

Prediction of PM_{2.5} Concentrations using Fuzzy Inductive Reasoning in Mexico City

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Abstract: The research presented in this paper is focused on the study and development of fuzzy inductive reasoning models that allow the forecasting of daily particulate matter with diameter of 2.5 micrometres or less (PM_{2.5}). FIR offers a model-based approach to modelling and predicting either univariate or multivariate time series. In this research, predictions of PM_{2.5} concentration at hour 12 of the next day, in the downtown of Mexico City Metropolitan Area, are performed. The data were registered every hour and include missing values. In this work the hourly modelling perspective is analyzed. The results are compared with the ones obtained using persistence models showing that the FIR models are able to predict PM_{2.5} concentrations more accurately than persistence models.

1 INTRODUCTION

The high levels of particulate matter in the air are of high concern since they may produce severe public health effects and are the main cause of the attenuation of visible light. There are very high levels of particles in North Africa, much of the Middle East, Asia, Latin America as well as in the large urban areas. Comparing it with population density maps, the WHO concluded that more than 80% of the world population is exposed to high levels of fine particles (PM_{2.5}) (WHO, 2006). Likewise, identifies PM_{2.5} as an important indicator of risk to health and might also be a better indicator than PM₁₀ for anthropogenic suspended particles in many areas (van Donkelaar et al., 2010). According to the WHO Guidelines, concentrations at this level and higher are associated with an approximately 15% increased risk of mortality, relative to the Air Quality Guideline (AQG) of 10 µg m⁻³ (WHO, 2006).

Regarding the PM_{2.5}, it has not yet been identified a threshold below which damage to health does not occur, this has motivated that the limits for the protection of public health are getting lower every year. The geographical characteristics of the Mexico city metropolitan area, i.e. its height, average temperature and terrain, added to the pressure exerted by the growth and intensification of urban activities cause high air pollution episodes that

constitute a permanent challenge to the health of its inhabitants. Although the measures taken over the past 15 years to reduce the impact of air pollution have managed to significantly decrease pollutants such as SO₂, CO or the Pb, the concentrations of ozone and fine particles exceed quite often air quality standards.

The monitoring of PM_{2.5} from 2004 to date shows that around 20 million people in Mexico city are exposed to annual average concentrations of this contaminant in between 19 and 25 µg m⁻³, exceeding by more than double the WHO standard of 10 µg m⁻³ and substantially exceeding the Mexican norm of 15 µg m⁻³.

The increase of the concentration of particles in Mexico city is strongly associated with the meteorology of the Valley. During the days of intense wind, resuspension of dust from the ground produces significant increases in the concentrations of total suspended particles (PST) and particles lower than 10 µm (PM₁₀). The presence of surface thermal inversions can contribute to the increase in the concentration of particles smaller than 10 µm and fine particles, due to the lack of dispersion and the accumulation in the atmosphere of the particles emitted by vehicles and industry. Higher concentrations usually occur when the layer trapped under the inversion is not very high and the duration of the thermal inversion is maintained throughout the morning.

The national weather service reported a total of 107 days with surface thermal inversions during 2010, the highest in the past 13 years. The largest part was recorded during the winter months, when the long and cold nights favor its formation. In the dry season months it has been reported a 40% of days with thermal inversion. The months of April and December had the largest number of events with 16 and 17 days, respectively. The influence of high pressure systems during the months of March to May was responsible for the formation of surface thermal inversions (NWM, 2012).

In this research we propose predictions models of hourly concentrations of $PM_{2.5}$, based on data obtained at downtown Mexico city. We show results obtained with two different methods, all of which use past values of $PM_{2.5}$ as input. The simplest method is persistence, which assigns hourly values on the next day equal to the values at the present day. Then we used the fuzzy inductive reasoning approach that is a non-linear methodology based on fuzzy logic and pattern recognition. We used registered data of 4 year periods, each lasting six months starting on December 1st. As explained before, the months from December to May are the ones that have higher levels of $PM_{2.5}$ concentrations in Mexico city metropolitan area.

In section 2 some basic concepts of the fuzzy inductive reasoning approach are introduced. In section 3 the methodology used is described, i.e. the data, the fuzzy models development and the models evaluation. Section 4 describes the results obtained. Finally the conclusions of this research are given.

2 FUZZY INDUCTIVE REASONING (FIR)

The conceptualization of the FIR methodology arises of the General System Problem Solving (GSPS) approach proposed by Klir (Klir and Elias, 2002). This methodology of modeling and simulation is able to obtain good qualitative relations between the variables that compose the system and to infer future behavior of that system. It has the ability to describe systems that cannot easily be described by classical mathematics or statistics, i.e. systems for which the underlying physical laws are not well understood.

The Fuzzy Inductive Reasoning (FIR) methodology, offers a model-based approach to predicting either univariate or multi-variate time series (Nebot et al., 2003); (Carvajal and Nebot,

1998). A FIR model is a qualitative, non-parametric, shallow model based on fuzzy logic. Fuzzy logic-based methods have not been applied extensively in environmental science, however, some interesting research can be found in the area of modeling of pollutants (Mintz et al., 2005); (Ghiaus, 2005); (Morabito and Versaci, 2003); (Heo and Kim, 2004); (Yildirim and Bayramoglu, 2006); (Peton et al., 2000); (Onkal-Engin et al., 2004), where different hybrid methods that make use of fuzzy logic are presented for this task.

Visual-FIR is a tool based on the Fuzzy Inductive Reasoning (FIR) methodology (runs under Matlab environment), that offers a new perspective to the modeling and simulation of complex systems. Visual-FIR designs process blocks that allow the treatment of the model identification and prediction phases of FIR methodology in a compact, efficient and user friendly manner (Escobet et al., 2008).

The FIR model consists of its structure (relevant variables) and a set of input/output relations (history behavior) that are defined as if-then rules. Feature selection in FIR is based on the maximization of the models' forecasting power quantified by a Shannon entropy-based quality measure. The Shannon entropy measure is used to determine the uncertainty associated with forecasting a particular output state given any legal input state. The overall entropy of the FIR model structure studied, H_s , is computed as described in equation 1.

$$H_s = -\sum_{\forall i} p(i) \cdot H_i, \quad (1)$$

where $p(i)$ is the probability of that input state to occur and H_i is the Shannon entropy relative to the i^{th} input state. A normalized overall entropy H_n is defined in equation 2.

$$H_n = 1 - \frac{H_s}{H_{\max}} \quad (2)$$

H_n is obviously a real-valued number in the range between 0.0 and 1.0, where higher values indicate an improved forecasting power. The model structure with highest H_n value generates forecasts with the smallest amount of uncertainty.

Once the most relevant variables are identified, they are used to derive the set of input/output relations from the training data set, defined as a set of if-then rules. This set of rules contains the behaviour of the system. Using the five-nearest-neighbors (5NN) fuzzy inferencing algorithm the five rules with the smallest distance measure are selected and a distance-weighted average of their

fuzzy membership functions is computed and used to forecast the fuzzy membership function of the current state, as described in equation 3.

$$Memb_{out_{new}} = \sum_{j=1}^5 w_{rel_j} \cdot Memb_{out_j} \quad (3)$$

The weights w_{rel_j} are based on the distances and are numbers between 0.0 and 1.0. Their sum is always equal to 1.0. It is therefore possible to interpret the relative weights as percentages.

For a more detailed explanation of the fuzzy inductive reasoning methodology refer to (Escobet et al., 2008).

3 METHODOLOGY

3.1 Data

The data used for this study stems from the Atmospheric Monitoring System of Mexico City (SIMAT in Spanish) that measures contaminants and atmospheric variables from 36 stations distributed through the 5 regions of the Mexico City metropolitan area (SIMAT, 2012). The registered variables are the air pollutants, including PM_{2.5}, as well as other 10 contaminants, and meteorological variables, 24 hours a day, every day of the year. The web page of SIMAT (SIMAT, 2012) offers a data base with meteorological and contaminant registers since 1986 up to date, although PM_{2.5} has been registered for the first time in 2004.

A mechanically oscillated mass balance type instrument, TEOM 1400a, is used for the registration of the PM_{2.5}. This instrument is very sensitive to changes in concentrations of mass and can provide accurate measurements for samples with less than an hour in length.

This study is centered on the univariate modeling and forecasting of particulate matter with diameter of 2.5 micrometres or less (PM_{2.5}) in the Merced station, located in the commercial and administrative district at the downtown of Mexico City Metropolitan Area (MCMA).

The PM_{2.5} variable is an hourly instantaneous observation, not the maximum or the mean of minute registered data. We have chosen to work with the scalar time series on PM_{2.5} concentrations keeping in mind the idea that if we use a large enough window of data as input, the effect of other

pollutants or meteorological data should be implicit in its structure (Pérez et al., 2000).

The typical pattern of PM_{2.5} from some city areas, such is for example downtown, suggests that concentrations of this contaminant increase regularly between 8:00 and 16:00 hours, with maximum concentrations around 13:00 hours (Muñoz et al., 2000).

Therefore, we have decided to use in this study data from the half of the year that Mexico city suffers higher PM_{2.5} concentrations, i.e. from December to May. We have used 4 data sets containing 6 month of hourly registers each one, i.e. from the 1st of December until de 31st of May, for years 2007-2008, 2008-2009, 2009-2010 and 2010-2011.

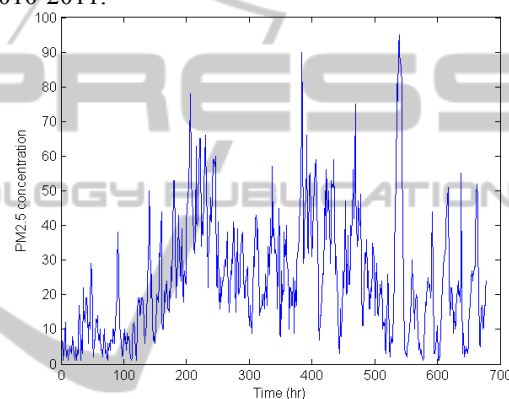


Figure 1: Hourly concentrations of PM_{2.5} data for December 2009. Units are $\mu\text{g m}^{-3}$. From the 720 data points, 42 are missing values that are not plotted.

For the first data set, i.e. 1st December 2007 to 31st May 2008, the average concentration is $31.2 \mu\text{g m}^{-3}$, the maximum is $147 \mu\text{g m}^{-3}$ and the standard deviation is $15.6 \mu\text{g m}^{-3}$. For the second data set, i.e. 1st December 2008 to 31st May 2009, the average concentration is $26.6 \mu\text{g m}^{-3}$, the maximum is $102 \mu\text{g m}^{-3}$ and the standard deviation is $14.3 \mu\text{g m}^{-3}$.

For the third data set, i.e. 1st December 2009 to 31st May 2010, the average concentration is $20.8 \mu\text{g m}^{-3}$, the maximum is $101 \mu\text{g m}^{-3}$ and the standard deviation is $13.4 \mu\text{g m}^{-3}$. For the last data set, i.e. 1st December 2010 to 31st May 2011, the average concentration is $32.5 \mu\text{g m}^{-3}$, the maximum is $175 \mu\text{g m}^{-3}$ and the standard deviation is $16.5 \mu\text{g m}^{-3}$. Fig. 1 shows the hourly concentrations of PM_{2.5} during December, 2009.

The data available contains missing values that correspond to data that was not registered due to instrument problems. From the total number of 17496 hourly data registered, 1316 are missing values.

3.2 Fuzzy Models Development

As mentioned before, our goal is to obtain FIR models capable of forecasting the $PM_{2.5}$ concentrations some time in advance, in such a way that efficient actions could be taken in order to protect the citizens of high concentrations episodes.

We first performed a study of the autocorrelation, both causal and temporal, of the $PM_{2.5}$ time series. To this end, we used the model structure identification process of the fuzzy inductive reasoning methodology that performs a feature selection based on the entropy reduction measure, described in section 2.

We have found that it is possible to relate the concentration of $PM_{2.5}$ at a given time of the day to the sequence of 24 points corresponding to the hourly concentrations on the previous day. Moreover, the structure of the fuzzy inductive reasoning model has determined that there is a direct causal relation between the level of pollution at present time and its values at hours 6, 12, 18 and 24. That is, there is a positive correlation at hours 12 and 24 and a negative correlation at hours 6 and 18.

With this information available we think that an interesting and useful approximation to modeling and forecasting $PM_{2.5}$ concentrations is to obtain a model for each hour of the day, based on the values of the 6, 12, 18 and 24 hours of the previous day, i.e. hourly models.

In order to study this approach, in this research we have developed FIR models for the prediction of hour 12 of the next day (FIR-12). The input variables of the system are $PM_{2.5}$ concentration at hours 6, 12, 18 and 24. Therefore, we have 4 input variables. The output variable is $PM_{2.5}$ concentration at hour 12 of the next day. Therefore, for this FIR prediction model, pollutant concentrations are given 12h in advance.

We plan to obtain FIR models, in the near future, for each hour of the day, i.e. FIR-1 to FIR-24, predictions will be made from 1 to 24 h in advance, respectively.

In order to obtain the FIR-12 model it is necessary to arrange the data in such a way that we have a data stream for each day instead of 24 data streams (one for each hour of that day).

The 4 data sets available have been arranged accordingly, obtaining now a total number of 725 daily data, out of which 220 are missing values.

In this work a 10-fold cross validation is used to assess how the results of the obtained models will generalize to an independent data set. The objective is to estimate how accurately the predictive models

developed in this study will perform in practice. As described before, 505 data points are available, i.e. 725 minus 220 missing. Therefore, 10 test sets with 50 data points and 10 training sets with 450 data points are used.

The first step in order to obtain the FIR-12 model is to convert quantitative values in fuzzy data, to this end, it is necessary to specify two discretization parameters, i.e. the number of classes per system variable (granularity) and the membership functions (landmarks) that define its semantics. In this study the granularity and the clustering method used to obtain the landmarks are summarized in table 1. Half of the folds are discretized into two classes using the fuzzy c-means clustering method. It is not possible to use more classes in this case because the number of training data (450 points) is not larger enough. Other clustering methods such as median linkage, k-means and equal frequency partition are also used in this study. However, no one of these methods take into account the uncertainty associated to the data in order to obtain the landmarks parameter.

Table 1: Interval values (landmarks) associated to each class for input and output variables.

	Number classes	Clustering method
FOLD 1, 5, 7, 8, 9	2	Fuzzy C-means
FOLD 2, 6	3	Equal Frequency Partition
FOLD 3, 10	2	Median Linkage
FOLD 4	2	K-Means

The FIR model structure obtained in this case may be described using the scheme shown in equation 4.

$$y_t = f_q(x_6, x_{12}, x_{18}, x_{24}) \quad (4)$$

where y_t is the predicted value at time t on the following day; x_i represent the pollution data on a given day at the i^{th} hour; and f_q is the qualitative relation of the FIR model. We focus this research in FIR models for $t=12$.

3.3 Model Evaluation

Two error measures were used to evaluate the performance of each of the FIR-12 models. These are: the root mean square error and the mean absolute error. The root mean square error (RMSE) is described in equation 5.

$$RMSE = \sqrt{\frac{\sum_{i=1}^N (y_i(t) - \hat{y}_i(t))^2}{N}} \quad (5)$$

where $\hat{y}(t)$ is the predicted output, $y(t)$ the system output and N the number of samples.

The mean absolute error (MAE) is defined in equation 6.

$$MAE = \frac{1}{N} \sum_{t=1}^N |y_t(t) - \hat{y}_t(t)| \quad (6)$$

4 RESULTS AND DISCUSSION

The results obtained by the FIR models are compared with the ones obtained when using the persistence method. This consist of a very simple prediction, i.e. tomorrow at time t PM_{2.5} mass concentration will be the same as today at time t . In this case equation 4 takes the form of equation 7.

$$y_t = x_t \quad (7)$$

Therefore, there are no parameters to adjust. The prediction results obtained by FIR and persistence models of the PM_{2.5} contaminant at hour 12 of the next day, for each fold, are summarized in table 2.

Table 2: Prediction errors of each fold separately and its average for the PM_{2.5} concentration series. Predictions are at hour 12 of the next day using FIR and persistence models. The inputs of the FIR models are PM_{2.5} at hours 6, 12, 18 and 24 today.

	MAE FIR	MAE PERS.	RMSE FIR	RMSE PERS.
FOLD 1 (1-50)	15.9	19.9	20.9	24.0
FOLD 2 (51-100)	13.6	13.7	17.6	18.3
FOLD 3 (101-150)	10.8	13.5	14.1	17.1
FOLD 4 (151-200)	13.3	14.7	16.8	18.6
FOLD 5 (201-250)	9.5	9.8	13.5	14.1
FOLD 6 (251-300)	17.0	19.7	21.9	26.8
FOLD 7 (301-350)	12.0	10.1	14.7	13.4
FOLD 8 (351-400)	19.0	22.1	25.1	31.4
FOLD 9 (401-450)	11.9	13.4	15.4	18.1
FOLD 10 (451-505)	11.9	13.1	15.5	17.0
MEAN FOLDS	13.5	16.5	17.5	19.9

From table 2 it can be seen that FIR models perform much better than persistence, for all the folds except for fold 7. Notice, that the range below the number of the fold means the set of forecasted

data. The mean prediction errors are significantly lower for the FIR models, i.e. 13.5 vs. 16.5 of MAE and 17.5 vs. 19.9 of RMSE. However, the accuracy of the predictions produced with the FIR models is probably poor in order for the results to have practical application in environmental pollution policies.

In order to try to enhance the previous results we have considered including meteorological variables in the study. Cobourn concludes that the meteorological variables that have a nonlinear relationship with PM_{2.5} statistically significant are maximum temperature and wind speed. Moreover, the strongest single relationship between PM_{2.5} and any one meteorological variable is the relationship with daily maximum temperature (Cobourn, 2010).

Therefore, the next step in our research was to study the prediction capability of the models when the maximum temperature of the day is also considered as an input variable.

In this case, the number of missing values increases and instead of 505 data available we only have 481. Therefore, each fold of the 10-fold cross validation has now 48 data points.

The FIR model structure obtained in this case may be described using the scheme shown in equation 8.

$$y_t = f_q(x_6, x_{12}, x_{18}, x_{24}, z) \quad (8)$$

where y_t is the predicted value at time t on the following day; x_i represent the pollution data on a given day at the i^{th} hour; z is the maximum temperature on a given day; f_q is the qualitative relation of the FIR model.

Table 3: Interval values (landmarks) associated to each class for input and output variables.

	Number classes	Clustering method
FOLD 1, 4, 8, 9	2	Fuzzy C-means
FOLD 2, 6, 7	2 and 3	Equal Frequency Partition
FOLD 3	2	Median Linkage
FOLD 5	2	K-Means

The granularity and the clustering method used to obtain the landmarks in this case are summarized in table 3.

Table 4 shows the prediction results obtained by FIR and persistence models of the PM_{2.5} contaminant at hour 12 of the next day, for each fold, when the inputs of the model are: PM_{2.5} at hours 6, 12, 18 and 24 and maximum temperature today.

As can be seen for the prediction errors of table 4 the inclusion of today's temperature as input

variable of the model does not enhance substantially the accuracy of FIR-12 models.

Table 4: Prediction errors of each fold separately and its average for the PM_{2.5} concentration series. Predictions are at hour 12 of the next day using FIR and persistence models. The inputs of the FIR models are PM_{2.5} at hours 6, 12, 18 and 24 and maximum temperature today.

	MAE FIR	MAE PERS.	RMSE FIR	RMSE PERS.
FOLD 1 (1-48)	17.1	20.4	21.4	24.4
FOLD 2 (49-96)	11.5	11.4	14.4	15
FOLD 3 (97-144)	11	13.8	13.8	17.7
FOLD 4 (145-192)	12.7	14.5	16.7	18.5
FOLD 5 (193-240)	10.6	9.5	14	14
FOLD 6 (241-288)	16.7	20.5	21.9	27.4
FOLD 7 (289-336)	10.4	10.3	12.7	13.6
FOLD 8 (337-384)	15.9	19.5	21.1	28.8
FOLD 9 (385-432)	11.6	12.7	15.7	17.3
FOLD 10 (433-481)	11.5	13.6	14.3	17.6
MEAN FOLDS	12.9	14.6	16.6	18.4

PM_{2.5} is a difficult contaminant to be predicted due to the fact that there are significant variations of the concentrations of this pollutant from one day to the next day, and, from one hour to the next one, even with similar weather conditions.

Previous works have been focused on the modelling and prediction of mean (Kang et al., 2010) or maximum (Cobourn, 2010) PM_{2.5} concentrations. Also, there are studies that perform binary predictions, i.e. if a dangerous level has been reached (Dong et al., 2009). Contrarily, we have focused on a short-term PM_{2.5} forecast, although uncertainties in hourly registers pose enormous challenges for developing accurate models.

5 CONCLUSIONS

In this paper PM_{2.5} models based on the fuzzy inductive reasoning approach were developed for downtown Mexico city metropolitan area, to predict the concentration of this contaminant at hour 12 of the next day.

The results obtained are better than the predictions encountered by persistence models.

However, we think that the accuracy reached is still poor for the results to have practical application in environmental policies.

In order to enhance the predictions the maximum temperature has been used as an additional input variable. The prediction errors are quite similar to the ones obtained by the FIR models when only PM_{2.5} is used.

As a future work we propose to:

- Include other meteorological variables into the model.
- Include additional information such as day of the week or hour of the day into the models.
- Develop models for all the hours of the day, in such a way that predictions will be from 1 to 24 hours in advance.
- Use hybrid modelling techniques such as fuzzy inductive reasoning with genetic algorithm, which will help to find in an efficient way the number of classes and landmarks parameters of FIR discretization process.

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