\mathbf{r}}^{*} \right]^{-1} \mathbf{L}_{\mathbf{r}}^{*\mathrm{T}} \mathbf{L}_{\mathbf{l}}$$

or by any other means (for example, using the least absolute values method).

Further on, utilizing the obtained estimate of vector of function Ψ parameters due to the transformation function (21), we perform a pixel-by-pixel transformation of lightness values in the shaded field according to the expression

$$\hat{L}(x_{i}, y_{i}) = \hat{\psi}_{3}L_{R}^{3}(x_{i}, y_{i}) + \\ + \hat{\psi}_{2}L_{R}^{2}(x_{i}, y_{i}) + \hat{\psi}_{1}L_{R}(x_{i}, y_{i}) + \hat{\psi}_{0}.$$
(13)

The order of model (11) may be depressed if the estimates for coefficients of higher orders of polynomial are found to be relative small.

The pixel-by-pixel transformation of lightness values in each row of twilight area is performed according to the next rule:

$$L_{i}^{*}(x_{i}) = L_{k}(x_{i}) + w(i) \cdot \Delta_{L},$$

$$\tilde{\Delta}_{L} = \Psi \left[L_{k}(x_{i}) \right] - L_{k}(x_{i})$$
(14)

where $\Psi[L_k(x_i)]$ is a transformation for the *k*-th row built in compliance with expressions (11) – (13), and x_i are coordinates of the next shaded point from the uniformly shaded area, the point being in the same row as the point under correction.

6 Results of Experiments

As test images, high-resolution digital photos of real paintings featuring a grove and sunset were used. The images processed have the size 554×3558 and 145×3933 pixels respectively. Image format is *TIFF*, color space is *Lab* (8 bit per channel). Enhanced fragments of two initial images with shadow area are shown in Fig. 3a and 3c.

The image featuring a sunset is more complex in respect of detecting the shadow boundary. Main difficulty consists in large dimensions of the twilight area (up to 120)

pixels). Besides, the width of this field is varying within the wide limits according to the value of *y*-coordinate.

On the image featuring a grove, the shadow boundary is rather distinct, which is determined by small width of twilight area, whereby the boundary is almost rectilinear. Both images feature a large number of contrast elements and are characterized by a wide range of lightness variation in channel L. Moreover, both images are noisy. Said peculiarities essentially complicate identifying the weight function (8) in the twilight areas.

Mean values within the twilight area of image featuring a sunset are represented by a white line in Fig. 3a, c. End result after shadow artifact removing is represented in Fig. 3b, d.

In this paper we present only two shadowed image, but our system was tested by prepress specialists on about 200 images and demonstrates sufficient quality in 75% cases. In other cases images needs some further correction. Altogether, autoimmunization of shadow correction process reduce time needed for processing one shadowed image from about one hour till 2-3 min.



Fig. 3. Example of colour correction of images with the curvilinear boundary of shadow stripe and area of slowly changing colour: a), c) initial images with the detected shadow line; b) d) images after correction.

7 Conclusions

The elaborated information technology for color correction of shadowed images admits a high automation degree. Its software implementation has resulted in essential reducing the time expenditures for prepress of color images. Apart from preparation of painting reproductions, the technology may be employed to process the areas of images obtained by aerospace monitoring systems and intended for print, and to provide the services of improving the quality of digital images to a wide range of users.

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