

HaF

A New Family of Hash Functions

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Abstract: Paper presents a family of parameterized hash functions allowing for flexibility between security and performance. The family consists of three basic hash functions: HaF-256, HaF-512 and HaF-1024 with message digests equal to 256, 512 and 1024 bits, respectively. Details of functions' structure are presented. Method for obtaining function's S-box is described along with the rationale behind it. Security considerations are discussed.

1 INTRODUCTION

In many cryptographic applications it is necessary to generate a shortened form of a much longer message. The shortened form called digest of the message or hash value, is produced by means of a hash function. A hash function h operates on an arbitrary-length message m and returns a hash value $h(m)$ of a fixed length. Cryptographic hash functions have many information security applications. We use hash function to verify message integrity. Keyed hash function is used for message authentication.

Recently we can see substantial effort in designing of new cryptographic hash functions. For example, as many as 64 proposals were submitted to NIST SHA-3 competition, for new hash function, in October 2008 (Regenscheid, 2009).

Our objective is to ensure that the security of HaF is high and its performance is significantly satisfactory.

The paper is organized as follows: Section 2 presents general overview of the family of algorithms. Method for obtaining function's S-box, along with the rationale behind it, is described in Section 3. In Section 4 we discuss security considerations. Section 5 is devoted to reference implementation and the algorithm performance. Concluding remarks are presented in Section 6.

2 PARAMETERIZED FAMILY HaF OF HASH FUNCTIONS

2.1 Design Principles

The following assumptions were taken into account during design process:

- the family should be parameterized;
- message digest length should be selectable;
- flexibility between performance and security should be guaranteed;
- iteration structure and compression function should be resistant to known attacks;
- its iteration mode should be HAIFA (it provides resistance to long message second preimage attacks, and handles hashing with a salt) (Biham, 2006).

2.2 Description of HaF

The HaF family is formed of three hash functions: HaF-256, HaF-512 and HaF-1024, producing hash values (message digests) with the length equal to 256, 512 and 1024 bits, respectively. The general model for HaF is based on Merkle-Damgård paradigm proposed by Biham and Dunkelman (Menezes, 1997); (Biham, 2006) (Figure 2.1).

After formatting the original message m we have the message M . We divide M into blocks M_0, M_1, \dots, M_{k-1} , $k \in \{1, 2, \dots\}$, and each block M_i is processed with the salt s by the iterative compression function

φ (Biham, 2006). The output H_k is the final result of the function.

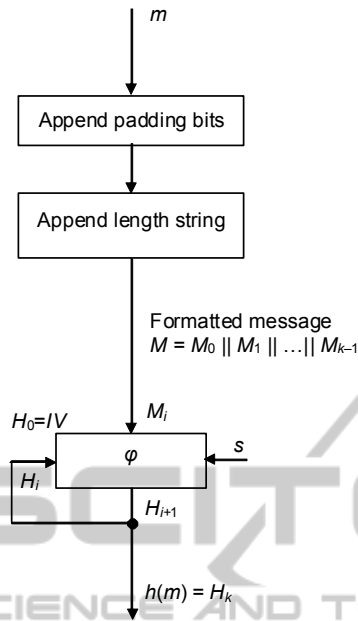


Figure 2.1: General model for HaF.

2.2.1 Notation

In the paper we use the following notation:

- $a \odot b$ – multiplication mod (2^n+1) of n -bit non-zero integers a and b ;
- A_r – working variable, $r = 0, 1, \dots, 15$;
- F_j – step function, $j = 0, 1, \dots, 15$;
- $GF(2)$ – Galois field of characteristic 2;
- $length$ – bitstring representing the length of the original message m , $|length| = 128$;
- $lsb_q(v)$ – q least significant bits of the string v ;
- IV – initial value;
- m – original message, $|m| < 2^{128}$;
- M – formatted message;

n – length of the working variable A_r (16 or 32 or 64 bits);

- s – salt, $|s| = 16n$;
- $|v|$ – length in bits of a string v ;
- $v \ll t$ – t -bit left rotation of a string v , $|v| = 16n$;
- $v \oplus w$ – bitwise XOR of strings v and w , $|v| = |w|$;
- $v \boxplus w$ – addition mod 2^n of integers represented (in base 2) by strings v and w ;
- $p_1(x) \otimes p_2(x)$ – multiplication of polynomials p_1 and p_2 modulo an irreducible polynomial $R(x)$;
- x^q – bitstring of the length q ; x^0 means the empty string;
- φ – compression function;
- $||$ – concatenation of bitstrings.

2.2.2 Message Padding

The original message m has to be formatted before hash value computation begins. The length of formatted message should be a multiple of $16n$ bits. The message m is formatted by appending to it a single 1-bit and as few 0-bits as necessary to obtain a string whose bit-length increased by 128 bits is a multiple of $16n$. Finally we must additionally append original message length. As a result we obtain the formatted message $M = M_0 || M_1 || \dots || M_{k-1}$ for some positive integer k , where M_i is a block of M . Therefore, $M = m || 10^t || length$, where t is the smallest nonnegative integer necessary to format m , and $|M| = 16nk$.

2.2.3 Compression Function

In the proposed schema the compression function is defined as follows: $\varphi: \{0,1\}^\mu \times \{0,1\}^\eta \times \{0,1\}^\sigma \rightarrow \{0,1\}^\rho$. The integers μ , η and σ are lengths of block M_i , chaining variable H_i , and salt s , respectively, where $|M_i| = |H_i| = |s| = 16n$ and $i = 0, 1, \dots, k-1$. The integer ρ is the length of the resulting hash value $h(m) = H_k$, $|h(m)| = 16n$.

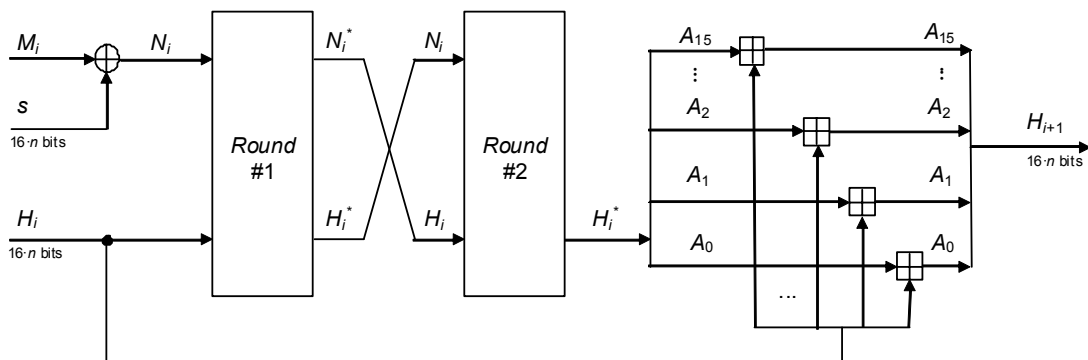


Figure 2.2: Method of one block processing.

The block M_i is processed in two rounds. The length of the block equals $16n$ bits, where n is a parameter depending on the hash value we want to obtain. For HaF-256, HaF-512 and HaF-1024 the parameter n equals 16, 32 and 64 bits, respectively. The parameter n indicates in fact the length of the working variable A_r used in the step function.

The method of one block processing is depicted in Figure 2.2. M_i , H_i and s are inputs for φ . Before processing in round $\#l$, $l = 1$ or 2 , the block M_i is modified. In the round $\#1$ four least significant bits of $N_i = M_i \oplus s$ indicate the number of bits the string N_i is rotated to the left: $N_i^* = N_i \ll ls_b_4(N_i)$. Before processing in the round $\#2$ the blocks are permuted: $N_i = H_i^*$ and $H_i = N_i^*$. After two rounds, the value H_i^* of chaining variable is split into 16 subblocks A_0, A_1, \dots, A_{15} of equal lengths. Each of them is modified by adding (mod 2^n) the respective input subblock of H_i which is the input to the round $\#1$. Next, all subblocks A_0, A_1, \dots, A_{15} are concatenated giving $H_{i+1} = A_0 \parallel A_1 \parallel \dots \parallel A_{15}$.

2.2.4 Round Function

The round function (Fig. 2.3) has two inputs N_i, H_i and two outputs N_i^*, H_i^* . The input block N_i is rotated by the number of bits corresponding to $ls_b_4(N_i)$ and added (mod 2 of respective bits) to H_i . Next the block $H_i \oplus (N_i \ll ls_b_4(N_i))$ is divided into

16 subblocks of equal length: A_0, A_1, \dots, A_{15} . They are processed by a step function. After processing they are concatenated giving H_i^* . The output $N_i^* = N_i \ll ls_b_4(N_i)$.

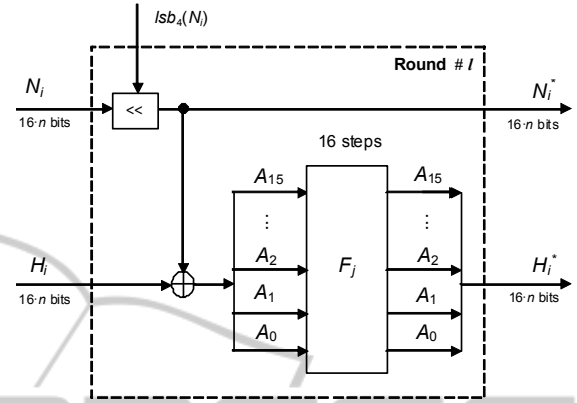


Figure 2.3: Round function.

2.2.5 Step Function

The essential part of the round is the step function F_j (Fig. 2.4). In each round the step function is executed 16 times, for $j=0, 1, \dots, 15$.

Let $GF[x]_n$ be a set of polynomials over $GF(2)$ of the degree smaller than n . If $w(x) \in GF[x]_n$ then $w(x) = w_{n-1}x^{n-1} \oplus w_{n-2}x^{n-2} \oplus \dots \oplus w_2x^2 \oplus w_1x \oplus w_0$ or

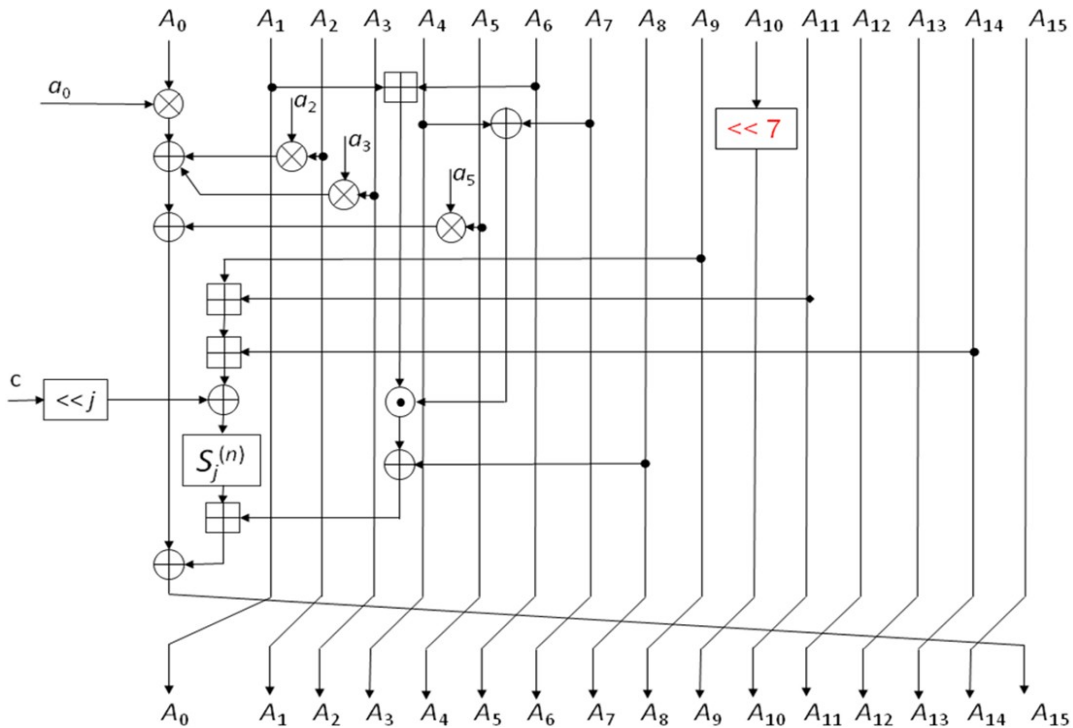


Figure 2.4: Step function F_j .

simply $w(x) = w_{n-1}w_{n-2}\dots w_2w_1w_0$, where $w_r \in GF(2)$ for $r \in \{0, 1, \dots, n-1\}$. Let $u(x), v(x), w(x) \in GF[x]_n$. We define two operations on polynomials, addition (\oplus) and multiplication (\otimes): $u(x) = v(x) \oplus w(x) \Leftrightarrow u_t = v_t \oplus w_t, t = 1, 2, \dots, n$, and $u(x) = v(x) \otimes w(x) = v(x) \cdot w(x) \bmod R(x)$, where $R(x)$ is a reduction polynomial of degree n . In the construction of the step function the multiplication of polynomials is performed four times: $a_0 \otimes A_0, a_2 \otimes A_2, a_3 \otimes A_3$, and $a_5 \otimes A_5$. The polynomials a_0, a_2, a_3 and a_5 , presented in hexadecimal form, are given in Table 2.1.

Table 2.1: Polynomials used in step function.

n	$R(x)$	Hexadecimal representation
16	$x^{16} \oplus x^{11} \oplus x^{10} \oplus x^5 \oplus 1$	10C21
32	$x^{32} \oplus x^7 \oplus x^6 \oplus x^2 \oplus 1$	1000000C5
64	$x^{64} \oplus x^4 \oplus x^3 \oplus x \oplus 1$	100000000000001B

The reduction polynomials must be irreducible; they are presented in Table 2.2.

Table 2.2: Reduction polynomials used in step function.

n	a_0	a_2	a_3	a_5
16	89CB	D949	0001	0001
32	AC2D B263	0000 0110	0000 0001	0000 0001
64	EDC0 28B9 A461 A403	0000 2500 0000 0001	0000 0000 0000 0001	0000 0000 0000 0001

After performing multiplications of polynomials a few additions modulo 2 (\oplus) and additions modulo 2^n (\boxplus) are done (Fig. 2.4). In each step the masking constant $c = 3236B539391FD066$ (in hexadecimal representation) is used. The particular value of c depends on n and j , and is indicated by a window of the length n sliding (cyclically, if necessary) from left to right on bits of c . For example, if $n = 16$ and $j = 0$ then $c = 3236$; if $n = 32$ and $j = 31$ then $c = 391FD066$; if $n = 64$ and $j = 5$ then $c = 6D6A72723FA0CD9$ (cyclic rotation of c to the left by 5 bits).

In each step a substitution $S_j^{(n)}$ depending (as the masking constant c) on n and j is used. It consists of four S-boxes S_0, S_1, S_2 and S_3 , each of dimension 16×16 , working in such a way that for $n = 16, S_j^{(16)} = S_{(j) \bmod 4}$; for $n = 32, S_j^{(32)} = S_{(j) \bmod 4} \parallel S_{(j+1) \bmod 4}$; and for $n = 64, S_j^{(64)} = S_{(j) \bmod 4} \parallel S_{(j+1) \bmod 4} \parallel S_{(j+2) \bmod 4} \parallel S_{(j+3) \bmod 4}$.

The multiplication modulo $2^n + 1$ of n -bit integers with the zero block corresponding to 2^n is denoted by \odot (Lai, 1991).

Table 2.3: Initial values of chaining variable.

n	$H_0 = h_0 \parallel h_1 \parallel h_2 \parallel \dots \parallel h_{15}$
16	34D906D3E3E5298EAC26F9FD2AC5AD23 DB84B0576C82CCA52517CF6B88B0A90C
32	34D906D3E3E5298EAC26F9FD2AC5AD23 DB84B0576C82CCA52517CF6B88B0A90C 0BC69C6F64D4B2664579E064AE220A5A 3DA7C5451DA429EF2AE8BF289D0F01E5
64	34D906D3E3E5298EAC26F9FD2AC5AD23 DB84B0576C82CCA52517CF6B88B0A90C 0BC69C6F64D4B2664579E064AE220A5A 3DA7C5451DA429EF2AE8BF289D0F01E5 8C6595B7B088D0C74BB82BF3CFDE5AA1 AB808B7E7425BC9EFA101925CBB0D528 3FA76FCBDF7B50D776DE280C8E2EE8B1 69D154F43B096994FDF52B5F148CC134

The initial values $H_0 = h_0 \parallel h_1 \parallel h_2 \parallel \dots \parallel h_{15}$ of chaining variable (depended on n) are given in Table 2.3 (H_0 for $n = 64$ is obtained as the hexadecimal form of consecutive 512 decimal places after the decimal point of π broken up into groups of 32). Before processing they must be assigned to $A_0 \parallel A_1 \parallel A_2 \parallel \dots \parallel A_{15}$ in such a way that $h_r = A_r, r = 0, 1, \dots, 15$.

2.3 Security Considerations

The round function composed of 16 steps can be represented in the equivalent form as a linear shift register (FSR) over $GF(2^n)$ generating maximum length sequences, additionally equipped with nonlinear feedback NL, and clocked 16 times (Fig. 2.5). The corresponding approach dealing with the use of feedback shift registers (over $GF(2)$) in the construction of hash functions has been presented in (Janicka-Lipska, 2004; Stokłosa, 1995).

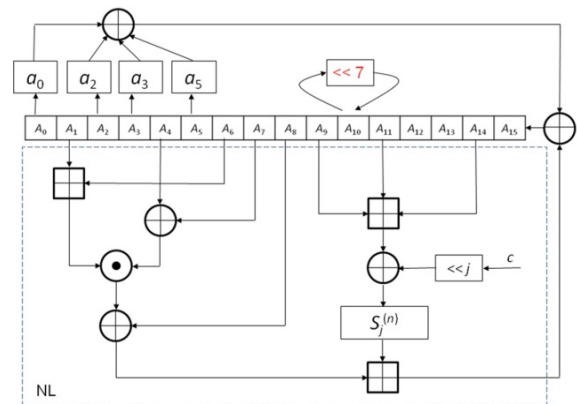


Figure 2.5: Equivalent form of round function.

Maximum 16-stages linear feedback shift register defined over $GF(2^n)$ generates the sequence of period length $T = 2^{16n} - 1$ ($n = 16$ or 32 or 64). This period length is considerably decreased by the nonlinear circuit (NL in Fig. 2.5). The processing of every consecutive block M_i of the formatted message modifies initial content of the register and consequently changes the period (meant as a sequence of states) of the FSR. The same effect can be observed when adding H_i to the result of processing the input by two rounds to obtain H_{i+1} (Fig. 2.2). This implies that collisions exist but finding them is difficult.

In order to achieve randomized hashing we use the construction (see Fig. 2.2) in which the random salt value s is added (mod 2) to each block M_i (Biham, 2006).

The function defined by the nonlinear circuit is a nonlinear $8n$ -argument function, $n = 16$ or 32 or 64 . For the function with such a number of arguments (128, 256 and 512, respectively) it is difficult, from the computational point of view, to perform the best affine approximation attack (Rueppel, 1986). Time needed for the attack is equal to time of the birthday attack, i.e. $O(2^{8n})$.

The sequence produced by the nonlinear circuit is immune to correlation attack (Rueppel, 1986).

3 S-BOXES

3.1 Involutorial S

Let F_2 be the Galois field $GF(2)$ and F_2^n be the n -dimensional vector space over F_2 . A substitution operation or an $n \times n$ S-box (or S-box of the size $n \times n$) is a mapping:

$$S : F_2^n \rightarrow F_2^n \tag{1}$$

where n is a fixed positive integer, $n \geq 2$. An n -argument Boolean function is a mapping:

$$f : F_2^n \rightarrow F_2 \tag{2}$$

An S-box S can be decomposed into the sequence $S = (f_1, f_2, \dots, f_n)$ of Boolean functions such that $S(x_1, x_2, \dots, x_n) = (f_1(x_1, x_2, \dots, x_n), f_2(x_1, x_2, \dots, x_n), \dots, f_n(x_1, x_2, \dots, x_n))$. We say that the functions f_1, f_2, \dots, f_n are component functions of S .

In case of HaF's S-box $n = 16$. HaF's S-box therefore is a function that takes 16 input bits and outputs also 16 bits – it is a 16×16 S-box. Additionally, it is generated in such a way that it is

its own inverse, i.e., $S^{-1} = S$.

HaF's S-box has been generated using the multiplicative inverse procedure similar to AES [Daemen 1999] with randomly chosen primitive polynomial defining the Galois field. Nonlinearity of this S-box is 32510 and its nonlinear degree is 15. Sixteen Boolean functions that constitute this S-box have nonlinearities equal to 32510 or 32512. The degree of each function is equal to 15.

The 16×16 S-box can be stored as a table of 65536 word values. Index for this table is an input of the S-box function, i.e., x_1, x_2, \dots, x_{16} . Values stored are S-box outputs (16 bits: $f_1(x_1, x_2, \dots, x_{16}), f_2(x_1, x_2, \dots, x_{16}), \dots, f_{16}(x_1, x_2, \dots, x_{16})$). To simplify the description of S-box generation let's consider a smaller S-box of size 8×8 . For presentation convenience such S-box can be displayed as a 2-dimensional table (Table 3.1). The input represented as a two digit hexadecimal number HL is divided – the low order digit (L) is on the horizontal axis and the high order digit (H) is on the vertical axis. For example, to see what is the S-box output at input 6F take 6 on the vertical axis and F on the horizontal axis. The S-box output is DA.

Table 3.1: Sample 8×8 S-box S .

L	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F	
H	0	9E	BC	C3	82	A2	7E	41	5A	51	36	3F	AC	E3	68	2D	2A
1	EB	9B	1B	35	DC	1E	56	A5	B2	74	34	12	D5	64	15	DD	
2	B6	4B	8E	FB	CE	E9	D9	A1	6E	DB	0F	2C	2B	0E	91	F1	
3	59	D7	3A	F4	1A	13	09	50	A9	63	32	F5	C9	CC	AD	0A	
4	5B	06	E6	F7	47	BF	BE	44	67	7B	B7	21	AF	53	93	FF	
5	37	08	AE	4D	C4	D1	16	A4	D6	30	07	40	8B	9D	BB	8C	
6	EF	81	A8	39	1D	D4	7A	48	0D	E2	CA	B0	C7	DE	28	DA	
7	97	D2	F2	84	19	B3	B9	87	A7	E4	66	49	95	99	05	A3	
8	EE	61	03	C2	73	F3	B8	77	E0	F8	9C	5C	5F	BA	22	FA	
9	F0	2E	FE	4E	98	7C	D3	70	94	7D	EA	11	8A	5D	00	EC	
A	D8	27	04	7F	57	17	E5	78	62	38	AB	AA	0B	3E	52	4C	
B	6B	CB	18	75	C0	FD	20	4A	86	76	8D	5E	01	ED	46	45	
C	B4	FC	83	02	54	D0	DF	6C	CD	3C	6A	B1	3D	C8	24	E8	
D	C5	55	71	96	65	1C	58	31	A0	26	6F	29	14	1F	6D	C6	
E	88	F9	69	0C	79	A6	42	F6	CF	25	9A	10	9F	BD	80	60	
F	90	2F	72	85	33	3B	E7	43	89	E1	8F	23	C1	B5	92	4F	

Cryptographically strong S-box should possess some properties that are universally agreed upon among researchers. Such S-box should be balanced, highly nonlinear, have lowest maximum value in its XOR profile (difference distribution table), have complex algebraic description (especially it should be of high degree). The above criteria are dictated by linear and differential cryptanalysis and algebraic attacks.

It is a well-known fact, that S-boxes generated using finite field inversion mapping fulfill these criteria to a very high extent. However, they are susceptible to (theoretical) algebraic attacks. To resist algebraic attacks multiplicative inverse mapping used to construct an S-box is composed

with an additional invertible affine transformation. This affine transformation does not affect the nonlinearity of the S-box, its XOR profile nor its algebraic degree. The best known example of such an S-box is the S-box of AES. It has been publicly known and it does not affect its security.

The algorithm used for generating the S-box for the purpose of HaF function presented in this paper uses similar method of generating S-boxes. Additionally it takes into account results of some recent studies (Fuller, 2002; Fuller, 2003) and incorporates changes in the S-box generating procedure to make it even more secure.

3.2 Generating Inverse Mapping

HaF S-box is based on so called inverse mapping $x \rightarrow x^{-1}$, where x^{-1} denotes the multiplicative inverse in a finite field $GF(2^n)$:

$$S(x) = \begin{cases} 0 & \text{for } x = 0 \\ x^{-1} & \text{for } x \neq 0 \end{cases} \quad (3)$$

As mentioned earlier, inversion mapping can be used to generate cryptographically strong S-boxes.

For any prime integer p and any integer n ($n = 1, 2, \dots$), there is a unique field with p^n elements, denoted $GF(p^n)$. In cryptography p almost always takes the value of 2. To generate an inverse mapping in $GF(2^n)$ we need an irreducible polynomial that defines a Galois field and another polynomial that would be a so called generator (see below). A polynomial is said to be irreducible if it cannot be factored into nontrivial polynomials over the same field. The n -bit elements of the Galois field are treated as polynomials with coefficients in F_2 . For example, in case of AES, where S-box is of size 8×8 we operate mostly on bytes represented as $b_7b_6b_5b_4b_3b_2b_1b_0$ which corresponds to the following polynomial:

$$b_7x^7 + b_6x^6 + b_5x^5 + b_4x^4 + b_3x^3 + b_2x^2 + b_1x + b_0 \quad (4)$$

where $b_i \in \{0, 1\}$.

An irreducible polynomial mentioned above is used to calculate a multiplication in $GF(2^n)$. When two polynomials are multiplied the resulting product is a polynomial of degree at most $2(n-1)$ – too much to fit into n -bit data word that represents polynomials in $GF(2^n)$, so the intermediate product of this multiplication is divided by the irreducible polynomial and the remainder of this division is the result of the multiplication. For $GF(2^n)$ an irreducible polynomial should be of degree n . For

example, in AES (with $GF(2^8)$) an irreducible polynomial selected for construction of the S-box is 11B (in hexadecimal notation).

A generator in Galois field is a polynomial whose successive powers take on every element except zero. Which polynomials are generators in a particular Galois field depends on the irreducible polynomial selected. So say polynomial 03 is a generator in $GF(2^8)$ with irreducible polynomial 11B (as in AES), but it is not a generator in $GF(2^8)$ with irreducible polynomial 1BD, for which the generator is for example 07.

For $n = 8$ the nonlinearity of this mapping treated as an S-box is 112. For $n = 16$ it is 32512. In general case, the nonlinearity of such a mapping is $2^{n-1} - 2^{n/2}$.

However, such an S-box would always have 0 and 1 as first two entries. This is because for $x = 0$, $x^{-1} = 0$ and for $x = 1$, $x^{-1} = 1$. These would be undesirable fixed points of an S-box. We remove them in the next step.

3.3 Affine Transformation

To avoid algebraic attacks (given multiplicative inversion's simple algebraic form) every element of the table of multiplicative inverses is changed using an affine transformation. Such transformation has to be a full permutation, so every element is changed and all possible elements are represented as the result of a change, so that no two different bytes are changed to the same byte. After applying this transformation the table is still a bijective mapping which is invertible and that is a prerequisite for most applications of S-boxes. In case of AES cipher this affine transformation is given by the following equation:

$$b'_i = b_i \oplus b_{(i+4) \bmod 8} \oplus b_{(i+5) \bmod 8} \oplus b_{(i+6) \bmod 8} \oplus b_{(i+7) \bmod 8} \oplus c_i \quad (5)$$

where c is an 8-bit constant (in case of AES it equals 63 in hexadecimal notation). i is the bit position. This transformation can also be represented as matrix multiplication:

$$\begin{bmatrix} b'_0 \\ b'_1 \\ b'_2 \\ b'_3 \\ b'_4 \\ b'_5 \\ b'_6 \\ b'_7 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \\ b_4 \\ b_5 \\ b_6 \\ b_7 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} \quad (6)$$

The algorithm used for generating S-box S of HaF function in this paper uses the same transformation, however adopted for 16×16 S-box size and with the constant part of this transformation (namely c_i) taken at random so that resulting S-box does not have fixed points (such that $S(x) = x$). Particularly the two fixed points mentioned in the previous paragraph (0 and 1) are removed by this transformation.

3.4 Removing Cycles

One of the requirements for HaF S-box is the absence of cycles. Cycle is such a sequence of S-box values S_0, S_1, \dots, S_{k-1} where $S_{(i+1) \bmod k} = S(S_i)$. HaF S-box should have only one such cycle containing all the values of the S-box (a cycle for which $k = 2^n$).

The affine transformation described in previous paragraph changes number of cycles in an S-box, without changing its nonlinear properties. Note that fixed points are also short cycles where $k = 1$.

Cycles are removed in a procedure with two steps. First step is actually the aforementioned affine transformation. It is applied repeatedly with a random value of c until the S-box with only 2 cycles is found. This might not always be possible. In such a case a new S-box has to be generated with another randomly chosen primitive polynomial using the inverse mapping as described earlier.

When 2-cycle S-box is found we move on to the next step, which is performed together with removing the affine equivalence.

3.5 Removing Affine Equivalence

According to (Fuller, 2002; Fuller, 2003), S-boxes based on multiplicative inverse in a finite field have such a peculiar property that all component functions of the S-box are from the same affine equivalence class (all the output functions of the S-box can be mapped onto one another using affine transformations). HaF's S-box has been processed to remove this linear redundancy, so that all Boolean functions are now from different affine equivalence classes, while still maintaining exceptionally high nonlinearity of the inverse mapping. The proposed S-box has the maximum XOR difference distribution table value of 6, which is extremely good.

Removing this linear redundancy in 2-cycle S-box is carried out in such a way that it will at the same time reduce the number of cycles to only 1. It is done by choosing randomly two S-box entries x and y , each belonging to another cycle, and

rearranging S-box entries in such a way, that both cycles are joined into one.

After such change a test for linear redundancy is performed. If affine equivalence is still present (between any component functions) the change is reversed and different S-box entries are randomly selected and tested – this procedure is carried out until S-box without linear redundancy is found. If such an S-box cannot be found, we need to generate another S-box with inverse mapping.

Many properties of Boolean functions covered by various cryptographic criteria (such as algebraic degree and nonlinearity) remain unchanged by affine transformations. Absolute values of Walsh transform as well as autocorrelation function are only rearranged by affine transformations. The frequency distribution of the absolute values in these transforms is invariant under such affine transformations. To prove that two functions are from different equivalence classes it is therefore sufficient to show that their respective Walsh transform or autocorrelation function frequency distribution is different.

4 REFERENCE IMPLEMENTATIONS OF HaF-256

HaF-256 algorithm was implemented using of C++ language and Microsoft Visual Studio 2008 environment. Two reference implementations were separately developed and tested using of reference data. The results produced by the implementations were compared with each other in order to verify algorithm implementation accuracy.

To evaluate performance a 20 MB text file was processed and the time was measured. Several options were considered. For Windows (64-bit Windows 7) two compilers were used: native Visual Studio C++ compiler and Intel C++ compiler. The code was generated for 32-bit and 64-bit platforms.

Table 4.1: Results of performance measurements.

System	Platform	Compiler	Performance [MB/s]
Windows 7	32-bit	VS2008	1.29
Windows 7	64-bit	VS2008	1.60
Windows 7	32-bit	Intel	2.99
Windows 7	64-bit	Intel	3.13
Linux	32-bit	GCC	0.74
Linux	32-bit	GCC -O	1.17
Linux	32-bit	GCC -O2	1.36
Linux	32-bit	GCC -O3	2.33

Linux (Fedora 9) GCC compiler was used without and with optimization. The code was generated for 32-bit platform only. PC machine with 2.2 GHz Athlon-64 processor was used as a testing platform. The results are presented in Table 4.1.

As shown in Table 4.1, the best result was obtained using Intel compiler. For 64-bit platform the performance was about 4.7% better than for 32-bit platform. Bigger improvement may be expected for HaF-1024 implemented using 64-bit variables. For the sake of comparison we measured performance of one of the NIST SHA 3 competition finalists – BLAKE hash function [Aumasson, 2011], using the same computer. BLAKE algorithm is very simple and does not use S-boxes. Results are presented in Table 4.2. As we can see, BLAKE significantly outperforms HaF. But in some applications it does not matter. For example, it takes 0.03 s to compute hash for a 100 kB message using HaF-256, whereas 0.0005 s is required for BLAKE-256.

Table 4.2: BLAKE-256 performance.

Compiler	32-bit version	64-bit version
VS2008	175 MB/sec	256 MB/s
Intel C++ Compiler	204 MB/sec	240 MB/s

5 CONCLUDING REMARKS

Most cryptographic hash functions designers focus on high processing speed. Therefore relatively simple algorithms are preferred. Implementations of these algorithms may be vulnerable to fault attack and side channel attack.

In HaF hash functions family processing scheme is more elaborated and we use relatively big 16×16 S-boxes. It leads to more complex implementation.

We expect it to give greater robustness against fault attack and side channel attack.

We currently experiment with fault attacks on HaF implementation, so it should be possible to verify what are the advantages of this approach.

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