

The Brain in a Box

An Encoding Scheme for Natural Neural Networks

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Abstract: To study the evolution of complex nervous systems through artificial development, an encoding scheme for modeling networks is needed that reflects intrinsic properties similar to natural encodings. Like the genetic code, a description language for simulations should indirectly encode networks, be stable but adaptable through evolution and should encode functions of neural networks through architectural design as well as single neuron configurations. We propose an indirect encoding scheme based on Compositional Pattern Producing Networks (CPPNs) to fulfill these needs. The encoding scheme uses CPPNs to generate multidimensional patterns that represent the analog to protein distributions in the development of organisms. These patterns form the template for three-dimensional neural networks, in which dendrite- and axon cones are placed in space to determine the actual connections in a spiking neural network simulation.

1 INTRODUCTION

If evolutionary development, i.e., the stepwise improvement through mutation and crossover, is seen as a means of understanding natural networks, two open questions in particular present themselves. First, how must a description language for neural networks (e.g. complex nervous systems) look like? And second, what are appropriate fitness functions to evolve complex networks? In this article, we propose an answer to the first question.

Because such a description language has to be capable of developing natural neural networks, it is imperative to know the intrinsic properties of the networks that should be modeled. In neuroscientific disciplines, numerous properties of natural neural networks are well-accepted that, in our opinion, should receive considerably more attention in those disciplines that try to model networks by evolutionary means.

For instance, the cortex of the brain consists of layers of different neuron types interconnected with each other. The connections are a side-effect of the position of the neurons within the layer, their anatomical form and their intersection with other neurons (Wolpert, 2001). Connections between neurons can be either specific (a clear and precise determination

of connections, e.g. as it can be found in the thalamus (Basso et al., 2005)) or driven by side effects (e.g. adjacent regions are interconnected with each other).

Furthermore, the (genetic) encoding scheme for natural organisms itself has certain properties that should be considered in simulations. In biological organisms, comparatively few genes (e.g., the human genome consists of circa 22,000 genes) encode complex structures by using highly indirect mechanisms. The encoding involves local interactions between cells, diffusion of substrates and gene regulatory networks. One purpose of these mechanisms is to generate global patterns from local interactions between genes that serve as axes for the organization and refinement of (cellular) structures (Meinhardt, 2008; Raff, 1996; Curtis et al., 1995). From this notion, it can be concluded that an encoding scheme for the evolutionary exploration of neural networks should work in a highly indirect manner as well and serve as a pattern generator for subsequent structural elements. If the network architectures should be improvable via evolutionary mechanisms, the encoding scheme must fulfill requirements for generating stable network architectures across generations, but should also facilitate alterations in the network that can impact (and improve) their functionality.

In the following, we propose an encoding scheme,

which we call *Brain In a Box* (BIB), that aims to generate networks with the outlined properties via pattern generation. It comprises three steps which will be described in detail in the following sections: *i*) Generate global patterns of protein densities, representing potential neuron locations and their properties; *ii*) Convert these patterns into a 3D-representation of neurons where axon- and dendrite-cones are used to determine connections between neurons; *iii*) Run a neural network simulation using the inferred network configuration. We think, that this encoding scheme is not only useful in the evolutionary exploration of network architectures, but can also serve as a model to describe real neural networks.

2 STEP 1: GLOBAL PATTERN GENERATION

In a BIB, network architectures are inferred from neurons placed in a three-dimensional space. Each neuron can be characterized by several properties impacting their potential connections to other neurons. These properties include, for instance, its position and its orientation in space. Potential axons and dendrites are indicated through cones projecting away from the neuron (Fig. 4). The length of the cone and its width (defined by its angle) determine a volume that may intersect with cones of other neurons. In case of an intersection, a density parameter of the neuron determines the chance for a potential connection. In a biological sense, different types of proteins form – depending on its concentration, location and combination with other proteins – the structure of a neuron. Connections between neurons are just a subsequent, probabilistic side-effect of their properties and placement in space.

BIBs are generated by mapping the three space coordinates, a distance and a bias value to several output values, representing the above mentioned properties of the neuron (Fig. 1). The mapping is computed by Compositional Pattern Producing Networks (CPPNs) which model how gene regulatory networks (GRNs) generate global patterns, while exploiting computational shortcuts in the simulated world (Stanley, 2007) (Fig. 2). An additional output node encodes whether a neuron is built at a given location. Intermediate genes are activated either by the (initial) input values or by other genes and generate density distributions that modulate, for instance, axon length and orientation of the neuron. Thus, a single gene may have a modulating influence on either one or several properties of neurons. This means, the functional role of neurons is controlled by genes influencing the struc-

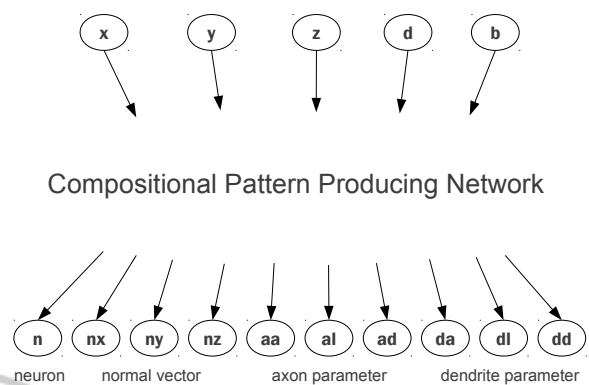


Figure 1: Structure of a CPPN for a BIB. The axes of the three-dimensional space (x , y , z) a bias value (b) and a distance value indicating the distance for a given point to the center of the volume (d (Stanley, 2007)), are mapped via a CPPN (see also fig. 2) on various parameters of the neuron. The output values encode, whether a neuron should be placed (n), the orientation of the neuron (nx , ny , nz), and the angle, length and density of the axon and dendrite cones (aa , al , ad , da , dl , dd).

tural properties of the neurons.

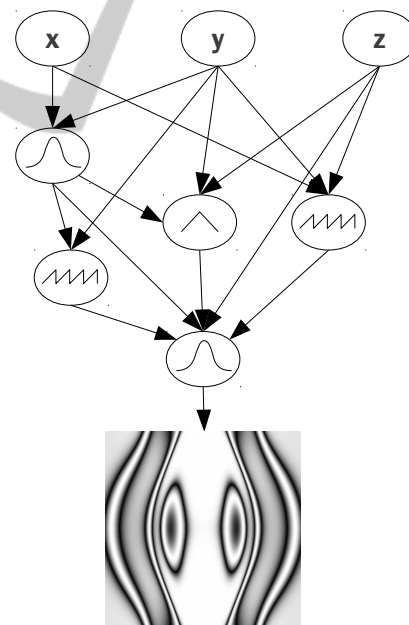


Figure 2: Example of a Compositional Pattern Producing Network. Global axes serve as input for concatenated functions generating two- or three-dimensional patterns. The functions represent the analog to density distributions of genes which activate other genes.

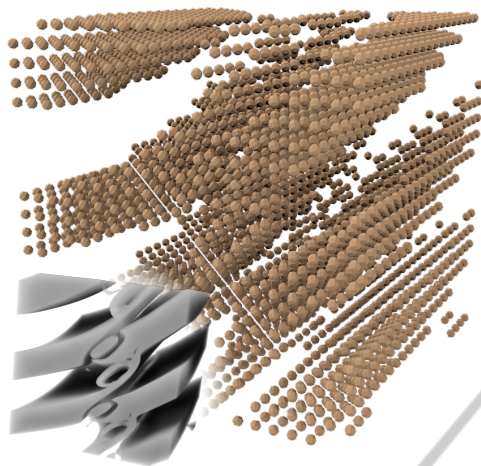


Figure 3: 3D-representation of a neural network using a resolution of $20 \times 20 \times 20$ neurons. For clarity's sake, cones for axon and dendrite connections are not displayed. In the lower left corner, the volume generated by the CPPN is depicted in a higher resolution.

3 STEP 2: CONVERSION OF THE NETWORK INTO 3D

The patterns generated in the previous step are used to generate a 3D-representation of the neural network (fig. 3). Only at this stage, it is necessary to specify the spatial resolution in which the neural network should be generated. A routine calls the CPPN with all coordinate values in the given resolution and determines, whether or not a neuron should be placed at a given location, and if yes, which properties the axon- and dendrite cones have (Fig. 4). If axon- and dendrite cones intersect, density parameters of the cones provided by the CPPN (ranging from 0.0 to 1.0) are multiplied and used as probability for a directed connection generated between both neurons.

Since BIBs can also be used to model real (biological) neural systems, such as cortex layers, the 3D-representation provides a means to obtain face validity upon a given anatomical structure. Here, again the role of genes within the model can be characterized and validated against the potential role of biological candidate genes.

4 STEP 3: SPIKING NEURAL NETWORK SIMULATION

The network information obtained from the previous step can subsequently be used in any type of neural network simulations to simulate and test

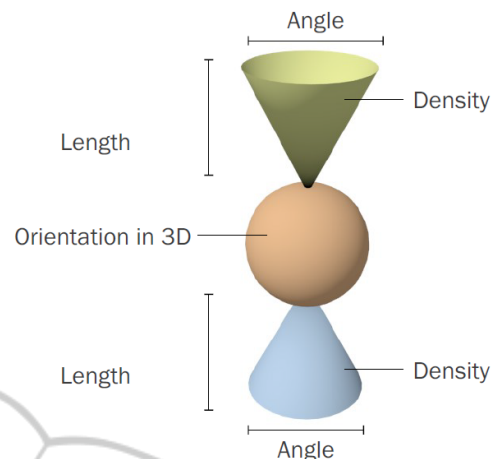


Figure 4: Three-dimensional representation of a neuron. A neuron is characterized by its location in space, its orientation and some parameters describing the cones for potential axons and dendrites. The green cone represents potential axon-connections and the blue cone potential dendrite connections.

the network. In our BIB-code, we chose *Brian* (www.briansimulator.org, (Goodman and Brette, 2008)) as framework for implementing a spiking neural network system. For each 3D-neuron generated in the second step, a neuron was generated in Brian and connected with other neurons as determined in the 3D-representation. The time-course of each neuron was defined as

$$\frac{dV}{dt} = \frac{-(V - E_L)}{\tau}, \quad (1)$$

where V is the activity of a neuron for a certain point t in time. E_L can be regarded as an attractor or resting state of the neuron and τ is a time-scaling factor. If V exceeds a threshold V_r , the neuron sends a spike through the axon and V is set to a reset-level V_r , from which it approximates E_L as described in Eq. (1).

5 SIMULATION

In the following, we will demonstrate that BIBs might be a valuable framework for two purposes: On the one hand, BIBs can be used to develop networks with evolutionary means. This implies, however, a well-defined fitness-function that reflects somehow the function of a dedicated region in a brain. On the other hand, BIBs can be used as a model to imitate biological relationships between genotype and phenotype of brain structures.

Having said this, we argue that, in principle, controller networks can be evolved and BIBs can generate networks, in which groups of neurons on different

scales can be altered in a semantical meaningful manner.

5.1 Proof of Principle

In a first test, we show that the evolutionary algorithm implemented in NeuroEvolution of Augmenting Topologies (NEAT) (Stanley, 2002) also works for BIBs. This is achieved via a simulation, in which an organism, controlled by a network of sensors, neurons and motors, can navigate on a 2D-plane with different concentrations of a notional substrate called “feed”. The plane is represented by a 10x10 raster, in which the center of each field has a different concentration of the substrate. The “feed” concentration of any intermediate point in the continuous space is the interpolated value of the four adjacent centers (Fig. 5a). The fitness value of the organism increases by harvesting the “feed” of the raster field on which it is located. At the same time, the “feed” volume decreases on the field when it is harvested. Thus, the organism has to move to other fields in order to “consume” more “feed”. Additionally, the fitness of the organism is decreased by the number of neurons (divided by 100). Thus, a solution with less neurons is regarded as more efficient.

To interact with the environment, we amended the BIB-model by sensors and motors, which represent special types of neurons. Sensors are able to measure the “feed”-concentration at their location. Motor neurons can generate an impulse for a movement. The direction of the movement is determined by the relative direction between the center of the neural net and the position of the motor neuron in the network. As we used spiking neurons for the transition of information, the “feed” concentration was converted into a sequence of spikes originating from the sensor neurons. A higher concentration of “feed” leads to a higher firing rate. Likewise, a higher firing rate of a motor neuron generates a stronger impulse for a movement into a certain direction. The CPPN of a BIB was extended by two output nodes encoding the existence of sensor and motor neurons for a given location. A BIB, converted to a neural network, was simulated for 5 seconds (simulation time) in intervals of 250ms.

The evolutionary algorithm of NEAT was used to improve the network configuration. 100 individuals per generation were tested and the four best individuals of each species were used to create the next generation. Crossover was always applied in order to generate a new genome. New genes were added with a probability of 0.1, new connections between genes with a probability of 0.2 and continuous changes of the connection weights with a probability of 0.2.

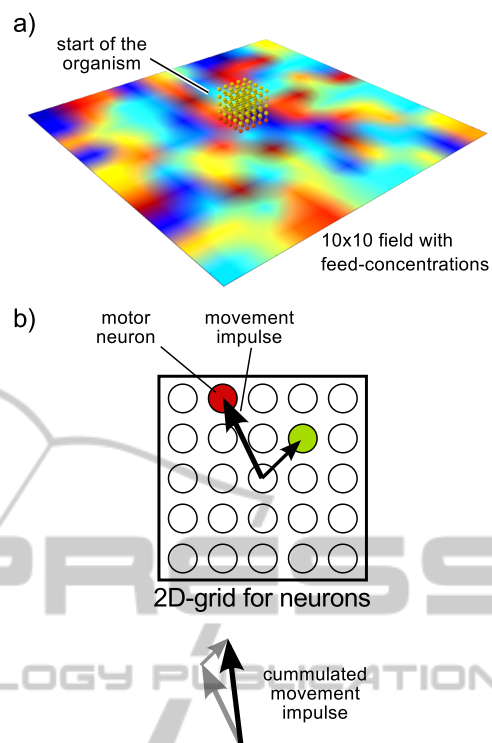


Figure 5: Some elements of the simulation. a) The organism moves on a 2D-plane with different concentrations of a fictive substrate called “feed”. The concentration of any point on this plane is the interpolated value of the centers of each field. b) The frequency of a spiking motor neuron determines the strength of a movement impulse towards its direction. The cumulated sum of movement impulses is the direction in which the organism moves.

Three-dimensional networks were created with a resolution of five neurons per axis.

The whole evolutionary search was repeated ten times. In all runs, networks were found in which sensors forwarded information to motor neurons in order to move the organisms towards higher concentrations of “feed”. In some solutions, normal neurons were completely avoided to transport sensory information to the motor neurons. Figure 6 shows some of the networks that have been generated. The evolutionary search revealed that those BIBs that have wider axon cones in order to reach more motor neurons, show increased fitness because they can move faster towards higher concentrations of “feed”. This example provides evidence that changes in the BIB can lead to abstract alterations in the neural model (such as axon cone width) that can influence the fitness of the model.

As the network is generated from a CPPN, changes in the expression intensity of a gene can have a global influence on the anatomy of the network, when they are directly or indirectly (via gene-

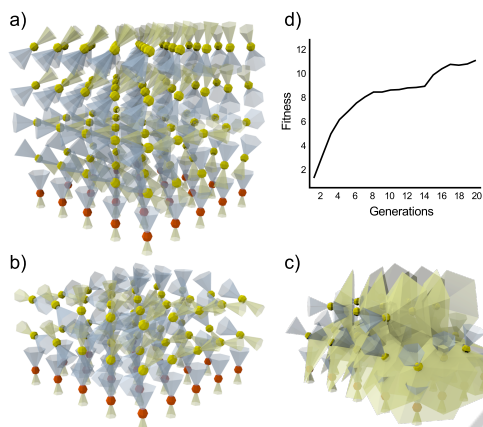


Figure 6: Some networks generated by the evolutionary search for BIBs. Yellow spheres represent sensor neurons, red spheres represent motor neurons. Cones indicate axon- and dendrite areas of the neurons. a) One of the first networks, that successfully controlled the organism towards more “feed”. b) and c) are more sophisticated versions of a) with less neurons and wider axon-cones leading to a faster movement of the organism and less energy consumption. d) depicts the averaged fitness for one run over 20 generations.

interactions) involved in the activation of certain neural parameters. However, continuous changes of gene-values cause continuous changes in the network architecture. Thus, an evolution-driven search can gradually improve fitness by altering the weights of the cis-regulatory elements. New genes or cis-elements can have a stronger influence of the network architecture leading to new innovations.

5.2 BIBs as a Model for Complex Nervous Systems

A BIB does not model a developmental growth process in terms of local interactions, cell division or cell movement but encodes the properties of a given location directly. However, this does not mean that a BIB does not reflect the outcome of a growth process. As already argued for CPPNs (Stanley, 2007), genes and their corresponding proteins are involved in a cascade of local interactions and diffusion processes that generate gradients of various protein concentrations (Meinhardt, 2008; Raff, 1996; Curtis et al., 1995). These gradients serve as local axes for subsequent local reactions with other genes. From this perspective, genes, not directly involved in building structural elements, can be regarded as density functions activating or inhibiting other genes and thereby facilitating coordination on various spatial scales. Therefore, CPPNs (and BIBs) implicitly model the chronology of developmental events and cell interactions by concatenating functions with each other as depicted in Fig. 2.

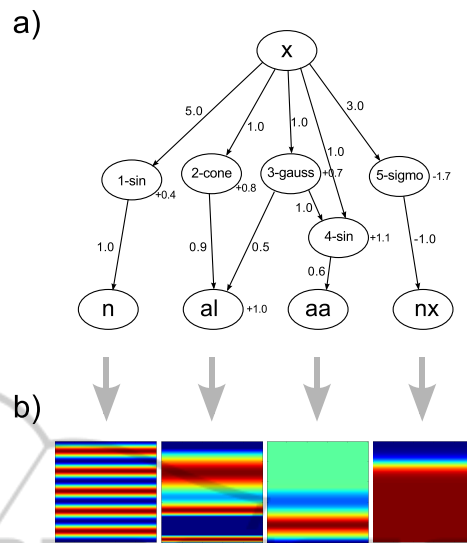


Figure 7: BIB as model for cortical layers. a) A CPPN with five genes generates patterns along the x-axis for certain properties of the neurons. b) 2D-Slides of the output values modulated by the genes.

The BIB-scheme amends the properties of CPPNs by modeling connections between neurons as side-effect of their location, orientation, anatomical structure and coincidental intersections with other neurons. This means that, like in biological systems, genes control global properties of the anatomy, single connections between neurons are derived from that as side-effect.

The BIB-approach might be therefore a valuable tool to combine gene interactions, single neuron properties and large-scale cortical and subcortical structures in one model. Rudimentary examples for this are given in figure 3 and 7. Figure 7a shows a CPPN for generating cortical layers. Using one coordinate axis, eight genes contribute to the formation of neuronal elements and the length and angle of the axon and dendrite cones. The density distribution of the output genes controlling the properties of the neurons are depicted in fig. 7b. Like MRI- or diffusion tensor imaging (DTI) data, the pictures show the anatomical properties of the network in one slice (for instance, neuron locations, projections) in a color encoding. These data can be sampled in any resolution to generate the three-dimensional representation of the cortical layers (fig. 8). In future work, such models can serve as a model to better understand the relation between certain genes and their phenotypic influence on the neural network.

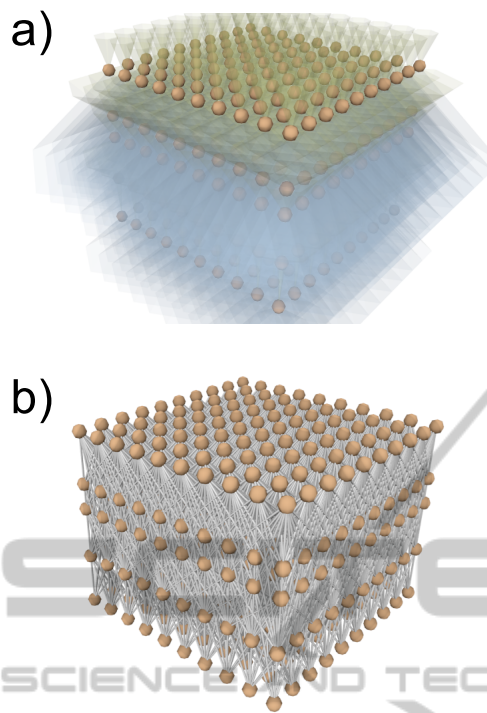


Figure 8: The neural network generated from the CPPN depicted in fig. 7. Neurons with axon and dendrite cones are placed in space according to the local properties generated by the CPPN a). These cones are used to detect connections between neurons, depicted in b).

6 DISCUSSION

In this paper, we proposed a model for generating complex neural networks based on an indirect encoding scheme for three-dimensional patterns, which we call *Brain in a Box*, or BIB. Connections between neurons are only affected indirectly, as their position, orientation, axon and dendrite parameters determine the connection to other neurons. In this regard, single genes in a BIB modify abstract properties of the network, such as the thickness of neuronal layers, the degree of branching or the proximity of neural groups. Thus, BIBs reflect a way of modeling networks that, to our mind, corresponds more to biological mechanisms for the emergence of complex nervous systems originating from gene regulatory networks. In this context, BIBs might also be a valuable tool to describe structural properties of real biological networks through gene interactions. By exploiting properties of CPPNs, BIBs show an inherent stability across generations and but also the ability to change global properties of the network architecture to increase fitness.

Future research will focus on defining appropriate fitness-functions to model certain functional prop-

erties of areas in complex nervous systems through BIBs. These functions may include short- and long-term plasticity for the storage of information, learning of patterns / sequences for motor control or the detection of errors between perceived and expected information.

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