

A COMPARATIVE STUDY OF IMPLEMENTED COLLISION DETECTION STRATEGIES

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Keywords: Collision Detection, Spatial Decomposition, Bounding Hierarchy, Strategies Comparative.

Abstract: Many computer interactive environments require to calculate collision detections between geometrical models, usually triangle meshes. In this paper, a comparative study of some collision detection strategies is realized. For this purpose, the compared algorithms have been implemented. Some of these algorithms also allow realizing other procedures, such as calculating distances or overlapping triangles. Hence, the main features of each algorithm have been explained. The compared strategies have been tested considering, in addition to the runtime, the pre-processing time and the memory usage. Finally, the results have been compared in order to extract the benefits and constraints of each strategy, and proposing some possible applications for each strategy.

1 INTRODUCTION

Interactive environments require methods that allow performing collision detection tests between geometrical models, usually triangle meshes (Lin and Gottschalk, 1998; Bergen, 2003). Since interaction must be in real time, it is necessary to utilize methods that resolve the collision detection quickly. In addition, the methods must be robust so that the interactive environment remains consistent.

Once the collision is detected, the interactive environment must give a response (Geiger, 2000). For that, it is important not only to detect the collision, but also to calculate a detailed collision. This involves calculating some collision parameters, such as overlapping triangles, distances, and nearest points. These calculations must be also calculated quickly in order to keep a real time interaction.

In the literature, there are several approaches that allow performing some of that calculations. Each approach has their advantages and disadvantages, hence the use of one method depends on each situation. In the present paper, we describe strategies to calculate a detailed collision between two triangle meshes. These strategies are implemented in order to test and compare them. These tests allow extracting the main benefits and constraints of each strategy.

The following section deals with the proposed strategies. Then, we will explain the implementations and make a comparison between the different strategi-

es. Later, a possible GPU implementation of the proposed strategies is studied. Finally, the benefits and constraints of each strategy are shown and some applications or each approach are suggested.

2 PROPOSED STRATEGIES

In order to perform a collision detection, we have proved different strategies and determined their positive and negative points. On the one hand, we pretend to calculate the collision detection. On the other hand, we want to identify other features that allow us to implement a correct response to a collision.

2.1 Spatial Decompositions

Hierarchical space decompositions allow increasing the efficiency of the collision detection. This is because spatial decompositions permit to reduce the space where the collision detection is performed. In order to check a collision, the two spatial decompositions are compared recursively. Each recursive step tests whether two nodes A and B, one from each hierarchy, collide. If A and B do not collide, the collision test ends. Otherwise, the collision test is performed recursively to their children. If A or B are both leaf nodes, the collision detection test is performed to the triangles that are inside the leaf nodes. When down

the hierarchy, some different strategies can be chosen. For example, if A and B do not collide, we can test A with each of the children of B, B with each of the children of A, or each of the children of A with each of the children of B. This choice modifies the efficiency of the method and depends on each case.

In order to perform the triangle-triangle collision test, we have used the point in solid algorithm by Feito (Feito and Torres, 1997). This method allows performing a point in solid test without any complex calculation, such as solving a system of equations. In addition, this method is robust because it can work with non-manifold polyhedra.

The octree (Chen and Huang, 1988) is one of the most used hierarchical data structures. This structure starts from a cuboid that contains all the triangles, usually a bounding box. In general, the root box is homogeneously divided into eight new boxes. The subdivision stops when a prefixed level is reached or a box contains less triangles than a threshold. There are variations in the octree that can improve its performance. One of the most used proposes a change in the subdivision method of the boxes. Instead of dividing homogeneously each box, the dividing point is selected so that it increases the efficiency.

The tetra-tree (Jiménez et al., 2006) is a hierarchical data structure that divides the entire space into eight equal parts named tetra-cones. In the following levels of the hierarchy, each tetra-cone is homogeneously divided into four new tetra-cones. Due to the adjustment obtained by bounding tetrahedra associated with each tetra-cone (Jiménez and Segura, 2008), the tetra-tree fits the mesh better than other approaches, such as the octree. In addition, the tetra-tree allows classifying triangles quickly and robustly because it is based on barycentric coordinates. In the same way as the octree, the subdivision stops when a prefixed level is reached or a tetra-cone contains less triangles than a threshold.

2.2 Convex Hull

Convex objects enable the application of specific algorithms in order to detect a collision. In general, these algorithms are more efficient because they take advantage of the convex object features. We considered to build the convex hull of the objects in order to apply specific algorithms, such as the GJK algorithm (Gilbert et al., 1987) or some of its variants (Cameron, 1997). The quick hull method was chosen to build the convex hull. Nevertheless, the main disadvantage is that the convex hulls do not fit the mesh properly in most cases, hence the obtained results are not exact.

2.3 Bounding Volume Hierarchies

As an alternative to spatial decompositions and convex hulls, we propose to use bounding volume hierarchies (Gottschalk et al., 1996; Klosowski et al., 1998). Unlike the spatial decompositions, bounding volumes do not fill all the space and their nodes can overlap between them.

In (Larsen et al., 1999), swept sphere hierarchies are used to perform collision detections, identify overlapping triangles, determine nearest points, and calculate distances. They used three different types of swept volumes: a sphere, a cylinder with hemispherical caps, and a rounded box. These volumes depend on the swept primitive used: a point, a segment, and a rectangle. The algorithm efficiency depends on the volume used. The sphere allows building the data structure quickly, but the rounded box fits the mesh better.

This algorithm utilizes a bounding volume traversal tree (BVTT) in order to perform a query. Each node of the BVTT represents a single collision test between two bounding volumes. Hence, the BVTT is traversed to perform a collision detection. In order to improve query performance, this method uses a priority directed search when the BVTT is being traversed. Moreover, temporal coherence is also taken into account. This method is implemented in the PQP library.

In (Ehmann and Lin, 2001), they present an approach to detect collisions and calculate distances based on convex surface decomposition. Moreover, this method has three main steps. First, the model is decomposed into convex parts. In order to achieve that, a method based on graph search is used. Second, a bounding volume hierarchy is constructed based on the previous decomposition. They proposed a top-down approach in which each node of the hierarchy bounds all the geometry in its child nodes. For that reason, the primitives are divided recursively in order to obtain new convex patches.

Once the hierarchy is constructed, queries can be executed. In order to perform queries between pairs of convex polyhedra, the method uses a distance minimization algorithm based on Voronoi marching (Ehmann and Lin, 2000). Queries are accelerated using spatial and temporal coherence. This method requires 2-manifold meshes and their triangles must be sorted counter-clockwise. This algorithm is implemented in the SWIFT++ library.

Table 1: Features implemented by each method. Tetra-tree and Octree utilize the Feito- Torres algorithm.

	Feito	GJK	PQP	SWIFT++
Collision	X	X	X	X
Overlapping triangles	X		X	
Distance		X	X	X
Tolerance			X	X
Contact features				X

Table 2: Pre-processing time (s) and size (MB) of the spatial decompositions.

	Vertices	Triangles	Tetra-tree		Octree	
			Pre-processing	Size	Pre-processing	Size
Horse	3582	7172	0,427	0,0351	0,496	0,0399
Skull	20002	40000	2,49	0,2608	4,329	0,261
Bunny	35947	69451	4,544	0,4211	8,744	0,3254
Armadillo	172974	345944	28,184	2,0322	44,579	1,6549
Dragon	437645	869928	70,25	4,8031	104,68	2,1975
Buddha	543652	1085634	84,704	5,5607	138,542	4,8717

3 IMPLEMENTATION AND RESULTS

In order to check their performance, the described strategies have been implemented under the same conditions. In order to developed this, we have used the same programming language (C++) and the same compiler (gcc). The implemented data structures are the octree and the tetra-tree. The Feito’s algorithm has been used to check the intersection between triangles. In addition, qhull, PQP, and SWIFT++ libraries have been used.

Spatial decompositions, as well as the Feito and Torres algorithm have been implemented without the use of any library. Moreover, we have not used any optimization, nor have considered spatial or temporal coherence. That means that the implementation is less optimized than other approaches which are based on a library. Hence, the obtained results should not be as good as the implemented libraries. In order to implement the convex hull, the qhull library has been utilized. This library implements the quickhull algorithm and is one of the most used libraries. Nevertheless, the collision detection based on the qhull implementation has not been tested because the results obtained are not as accurate as the rest of approaches, hence the obtained results should not be compared with them. The PQP library, that is written in C++, can work with any model composed of triangles. Hence, it is not necessary that the mesh is closed or 2-manifold. This library allows detecting collisions and overlapping triangles, calculating dis-

tances and nearest points, and determining if two models are closer than a given threshold. The SWIFT++ library is implemented in C++ and is divided into two parts. The main part allow performing intersection, calculating exact and approximate distances, and resolving contact determination queries between two or more objects. These objects must be convex and closed. However, the other part of the library enables the conversion of non-convex and opened models into convex hierarchies that can be processed by the main part of the library. This library can not work with non-2-manifold models or that contain counter clockwise triangles. The features of the algorithms are summarized in table 1.

3.1 Results

We have performed some tests to measure the efficiency of the proposed strategies. These tests were done with six models with a polygonal complexity in the range from 7172 to 1085634 triangles (table 2). Some of the models used (figure 1) have holes and are not-2-manifold, therefore we can test the robustness of each strategy. The measured parameters have been the pre-processing time, the size of the data structures, and the time to determine the collision detection and to calculate the overlapping triangles. These tests were performed on a 2,8 GHz Intel i7 PC with 4 GB of RAM.

Firstly, we have developed some tests to measure the spatial decomposition performance. Both data structures have been built under the same conditions:

Table 3: Pre-processing time (s) and size (MB) of the proposed strategies.

Models	Convex Hull		PQP		SWIFT++	
	Pre-processing	Size	Pre-processing	Size	Pre-processing	Size
Horse	0,202	0,0252	0,045	2,8726	0,599	2,9544
Skull	3,8	0,6182	0,265	16,0216	8,094	20,6092
Bunny	4,3	0,2916	0,47	27,818	8,148	31,6224
Armadillo	15,7	0,3662	2,552	138,5654	380,121	162,3651
Dragon	42,5	0,4613	6,678	348,9311	Not 2-manifold	Not 2-manifold
Buddha	130,4	1,1556	8,327	435,5262	Not 2-manifold	Not 2-manifold

Table 4: Collision detection (C.D.) and overlapping triangles (O.T.) calculation (s) between object A and B using the proposed strategies.

Model A	Model B	Octree		Tetra-tree		PQP		Swift++
		C.D.	O.T.	C.D.	O.T.	C.D.	O.T.	Collision
Buddha	Horse	0,5807	0,6236	0,2161	0,409	0,0034	0,0104	Not-2-Manifold
Buddha	Skull	1,8118	2,2317	0,2787	1,712	0,0076	0,017	Not-2-Manifold
Buddha	Bunny	1,2058	1,7777	0,2481	1,1735	0,0102	0,041	Not-2-Manifold
Buddha	Armadillo	2,026	4,5383	0,875	3,447	0,0106	0,4625	Not-2-Manifold
Dragon	Horse	0,4144	0,3593	0,1444	0,307	0,0014	0,0043	Not-2-Manifold
Dragon	Skull	0,8103	1,7643	0,2064	1,1583	0,0034	0,009	Not-2-Manifold
Dragon	Bunny	0,6852	1,4197	0,2195	0,8823	0,0045	0,0145	Not-2-Manifold
Dragon	Armadillo	1,1456	3,622	0,573	2,69	0,0087	0,0313	Not-2-Manifold
Armadillo	Horse	0,0923	0,32	0,0892	0,22	0,0013	0,004	≈ 0
Armadillo	Skull	0,2605	1,5928	0,1108	1,184	0,0026	0,0054	≈ 0
Armadillo	Bunny	0,234	1,483	0,1673	0,9248	0,0033	0,009	≈ 0
Armadillo	Armadillo	0,588	3,3435	0,4418	3,207	0,0037	0,016	≈ 0

same level and maximum threshold of triangles per node. Nevertheless, it should be noted that the octree performs 8 subdivisions in each node and the tetra-tree performs only 4, hence the number of octree nodes is higher. The results are shown in table 2. In general, the tetra-tree has less pre-processing time, but it needs more memory space.

The pre-processing time and size of the proposed bounding volumes hierarchies have been measured. Moreover, the convex hull has also been tested. The size of each structure has been measured theoretically because the real size depends on each machine and compiler. Therefore, the calculated size is approximate.

In the case of spatial decompositions, size has been calculated based on the theoretical size of each node. In order to achieve this, the number of nodes and their associated triangles have been measured. It was considered that each node in the tetra-tree requires 88 bytes: 16 bytes for children nodes (4 bytes for each child pointer) and 72 bytes for tetra-cone vertices (24 bytes per vertex). Since the centroid is a common vertex for all the tetra-cones, it only needs to store 3 vertices per tetra-cone. Additionally, the root node requires 340 bytes: 4 bytes for the origin pointer,

8 bytes for the pointers to the lists of vertices and triangles (4 bytes per pointer), 8 bytes for the number of vertices and triangles (4 bytes per number), 32 bytes for the eight initial tetra-cones (4 bytes for each tetra-cone pointer), and 576 bytes for the vertices of the initial tetra-cones (3 vertices per tetra-cone and 24 bytes per vertex). The octree requires 80 bytes per node: 32 bytes for children nodes (4 bytes for each children pointer) and 48 for the structure (2 vertices and 3 coordinates per vertex). In this case, the root node requires 72 bytes: 8 bytes for the pointers to the lists of vertices and triangles, 8 bytes for the number of vertices and triangles, 32 bytes for the initial octants (4 bytes for each octant), and 24 bytes for the initial structure. In addition, both spatial decompositions need 4 bytes for each classified triangle.

PQP allows knowing the size of each structure at runtime, hence this procedure has been used to calculate the approximate size of the structure associated with each model. It has not been possible to reach the size of the data structures used by SWIFT++. However, this library allows exporting the hierarchies to a file in order to facilitate reuse. We have used the size of this file to approximate the size of the hierarchical structure.

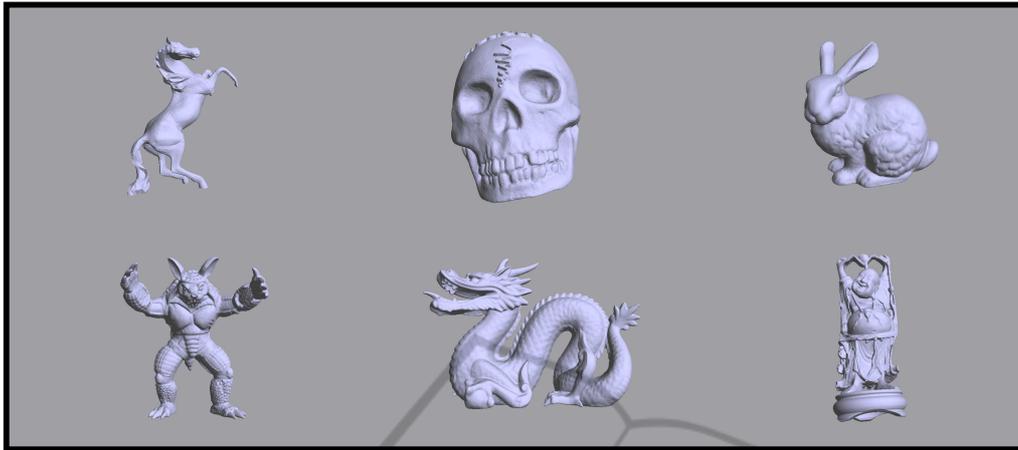


Figure 1: Models used for testing. From left to right and from top to bottom: horse, skull, bunny, armadillo, dragon and buddha.

The results are shown in table 3. PQP is the option that requires less pre-processing time, but it needs a large amount of memory space. SWIFT++ also take a long time and a lot of memory to build its structure. Moreover, it can not work with all of the proposed models. The convex hull size is small because its structure is very simple.

Table 4 shows the performance of each method to calculate a collision detection and overlapping triangles. SWIFT++ is the fastest method we are tested, but it can not work with all the proposed models because some of them are non-2-manifold. Moreover, it does not allow determining overlapping triangles. PQP has a reasonable good performance and its main advantage is that can work with all the proposed models. The spatial decomposition based methods do not have good results. In both cases, spatial decompositions have been built under the same conditions as in table 2.

Some tests to measure the performance of the tetra-tree in an interactive environment are realized in (Jiménez et al., 2011). Models of different sizes are used in order to perform these tests. Their results show, in the same way as ours, that the tetra-tree require less pre-processing time that the octree, but it needs a little more space in memory. The tests show that the tetra-tree has some advantages with respect to other approaches. Some of the main benefits are that the tetra-tree enables the selection of inaccessible parts without the use of extra algorithms and enable an accurate level of detail.

3.2 GPU Optimization

Some of the proposed strategies obtain good results, hence they can be applied to real-time interactive en-

vironments. However, some complex applications, such us haptic interaction or complex deformations, may require higher performance. In haptic interaction, the refresh rate is 1Khz (Lin and Otaduy, 2008), hence the collision detection should be calculated in less than one millisecond. In order to achieve that, the approaches shown could be improved and optimized by using the GPU.

Spatial decompositions are not easily adaptable to be used in parallel algorithms. However, in (Jiménez et al., 2009) a novel algorithm is presented. This algorithm allows building and utilizing spatial decompositions in GPU. For that, they propose to use the geometry shader. Each execution unit classifies a triangle in a certain level, regardless of others. They propose to use a n-sized texture for each level of the hierarchy, where n is the number of triangles. Hence, the mesh should be processed l times, where l is the level of the hierarchy, in order to classify the mesh. In addition, they propose to pre-calculate the spatial decomposition volume and codify it through a 2D texture.

The other libraries used do not have a GPU implementation. However, in (Srungarapu et al., 2011) the authors present a method to construct a convex hull in GPU that could be adapted to build it in 3D. This could be used in order to improve the convex hull strategy. Moreover, it would be interesting to consider a GPU implementation of the other proposed strategies.

4 CONCLUSIONS

In this work, we have presented some strategies to detect collisions in interactive environments. Moreover, some of the exposed methods allow performing other

interesting calculations, such as distances or nearest points. On the one hand, SWIFT++ is the faster library we tested, but it requires a lot of pre-processing time. On the other hand, PQP does not require much pre-processing time and it is quite efficient at calculating collisions. Therefore, the use of each library depends on the needs of each particular problem.

Since the octree and the tetra-tree has been implemented without the use of any library, both spatial decompositions, along with the Feito's algorithm, can be utilized to develop interactive systems that require to implement extra functionality. Due to its robustness, PQP is a good option in systems that work with meshes that could be topologically not correct. This is the case of systems that work with reconstructed meshes, such as surgery simulators with medical images and scanner data. Moreover, PQP could be a good solution for visualization applications, since meshes used in such applications do not need to be topologically correct. Finally, the SWIFT++ library is suitable for real time environments that require a good performance but that can ensure that the topology of the models is correct. For that reason, this library could be used for working with solid models which have been generated by mathematical and boolean operations that conserve their topology. In addition, this library could also be used in machining simulation. In all three approaches, the implemented systems must support a pre-processing step in which construct the data-structures.

ACKNOWLEDGEMENTS

This work has been partially supported by the Ministerio de Ciencia e Innovación and the European Union (via ERDF funds) through the research project TIN2011-25259 and by the University of Jaén through the research project UJA2010/13/08 sponsored by Caja Rural de Jaén.

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