

KNOWPATS: PATTERNS OF DECLARATIVE KNOWLEDGE

Searching Frequent Knowledge Patterns about Object-orientation

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Abstract: In order to better understand the structure of students' knowledge in computer science, we are trying to identify patterns – in form of frequently occurring subgraphs – in concept maps. Concept maps are an externalization of a person's declarative knowledge represented as a graph. We propose an algorithm that can be employed to identify frequently occurring subgraphs, based on existing algorithms in that field. We are currently working on a project that will gather concept maps from a large group of freshman in the coming semesters, providing us with extensive material for information mining about the structures of knowledge in CS. We hope to get a better understanding of the relationship between knowledge and competence.

1 INTRODUCTION

During the last decades, the focus of educational research activities has shifted from knowledge to competencies. This makes sense, because at the end of the learning process the students should be able to *do* something instead of just to *talk* about it. Nevertheless, it might still be helpful to have an idea of the knowledge that is needed to gain a certain competency. Nearly every teacher has already heard a student sigh: “If I had known this before!” after having solved a problem finally. Particularly, if learning environments are designed following modern constructivist approaches, the students should be active and should try to find solutions on their own. If the teacher has a very detailed idea of what the students need to know, he or she is able to support the learning process with short, precise information input.

Therefore, our long-term goal is to identify the prerequisite knowledge for certain competencies. As subject domain we chose the field of object-oriented modeling and programming, because it is central to Informatics in schools as well as in universities.

The first step was to find and evaluate suitable methods for the investigation of student knowledge. To this purpose we have investigated the structure of the knowledge that was presented during a typical non-major CS1 course (for students of engineering) by extracting the relevant information out of the

teaching material (textbook and slides) and by asking the students to draw concept maps at different points in time during the course. That way, we tried to find out how the presented knowledge was taken up and later externalized by the students. Additionally, we are collecting concept maps about object oriented programming from high school teachers and students as well as from bachelor and teacher students of Informatics at our university.

Our next goal is to identify typical *knowledge patterns* (which we call *knowpats*) in the student maps that might have been similarly presented in the lectures. As our next step we want to find out how the knowpats as expressed by the students correlate with the type and duration of Informatics courses they had attended at school. Finally, we aim to correlate these patterns with certain competencies.

2 BACKGROUND

First of all we have to limit the range of knowledge that might be relevant to our research. For this purpose we rely on the categorization of (Anderson 2009), because it was designed for a similar purpose, namely the assessment of learning objectives. They distinguish between:

1. *Factual Knowledge*: “basic elements that students must know to be acquainted with a discipline or solve a problem in it”,

2. *Conceptual Knowledge*: “the interrelationships among the basic elements within a larger structure that enable them to function together,”
3. *Procedural Knowledge*: “how to do something: methods of inquiry, and criteria for using skills, algorithms, techniques and methods,”
4. *Metacognitive Knowledge*: “knowledge of cognition in general as well as awareness of one’s own cognition.”

A comparison of the definitions (see e.g. Anderson 2009; Anderson, 2005) shows that factual knowledge can be represented by propositions, Conceptual knowledge by propositional networks, semantic networks or schemata. Procedural knowledge might be described by *scripts* following (Schank and Abelson, 1977), while Metacognitive knowledge might be hard to describe anyway.

The first two categories describe both declarative knowledge, but we are interested mainly in the second category, which comprises “‘mental models’, ‘schemas’ or ‘theories’ that individuals may use to help them organize a body of information in an interconnected, non-arbitrary and systematic manner” (Anderson, 2009).

There are many research activities that use concept mapping techniques in order to investigate cognitive structures, for example (Vanides et al., 2005). The students are asked to draw a graph with nodes representing concepts and with edges symbolizing associations between these concepts, e.g. “is a”. There are many measures for the assessment of concept maps and many validations for these measures, e.g. (Shavelson and Ruiz-Primo, 1999), (Albert and Steiner, 2005). (Sanders et al., 2008) compared the knowledge of students in several nations using concept mapping techniques. (Goldsmith and Davenport, 1990) developed a graph-theoretical measure for the similarity of graphs based on neighborhood structures. (McClure et al., 1999) validated this measure by correlating it with several scoring techniques. Hereby, they also detected that the scoring of locally correct edges using a master map is the most convincing scoring technique for concept maps.

Nevertheless, we have to remember that a concept map does not represent the knowledge of its author directly, but has to be regarded merely as an externalization of this knowledge that might be influenced by motivation, by the focus of attention or by many other external influences (Norman, 1983).

Concerning the representation of the specific subject domain knowledge of object-oriented programming, (Pedroni and Meyer, 2010) proposed to organize it in *Trucs*, (testable, re-usable units of cognition) which are collections “of concepts, opera-

tional skills and assessment criteria”.

Usually the students start drawing concept maps with a list of given concepts that they have to pick nodes from and connect them by associations (Sanders et al. 2008). Suitable concepts that could be included in such a list might be taken from the “the quarks of object-oriented development” that were identified by (Armstrong, 2006), comparing several definitions of “object-orientation”.

(Mons et al. 2008) introduced *knowlets* as small knowledge elements, which are restricted to the connection of two concepts. In regard of constructivist learning approaches we need larger graph structures, as (Kinchin et al., 2000) argues.

For the mining of frequent patterns in large graphs (Inokuchi et al., 2000) proposed the Apriori-based Algorithm *AcGM*. It uses the monotony of the *support of induced subgraphs*. $G_s = (V_s, E_s)$ is an induced subgraph of $G = (V, E)$ if and only if $V_s \subset V$ and $\forall v_1, v_2 \in V_s: (v_1, v_2) \in E \Leftrightarrow (v_1, v_2) \in E_s$. The definition of the support of G_s is

$$sup(G_s) = \frac{N_s}{N}, \quad (1)$$

with N_s being the number of graph transactions G where $G_s \subset G$ and N being the total number of graph transactions of G . A transaction in our context is just a graph. If G_1 is an induced subgraph of G_2 , the monotony can be expressed as

$$sup(G_2) \leq sup(G_1) \quad (2)$$

This allows to derive candidates for frequent subgraphs of size k from already found frequent subgraphs of size $k - 1$.

(Dominguez, 2010) applied a clustering approach to Mining for hints in eLearning. They used the K-Means clustering algorithm to group the students according their abilities according to their answers on 25 questions. Following this, association rules and numerical analysis were applied to find common patterns affecting the learners’ performance that could be used use to provide hints to the students of the following years.

(Madhyastha and Hunt, 2009) presented a method for mining multiple-choice assessment data for similarity of the concepts that were represented by the multiple choice responses. They used the resulting similarity matrix to visualize the distance and hereby the relative difficulty of concepts among the students in the class.

(Romero et al., 2010) explored the extraction of rare association rules, gathering student usage data from a Moodle system. They defined rare associa-

tion rules are those that only appear infrequently there even though they might be highly associated with very specific data. Thus, these rules are supposed to be appropriate for using with educational datasets since they are usually imbalanced. To this purpose they compared several frequent and rare association rule mining algorithms, e.g. the A priori-Frequent algorithm.

3 DECLARATIVE KNOWLEDGE

For our investigation we chose one of our currently running courses, introducing freshmen of engineering into the fundamentals of object-oriented programming (CS1 for non-majors). The course was attended by about 40 students and taught in German language, thus all the text material, the concepts and the concept maps had to be translated from German to English for this paper.

In order to compare the knowledge that was externalized by the students with the knowledge they *should* acquire by studying the course material, we tried to find representations of the relevant information that are as formal as possible. For that purpose we have summarized all learning elements that we expect the students to know by reducing the slides and the textbook for the course (Hubwieser et al., 2008) to a list of “naked” statements without any examples or explanations (called *knowledge elements*), for example:

The state of an object is determined by the values of its attributes. (*)

In order to derive a list of concepts that should form the possible nodes of the concept maps, we reduced these statements in the following steps:

At first we listed all words that were contained in the texts, sorted this list alphabetically (case-sensitive) and removed all words starting with a lower case letter. In German, this condition assures that the deleted words are all non-nouns. We removed all remaining non-nouns, transformed all words to singular nominative and removed all variations or abbreviations of the same noun. Finally, all proper nouns and all purely didactical, organizational and pedagogical keywords were omitted. Afterwards, we coded and categorized the resulting set of words following the rules of qualitative research (Mayring, 2000), finally obtaining a list of 40 concepts (CL), e.g. *aggregation, algorithm, association, attribute, class, condition, conditional statement*.

We asked the students to draw their maps in the following way: We presented the concepts of CL in

the form of a checklist. At first the students should check all the concepts that they believed to know something about. Following this, they should draw a graph, using the checked concepts as nodes and connecting these by associations, which all should be denoted by suitable labels. For the evaluation of the maps we have removed all associations that were not labeled, assuming that these did not reflect any precise knowledge.

To get an “expert map” that is as objective as possible, we derived it from the same material that we have used for the derivation of our CL. We coded all sentences from the list of the *knowledge elements* (see above) by the occurrence of one or more of the 40 concepts of CL. Afterwards we produced a list of all sentences that were marked with two or more concepts of CL, assuming that these sentences might suggest associations between those concepts. For the structure of our knowpats, we were interested in the assumed arity of the associations (see table 1) that were suggested by the 161 sentences that contained more than one concept.

Table 1: Assumed arity of suggested associations.

| Number of concepts | Number of sentences | Percentage |
|--------------------|---------------------|------------|
| 2 | 101 | 62,7% |
| 3 | 40 | 24,8% |
| 4 | 17 | 10,6% |
| 5 | 3 | 1,9% |

Following this, we translated the information that was contained in these sentences to associations by qualitative means, which ended up with a set of 98 associations that formed our *objective expert map* and that was used e.g. to score the students’ maps by comparing the names they gave to their associations with the respective names in the expert map.

4 DATA GATHERING

Over the academic year 2010/11 we have gathered a variety of concept maps from students of different groups.

As described in Detail in (Hubwieser and Mühling, 2011) we have collected four generations of concept maps from the students of the CS1 course at four distinct points in time. As the drawing was done partly in the main lecture and partly in the tutorials, we had varying numbers of participants. The pre-test was done by 39 students before the course started. The first mid-test was done by 38

students after 4 weeks. Three weeks later, the students had to pass a small midterm exam.

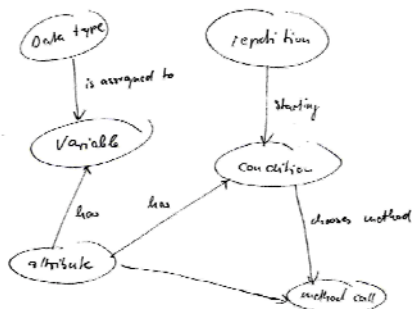


Figure 1: Exemplary concept map from a student.

One week later, another collection of concept maps yielded 19 student maps. Finally, immediately after the end of the lecture and some weeks before the final exam, there was a last test (post-test) that was attended by 17 students. In the final exam, 13 students gave us their code number and hereby allowed us to correlate their maps with their scoring in the exam.

After the Bavarian government has shortened the number of grades of the Gymnasium from 9 to 8 (from the type G9 to type G8) and introduced a new compulsory subject of Informatics simultaneously in 2003, we will welcome two different age groups of freshmen at the universities this year. The first group has entered Gymnasium in 2003 (graduated from G8), the second has started G9 at 2002. More interestingly, there are 5 groups of freshmen regarding their education in Informatics (shortly called *EI-groups*): graduates from G9 didn't have any regular education in Informatics, graduates from G8 have had, depending from their direction of study, 2 or 4 years of compulsory education and, eventually depending from their choice of courses, 1 or 2 years of elective courses.

Due to a specific program of our university, the graduates from G9 were allowed to start their studies already in summer 2011, while nevertheless, most of them will enroll regularly at autumn 2011. Therefore we have the singular opportunity to compare the knowledge about Informatics of freshmen that belong to several different *EI-groups*. We are collecting concept maps together with interviews dealing with the ideas about typical topics and characteristic working methods of Informatics and about the reasons for their choice of Informatics as major. Our goal is to find correlations between the declarative knowledge (knowlets), the ideas about and the attitudes towards Informatics and the *EI-groups* of the students. In October 2010 we have already collected

concept maps and interviews from about 100 freshmen (G9). Some weeks ago, we have collected another 250 sets, which we are scanning and digitalizing currently. After having completed their first semester, we hope to collect a second generation of concept maps from these 250 students in October, and another 250 sets of maps and interviews from the freshmen that will enroll at this time.

Additionally we are collecting concept maps in a longitudinal study at a several classes (of grade 10 and 11) at a local Gymnasium (called GYS). The goal is to detect if there are relevant differences in the concept maps compared to the students at university. Finally, we will collect concept maps from the teachers using a specific internet based tool (*CoMapEd*) that is under construction at the moment. Based upon the results of our teacher survey from 2009 (see Mühling, Hubwieser & Brinda 2010), we expect about 300-400 teachers to draw a concept map, using the same concept list CL as described above.

5 DATA ANALYSIS

Before analyzing the CS1 maps, we normalized the labels of the edges (which were freely chosen by the students) in the following way: all verbs were transformed to a standard form (first person singular indicative), all isolated prepositions and articles were deleted, all auxiliary verbs were removed, isolated nouns or adjectives were deleted and all multiplicity specifications ("some", "many" etc.) were removed. In the next step we categorized the resulting labels from all surveys, following the rules of qualitative text analysis (Mayring, 2000).

Based on this categorization, all associations were scored by the lecturer of the course with points (0 points for "totally incorrect", 0.5 points for "partly correct" and 1 point for "totally correct"). This was performed by comparing the categories locally to the *objective expert map* (see section 3), following the technique "relational with master map" suggested by (McClure et al., 1999).

5.1 Analysis of the Maps as a Whole

The results of the formal analysis of the CS1 maps are described in detail in (Hubwieser and Mühling, 2011). First of all we detected that the students did not use many different labels, although they were totally free in choosing them. There were only 16 categories of association labels that were used in more than 2% of all edges of at least one survey, and

additionally their relative frequency was very similar over the four surveys. If we set the threshold at 5%, there remained only 5 different labels. 35% of all associations over all surveys were labeled with a word that was synonymous to *contains* or to *has*. This result suggests that it is possible to restrict the labeling to multiple choice without losing too much information, which would ease automatic scoring dramatically.

Concerning the graph theoretical measures we found that the average number of correct edges increased from 3.0 in the pretest to 11.0 in midstest2, which showed that the students were learning indeed. We also found a significant high correlation (0.68 with a p-value of 0.002) between the number of correct edges in the first mid-test with the achieved score in the midterm exam.

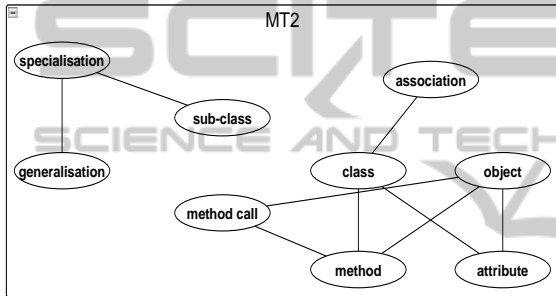


Figure 2: High-scored associations for Midtest 2.

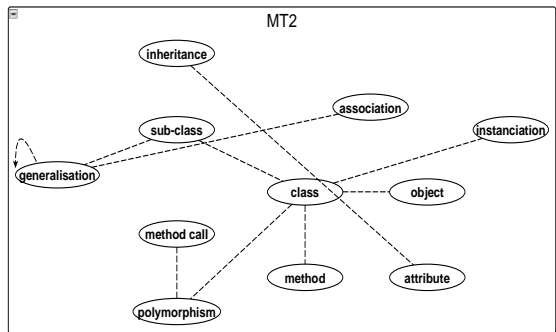


Figure 3: Low-scored associations for Midtest 2

By selecting only the edges that were labeled mostly correct (restricted to 9 the most important concepts for object-orientation), we could identify the concepts where the learning process was most efficient (see Figure 2).

In contrary, the edges that were labeled mostly incorrect show the problematic concepts (see Figure 3). More details are presented in (Hubwieser and Mühling, 2011).

5.2 The Internal Structure of the Maps

As already explained in the introduction of this paper, we are looking for patterns in the concept maps that are frequently used by the students. We called this patterns *knowpats*, which we define as induced subgraphs of concept maps. We will look for frequent knowpats in the student maps at four different levels, which allows the reduction of the regarded graphs to undirected ones:

1. *General Level*: The labels that have been given by the students to the associations are ignored (as long as there is any label). The existence of any labeled association means that the student at least knows that there is some connection between the two concepts (Kinchin et al., 2000).
2. *Scoring*: only edges that have a score > 0 are taken into account, thus taking into consideration all totally correct as well as all partly correct edges.
3. *Total Correctness*: Only the totally correct edges are considered.

As we suggest that the students get their knowledge mainly from the material that was presented in the course, the assumed arities of associations that were suggested by these texts (see table 1) restrict the range of the size of the expected knowpats from 2 to 5.

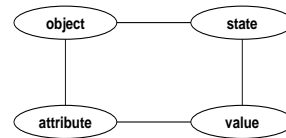


Figure 4: Knowpat suggested by knowledge element (*).

For the search we will apply the *AcGM* Algorithm of (Inokuchi et al., 2000), which can be adapted to our purposes and environment. It extracts frequently occurring subgraphs (in our case knowpats) from a large database of graphs (in our case concept maps) and is especially suited for finding large subgraphs, as it successively builds larger and larger candidate subgraphs and checks how often they occur in the database.

We could simply use the *AcGM* algorithm for the task. However, as we're dealing with a problem that contains the NP-complete subgraph-isomorphism problem, it might be worthwhile to adapt the algorithm for our specific needs, in order to achieve somewhat better running times in real-life scenarios.

Firstly, concept maps are typically directed, small and sparse graphs. The list of concepts puts a

bound on the number of vertices, so those will never exceed 50 at most. Additionally, even if the graphs are not always strictly DAGs, they tend to resemble directed trees (or forests) and can be considered sparse graphs in which the number of edges grows at most linear with the number of nodes.

Secondly, as outlined above, we're only concerned with subgraphs of size 2 to 5 nodes. As there are only three knowledge elements with an arity of 5, we might exclude these from the analysis, leaving us with subgraphs with at most 4 nodes. The nice thing about this is that there are well established algorithms for finding subgraph-isomorphisms with 3 and 4 nodes (e.g. the VF2 algorithm by Cordella et al., 2004). For 2 nodes the isomorphic class of a subgraph is trivially decided by using the edge count of the induced subgraph. That means, we can avoid the coding and normalizing of the adjacency matrices that's a big part of AcGM and instead use existing algorithms for those sub-tasks.

Thirdly, we're interested in connected subgraphs only. A missing connection can never serve as evidence in favor of a knowpat since we cannot infer anything from it, by itself.

For the analysis, we treat the concept maps as undirected graphs, as the direction is only dependent on the chosen edge label and not on the concepts involved. Multiple edges between concepts will then be collapsed into one. The graphs may still contain self-loops however. Typically, isomorphism checking relies on simple graphs (as does the AcGM algorithm), so we'll either have to ignore self-loops or transform the concept maps into a simple graph first. As they may very well contain valid statements (e.g. object - communicates with - object) they should not be ignored. Transformation is easily done by adding, for each self-loop $\{v, v\} \in E$, a new node with the same label as v and replacing the loop with an edge to the new node (keeping the label of the edge).

In the worst case, this doubles the size of our graphs, but in real life, the data typically only exhibit a very small number of self-loops.

After this step, we have a database of simple, undirected graphs. The main algorithm based on the ideas of AcGM works as follows:

Starting with the only connected isomorphism class of size 2 (two nodes connected by an edge), we count the frequency for each pair of nodes in the database. This can easily be done by simple counting and comparing the entries in the adjacency matrices. For example, the following associations were the most frequently used at the CS1 course among 1.665 associations in 115 maps: (class, object) with 58

occurrences, (data, data type) and (object, attribute) with 44 occurrences each.

Starting from this, we get a list of candidates that have a support higher than a chosen threshold. For sparse graphs, this list will contain $O(|V|)$ entries.

From these frequently occurring size 2 subgraphs, we can create the list of candidate size 3 subgraphs that need to be checked. According to the observation in AcGM, those must be formed by combining two subgraphs of size 2 that have a high enough support and that share exactly one node. We can simply do a pairwise join of the size 2 candidates and extract all those with 3 nodes. All those candidates exist in exactly two forms: Either with 2 edges, or with 3.

We count the frequency of those candidates in our database using the VF2 algorithm. Finally, the list of frequently occurring size 3 subgraphs leads to a list of candidate size 4 subgraphs, again by recombination of two size 3 graphs that share exactly 2 nodes. Those too, exist in two forms, one in which the two non-shared nodes are neighbors and one in which they're not.

This leaves us with a final list of at most $O(|V|^4)$ entries. However in real life we expect the lists to be much shorter. The frequency of those candidates will then be found again using the VF2 algorithm.

While there really is no way around the combinatorial complexity when searching the subgraphs in the database, this approach at least only creates a small subset of all possible size 3 or 4 subgraphs according to what actually can be present in the database. As the algorithm is in a certain way more sensitive to the size of the graphs than to the number of graphs, we should be able to handle the large amounts of data that arise in the current and subsequent studies.

6 CONCLUSIONS

We presented a method that allows searching for small, frequently recurring subgraphs in a database of concept maps. We take those subgraphs as indicators for recurring structures in declarative knowledge in computer science (called knowpats). Finding knowpats will allow us a deeper understanding of the prerequisite knowledge that a competent CS student needs to possess. As we have collected many comparable maps from freshmen of CS, we hope to find such patterns there. Once candidate patterns are identified, the next step will be to validate them (for example by using a broader, more diverse group of students as the basis) and to investigate how those

candidates correspond to the actual abilities and the biography of the students. Clearly, knowing about the internal structures of CS knowledge is also an effective way of evaluating and designing CS courses.

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