

PREDICTION MODEL OF INPATIENT MORTALITY FOR PATIENTS WITH MYOCARDIAL INFARCTION

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Abstract: We propose and investigate a prediction model of inpatient mortality for patients with myocardial infarction. The model is based on complex clinical data from a hospital information system used in the Czech Republic. The prediction of the outcome is an important risk-adjustment factor for objective measurement of the quality of healthcare; thus it is a very important factor in healthcare quality assessment. For our experiments we studied hospital mortality in acute myocardial infarction, because: (1) this indicator is reliably detectable from available data; (2) treatment of acute myocardial infarction has a significant socio-economic impact; and (3) the prediction of mortality based on admission findings is the subject of many research papers and thus, we have a good benchmark for our experimental results. We considered only variables that convey information about the patient at the time of admission. We selected 21 out of 637 variables and used them as predictors in logistic regression to form a prediction model for hospital mortality. The achieved prediction accuracy was 85% and the size of the area under the ROC curve was 0.802. The results are based on a relatively small data sample of 486 patient records. Our future work will aim at increasing the accuracy by using a larger data set.

1 INTRODUCTION

The results of medical treatment depend not only on appropriate selection and proper execution of the treatment, but also on initial individual conditions of the patient. Evaluation of the patient's initial conditions is applicable in two major tasks: (1) in estimating the prognosis of the patient in order to select the most efficient treatment, e.g., the selection of an adequate mix of interventions and medications, or to decide on timely referral to the facility with higher or (less commonly) lower specialization, i.e., for risk stratification, (2) for the retrospective statistical evaluation of the care using standardized quality indicators, i.e., for the risk adjustment task.

Conceptually, these two processes must be mutually consistent. Risk adjustment of the outcome quality indicators is essentially based on the stratification of the risks and on empirical knowledge and scientific evidence of the influence which each patient's individual risk factors have on the result of care in the group of patients.

In practice, there are significant differences in

performing risk stratification and risk adjustment (standardization). Risk stratification is done in real time by physicians and it is based on all available information while standardization of the risks is done retrospectively, mostly by medical or regulatory authorities. During risk stratification of a particular patient, all relevant information is available or can be relatively easily obtained from the clinical documentation or from additional medical investigation. Retrospective evaluation of the quality of outcomes is subject to many restrictions: e.g., missing values of the variables cannot be completed; evaluation is mostly done outside of the healthcare facility and is based on limited sets of available data which have not necessarily been designed for the purpose of quality measurement. These data sets are in general denoted as "administrative" and the models based on them are generally called "administrative" models.

Administrative data, i.e., demographic data, diagnoses, procedure codes, and coded results of hospitalization case outcomes are part of an inpatient service reimbursement form which is utilized for all inpatient cases reimbursed from the mandatory

healthcare insurance scheme in the Czech Republic.

Differentiation of positive or negative results as they relate to quality of service is crucial for efficient allocation of funds; as such it is (or should be) of primary interest to the insurance companies.

In order to create and validate an administrative prediction model, a clinical model, i.e., risk-adjusted clinical model, should be built first as a “gold standard”.

For our experiments with risk-adjusted clinical models we chose hospital mortality in acute myocardial infarction, because: (1) this indicator is reliably detectable from available data; (2) treatment of acute myocardial infarction has a significant socio-economic impact; (3) prediction of mortality based on admission findings is the subject of many research papers, thus we have a good benchmark for our experimental results; and (4) no outcome-prediction models are currently used in the Czech Republic; thus they are a necessary novelty in quality measurement.

Our work has been motivated by the work published at the Yale University (Krumholz, H. M., et al, 2007).

2 METHODS

2.1 Risk Adjustment

Risk adjustment is a statistical process used to identify and adjust for variations in patient outcomes that stem from differences in patient characteristics (or risk factors) across healthcare organizations in order to achieve better comparison of patient outcomes between different organizations and to improve the interpretability of results. The quality of healthcare can be measured by several types of indicators: by mortality, by re-hospitalization rate or by complication rate. In this part, we will show reasons and principles of risk adjustment of a mortality indicator. Standardization of other types of indicators follows the same principles.

A straightforward comparison of mortality rate of two different healthcare facilities will not give objective results as it also depends on the presence of risk factors at the time of health care encounters. Patients may experience different outcomes regardless of the quality of care provided by the healthcare organization, so comparing patient outcomes across healthcare organizations without an appropriate risk adjustment could be misleading. By adjusting for the risks associated with outcomes of interest, risk adjustment facilitates a fairer and more

accurate inter-organizational comparison. (CMS, 2005).

There are two essential methods: (1) case stratification, i.e., decomposition of cases into more homogeneous sub-groups based, for example, on age and/or sex grouping, or (2) standardization of results (indicators), i.e., risk-adjustment. The first method, however, is disadvantageous both in terms of statistics (subgroups will often have small numbers of patients) and in terms of subsequent interpretation (different subgroups may have different comparative results and it may not be clear how the provider should actually be evaluated with respect to the overall quality in the clinical area).

2.2 Selection of Risk Factors

The requirements for the selection of risk factors applicable in the standardization process indicators are as follows: (i) there must be a statistically significant relationship between risk factor and the outcome indicator. For example, if the probability of death from myocardial infarction is related to the value of blood pressure at the time of admission, then it is included as a risk factor. The prediction model should also reflect situations in which certain combinations of factors have greater impact than each of the individual factors alone; (ii) the composition of patients, in terms of risk factors, must be different in different healthcare facilities. Otherwise, there is no need to carry out standardization, although there is a strong correlation between the indicator and risk factor – all healthcare facilities are “disadvantaged” in the same way. In practice, this requirement is usually met, as healthcare facilities usually have different distributions of risk factors among their patients; (iii) each risk factor must clearly reflect the condition of the patient upon admission to a healthcare facility and may not be the result of the treatment process itself; (iv) each risk factor has to be reliably documented within the available data – unfortunately, this is a very limiting restriction in many cases, and especially in administrative data.

It is obvious that the correction of the measurement bias is never perfect. Even after standardization, residual bias remains. Residual distortion can, for example, be caused by risk factors that are not yet known or that are not reflected in the data.

2.3 Standardization of Indicators

When standardizing the quality indicators it is first

necessary to find and express the relationship between the indicator and each risk factor. Suppose that the risk factor is age and the outcome indicator is the hospital mortality of acute myocardial infarction. Based on data from the entire set of healthcare facilities (standard population) it is therefore necessary to express, with the help of statistical methods, the relationship between the patient's age and the likelihood of death from heart attack. Then, for each hospital the correlation index (CI) is calculated. CI is defined as the proportion of two variables: the actual number of deaths and the predicted (expected) deaths: $CI = \frac{\text{actual number of deaths}}{\text{predicted (expected) number of deaths}}$.

The expected number of deaths in a hospital is the sum of individual probabilities of death of all patients admitted to the hospital, determined with respect to their risk factors. The expected number of deaths is the number of deaths that would be expected if the hospital held the same mortality risk as the population of all hospitals. If the actual number of deaths differs from the expected number, we can conclude there are internal factors that have an influence on the number of deaths in this particular hospital. The correlation index is a dimensionless number that indicates the relative position of the hospital compared with the average: an index value greater than one indicates above average mortality, while an index value less than one indicates the contrary, i.e., below average mortality. Standardized mortality rate is obtained by multiplying the index value by general mortality, i.e., the average mortality for all hospitals: $\text{standardized mortality} = \text{general mortality} * CI$.

The result of standardization of the indicator is the value of the indicator on the condition that the hospital had the same distribution of risk factors as the entire group of providers.

2.4 Patient Sample

Our initial study is comprised of cases from one Czech hospital. After exclusion of patients transferred for treatment elsewhere, we selected all patients admitted to the hospital with the main diagnosis of acute myocardial infarction (ICD-10 codes in the range of I210 - I214). Our resulting data set consisted of 486 patients (both male and female, without age restrictions). The data set includes the usual demographic and administrative data including outcome status, principle and secondary diagnoses coded using ICD-10, list of procedures coded using the Czech national list of medical procedures, and laboratory results. In addition, we had complete

information about previous hospitalizations in the same hospital during the 12 months prior to the respective hospitalization. In total we considered 637 variables (possible risk factors). Only 151 patient records included all values of the potential risk factors. Patient records with missing values were not excluded; instead, to keep maximum usable information, we used a method of imputation of missing data values (Rubin, D. B., 1987).

2.5 Statistical Analysis

The first and most difficult step in the standardization of a selected indicator is to identify relevant risk factors and formally characterize their influence on the selected indicator. Often (see, e.g., Krumholz et al, 2007) the relationship between the risk factors and the selected indicator is expressed using logistic regression.

Let $P(Y = 1|X=x)$ denotes the probability that the variable Y reaches the value 1 given the value x of the vector of risk factors X . In our case it is the probability that the patient will die within 30 days after admission to the hospital.

The logistic regression model defines the relationship between the dependent variable Y and a vector of the risk factors X having values of vector x . The relationship is defined by the logistic function

$$P(Y = 1|X = x) = \frac{\exp(\beta'x)}{1 + \exp(\beta'x)}, \quad (1)$$

where β is the vector of parameters to be found and β' denotes its transposition. Vector x is usually of the form $(1, z)$ and the first component of vector β , referred to as β_0 , is the absolute member (intercept).

First, we selected candidates for the risk factors based on the information gain method. Information gain of each risk factor X and the dependent variable Y is defined as

$$I(Y, X) = H(X) + H(Y) - H(X, Y), \quad (2)$$

where $H(X)$ is the entropy of variable X defined as

$$H(X) = - \sum_x P(X = x) \log P(X = x) \quad (3)$$

and $H(X, Y)$ is the mutual entropy of variables X and Y defined similarly as

$$H(X, Y) = - \sum_{x,y} P(X = x, Y = y) \log P(X = x, Y = y). \quad (4)$$

Log is the binary logarithm. The higher the information gain, the more information variable X

brings about the value of variable Y . Absolute values of laboratory tests have been used, not relative values against the standard range for age and sex of the patient. Values of continuous variables were divided into ten bins for the purpose of information gain calculations. For further processing, we ranked only variables whose information gain was greater than 0.01. The finally selected variables are given in Table 1.

Table 1: Variables with an information gain greater than 0.01.

| Code | Description | Information gain |
|---------|---|------------------|
| Urea | Serum urea | 0.11674202 |
| Crea | Serum creatinine | 0.09532763 |
| Leuco | Leukocytes in full blood | 0.06820710 |
| I48 | Atrial fibrillation and flutter | 0.02425088 |
| O.E78 | Disorders of lipoprotein metabolism and other lipidaemias | 0.02318073 |
| O.I20 | Angina pectoris | 0.02044021 |
| O.I48 | Atrial fibrillation and flutter | 0.01997538 |
| I73 | Other peripheral vascular diseases | 0.01971532 |
| O.I27 | Other pulmonary heart diseases | 0.01971532 |
| O.I73 | Other peripheral vascular diseases | 0.01971532 |
| Age | Patient's age | 0.01926587 |
| O.I46 | Cardiac arrest | 0.01851840 |
| K92 | Other diseases of digestive system | 0.01758336 |
| O.I21.0 | Acute transmural myocardial infarction of anterior wall | 0.01651995 |
| I74 | Arterial embolism and thrombosis | 0.01576957 |
| I42 | Cardiomyopathy | 0.01474711 |
| O.I42 | Cardiomyopathy | 0.01474711 |
| O.I10 | Essential (primary) hypertension | 0.01471863 |
| O.I21.1 | Acute transmural myocardial infarction of inferior wall | 0.01440448 |
| O.I64 | Stroke, not specified as haemorrhage or infarction | 0.01358037 |
| I27 | Other pulmonary heart diseases | 0.01349612 |
| K29 | Gastritis and duodenitis | 0.01338366 |
| K62 | Other diseases of anus and rectum | 0.01290232 |
| L95 | Vasculitis limited to skin, not elsewhere classified | 0.01290232 |
| K57 | Diverticular disease of intestine | 0.01217010 |
| I50 | Heart failure | 0.01158408 |
| O.I21.4 | Acute subendocardial myocardial infarction | 0.01140944 |
| K80 | Cholelithiasis | 0.01054740 |

Variables prefixed with "O" indicate diagnoses that the patient encountered during the examined hospitalization. Other diagnoses (without the "O"

prefix) were taken from the patient's hospitalizations within one year prior to the hospitalization studied.

Variables in Table 1 were then used for training the logistic regression model. For this purpose the values of all the considered variables were normalized to the interval $\langle 0, 1 \rangle$. Some patients did not have all selected variables examined. One option for such patients was their exclusion from the data set. This would, however, significantly reduce the available data. Therefore, we chose Multivariate Imputations by Chained Equations (cf. Rubin, D. B., 1987 or Buuren, S., at al, 2006) to substitute the missing values. Alternatively, we also tested the replacement of missing risk factor values by the average value of this factor, but in this case the results proved to be less accurate. We also excluded variables that were causing singularities: O.I73, O.I42 and L95, and also those that might yield misleading information due to co-morbidities: O.I20, O.I48, O.I46 and O. I64.

For the actual learning of the model parameters of logistic regression we have used the *glm* module, which is part of the statistical system R (R Development Core Team, 2010).

3 RESULTS

The resulting model is described in Table 2. The first column includes the names of the risk factors as in Table 1.

In the second column there are individual coefficients β , i.e., the components of vector β of the logistic regression formula. Standard deviations of the coefficient are in the third column, and the fourth column contains the corresponding values of t Student's t-test -- i.e., whether coefficient β has the given mean value. The fifth column shows the number of degrees of freedom of the Student's t-distribution calculated in accordance with (Barnard and Rubin, 1999). The last column gives the probability of alternative hypotheses of the t-test presented. Values lower than 0.05, which corresponds to the static level of significance of 5%, are shown in bold. These values indicate that the hypothesis that coefficient β has the given value as its mean value is accepted at a static level of significance of 5%.

The values of coefficients β thus can be roughly interpreted as follows: the greater a positive number, the greater the influence of the corresponding risk factor on the probability of death. The lower a negative number, the greater the influence of the corresponding risk factor on the probability of

Table 2: Parameters of the logistic regression model.

| Code | β | SD | t value | degrees of freedom | Alt. hyp. |
|--------------|-------------|--------------|--------------|--------------------|-------------|
| (Intercept) | -2.1060975 | 1.2651842 | -1.664656859 | 31.598080 | 0.105868127 |
| Urea | 8.6381220 | 3.2418691 | 2.664549922 | 6.539030 | 0.034363798 |
| Crea | -1.0298399 | 3.1864171 | -0.323196842 | 6.948143 | 0.756055460 |
| Leuco | 1.3401639 | 2.5917890 | 0.517080649 | 6.072126 | 0.623388122 |
| I48 | 1.1774437 | 0.5043932 | 2.334376623 | 62.932775 | 0.022781215 |
| O.E78 | -1.1969985 | 0.4437995 | -2.697160631 | 456.217585 | 0.007252314 |
| I73 | 24.2072289 | 3127.7478688 | 0.007739508 | 463.999987 | 0.993828154 |
| O.I27 | 22.4904111 | 3055.1132840 | 0.007361564 | 463.999942 | 0.994129539 |
| Age | -0.8665293 | 1.2988153 | -0.667169004 | 46.748401 | 0.507944173 |
| K92 | 0.1754608 | 2.1248919 | 0.082573969 | 260.797168 | 0.934253641 |
| O.I21.0 | 2.0831447 | 1.2175409 | 1.710944339 | 14.713859 | 0.108083943 |
| I74 | 0.8435731 | 1.2306952 | 0.685444349 | 363.623078 | 0.493500307 |
| I42 | 18.6880782 | 3580.0597075 | 0.005220047 | 463.999856 | 0.995837268 |
| O.I10 | -1.7197621 | 0.5011027 | -3.431955378 | 32.644378 | 0.001645515 |
| O.I21.1 | -18.4366694 | 1142.1321492 | -0.016142326 | 463.999889 | 0.987127785 |
| I27 | -0.3723272 | 2.1099515 | -0.176462425 | 220.553439 | 0.860092594 |
| K29 | -0.6493484 | 1.1797607 | -0.550406839 | 49.675659 | 0.584507085 |
| K62 | 1.6111716 | 3.1727303 | 0.507818643 | 83.887081 | 0.612913195 |
| K57 | 1.5036105 | 1.8285737 | 0.822285931 | 17.330469 | 0.422084093 |
| I50 | -0.2095659 | 0.5698730 | -0.367741513 | 18.221241 | 0.717302894 |
| O.I21.4 | -0.2596627 | 1.1148068 | -0.232921682 | 9.406510 | 0.820811800 |
| K80 | 1.4525334 | 0.5681741 | 2.556493236 | 388.428873 | 0.010952816 |

survival. The number in the last column tells us to what extent this effect is statistically significant. For values greater than 0.05 (which is true for most of our risk factors), we can say that the impact on the probability of death was not statistically proven in our data set. However, it is necessary to remark that these results are affected by the small number of patients in our data set.

3.1 Evaluation of Results of the Logistic Model

For a reliable evaluation of the quality of the trained prediction model, independent data that were not used to learn the model are needed. For this purpose we used the method of K-fold cross-validation, where K had a value of ten. We randomly divided the data set into ten groups of approximately equal size. The remaining nine groups were used to train the model which was then validated on the selected group. This procedure was repeated for each of the ten groups. The results presented below summarize all partial results.

The basis for evaluation is the confusion matrix, which includes numbers of true positive (tp) and false positive (fp) predictions that the patient will die and true negative (tn) and false negative (fn) predictions that the patient will not die.

The results of our model were as follows: $tp = 28$, $tn = 383$, $fp = 9$, $fn = 66$. Based on these values we can express the results of model evaluation:

$$accuracy = 0.85, precision = 0.76, recall = 0.30, \text{ and } false\ alarm\ rate = 0.02.$$

The output of the logistic regression model is not only an estimate of whether or not the patient dies within 30 days, but it gives the probability with which this event occurs. Also, it is possible to change the decision threshold (which is normally set to 0.5) of the classification. This enables us, for example, to increase recall at the expense of precision and vice versa. The overall behavior of such a classifier is best characterized by the ROC curve, see Figure 1.

The ROC curve shows the dependence of *recall* and *false alarm rate* on the value of the threshold (threshold values are shown below the curve in Figure 1). The higher the curve is located, the better results the model gives. A good measure of classifier's performance is the size of the area under the curve, i.e., the ROC area. The maximum value that represents the ideal classifier is 1.0. On the contrary, a value of 0.5 can be reached by a random classifier. The value of the ROC area of our model was 0.802.

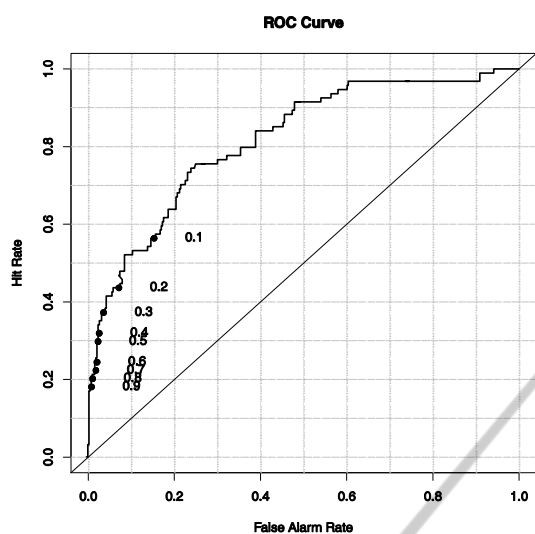


Figure 1: ROC curve of the classifier.

4 CONCLUSIONS

In this work we studied the standardization of outcome indicator “hospital mortality in acute myocardial infarction.” Although we had a relatively small data sample and we used only the main and secondary diagnoses and the results of three laboratory tests to build a predictive model, we succeeded in predicting the 30-day mortality of patients relatively successfully. The achieved accuracy was 85% and the size of the area under the ROC curve was 0.802. With regard to the statistical properties of predictive models of this type, it can be expected that a better prediction could be achieved by using other data from an electronic patient record, such as ECG, localization of pain and blood pressure (these data are stored only in free text format and would involve difficult pre-processing to enable us to use them in the classifier construction; this was beyond the scope of this paper). For practical use of our result in the standardization of mortality indicators, it will be necessary to train the model using a larger data set from many hospitals. Then it will also be possible to make a better medical interpretation of the achieved results.

Another challenge, which we intend to address in the future, is researching the effect of a combination of several risk factors and the use of ratings of laboratory test results performed with respect to the normal ranges for a particular sex and age combination, rather than with respect to their nominal values only.

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