

FPGA Implementation of SOBI to Perform BSS in Real Time

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Keywords: EEG, BSS, SOBI, FPGA.

Abstract: Blind Source Separation (BSS) is an effective and powerful tool for source separation and artifact removal in EEG signals. For the real time applications such as Brain Computer Interface (BCI) or clinical Neuro-monitoring, it is of prime importance that BSS is effectively performed in real time. The motivation to implement BSS in Field Programmable Gate Array (FPGA) comes from the hypothesis that the performance of the system could be significantly improved in terms of speed considering the optimal parallelism environment that hardware provides. In this paper, FPGA is used to implement the SOBI algorithm of EEG with a fixed-point algorithm. The results obtained show that, FPGA implementation of SOBI reduces the computation time and thus has great potential for real time.

1 INTRODUCTION

EEG is one of the most widespread brain mapping techniques to date and is used extensively for monitoring the electrical activity within the human brain both for research and clinical purposes. The raw EEG data represent a projection of a set of signals, which are a mix of brain and artifact information. BSS is the process of recovering the source signals from a linear mixture of measured signals.

There is no general consensus about any one BSS Algorithm being the best. Each algorithm has its unique set of pros and cons and makes certain assumptions about the sources in order to compensate for the lack of information about the mixing matrix and to be able to process the signals blindly. (Joyce et al., 2004; Fitzgibbon et al., 2007) and (Hyvarinen et al.) can serve as good reads for literature on Artifact detection and removal in EEG signals. SOBI using time structure of signals has its unique set of advantages to offer as mentioned in (Delorme et al., 2007) and was the chosen algorithm in this work.

SOBI assumes stationary sources with non-identical spectra and considers components at various time lags and focuses on decorrelating them as much as possible. As mentioned earlier, SOBI

offers some unique advantages such as ability to resolve correlated signals, ability to resolve more than one gaussian sources, more robust behaviour in adverse Signal to Noise ratio (SNR), need for fewer data points implying shorter epoch length – something which is must for real time processing. The application and usefulness of SOBI in Brain Computer Interface has been shown in (Wang et al.). It was shown that SOBI converges after only a few iterations thus proving it worthy for real time applications. However, the computational complexity and cost for SOBI is high which can be partially taken care of by appropriate design of the FPGA architecture. Also, when real time processing is the main goal a little additional cost is justifiable.

In this paper, an FPGA implementation of the SOBI algorithm of BSS model is presented with co-simulation design concept based on the fixed-point number representation. The BSS Model and SOBI algorithm are introduced in Section 2. In section 3, the FPGA implementation is described. The result analysis and the conclusion are given in section 4 and 5.

2 ALGORITHM AND PROBLEM FORMULATION

2.1 BSS Model

BSS is the process of recovering the source signals from a linear mixture of measured signals. There are three distinct steps required for removal of artifact/noise from EEG using BSS: 1) separate (unmix) the measured EEG into sources using a BSS algorithm, 2) identify and discard artifact/noise sources and retain brain sources, and 3) project the retained brain sources back into sensor space resulting in artifact/noise-free EEG as is illustrated in Fig. 1

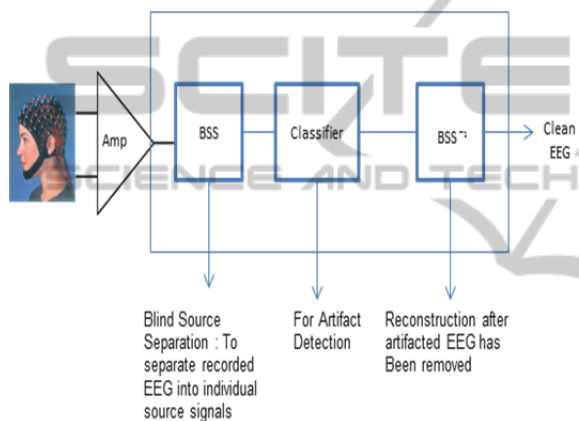


Figure 1: Artifact detection and removal using BSS.

Component estimation from EEG data can be mathematically formulated as follows.

$$X = AS \tag{1}$$

meaning that the sensor data X is rotated by an unmixing matrix A^{-1} , to arrive at the components S . To clarify, all quantities in Equation 1 are matrices. A is referred to as the mixing matrix, each column of

which describes signal propagation from an individual source to each electrode site. The meaning of “blind” is that both the original sources (represented by matrix S) and the way the sources were mixed (represented by A) are all unknown, and only mixed signals or mixtures represented by X) can be measured and observed.

2.2 SOBI Algorithm

SOBI was first introduced by Adel Belouchrani, Karim Abed-Meraim, Jean François Cardoso and Eric Moulines in the year 1997. The steps involved in SOBI algorithm are illustrated in Figure 2 while the detail explanation of the algorithm may be found in (Belouchrani et al., 1997). As previously stated, SOBI exploits the time coherence of the source signals for source separation. As opposed to the other approaches, it relies only on stationary second order statistics. It was shown in (Tong et al., 1990; Belouchrani et al., 1993) that blind identification is feasible based on the eigen decomposition of spatial covariance matrices. In (Belouchrani et al., 1997), blind identification is achieved by performing joint diagonalization of a set of spatial covariance matrices. In (Belouchrani et al., 1997) it was also shown that considering a set of matrices rather than unique correlation matrix increases the robustness at a low additional computing cost. SOBI exploits the time coherence of the source signals and assumes that the signals are uncorrelated in time. Also, for the sake of simplicity the noise is modelled as additive white noise. However, this assumption is not crucial. The aim of BSS is to identify the mixture matrix A and to recover the source signals $s(t)$ from the array output $x(t)$ without any a priori knowledge of the array manifold.

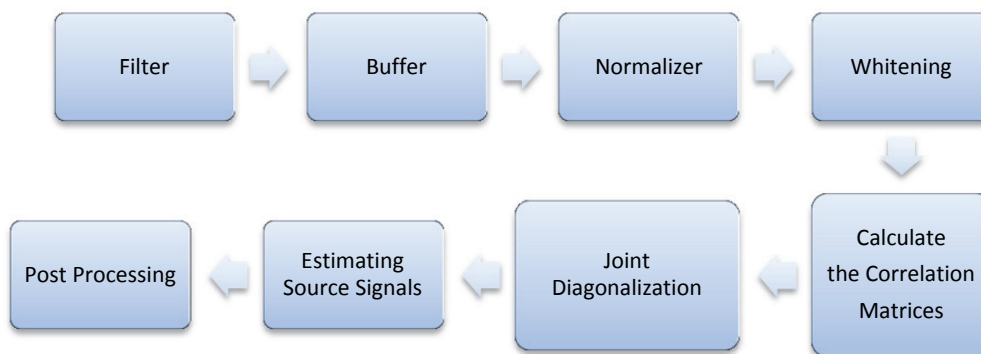


Figure 2: Schematic Representation of BSS using SOBI.

The first pre-processing step is Normalization so as to ensure that the source signals have unit variance. The next step is Whitening which is achieved by Singular Value Decomposition of the mixture matrices. Whitening reduces the dimensionality of the BSS problem, following which the mixing matrix A may be defined as

$$A = W^{\#}U \quad (2)$$

Where W is the whitening matrix and U is a unitary matrix. It is shown in (Belouchrani et al., 1997) that the whitening matrix is determined from covariance matrix at $t = 0$ ($R(0)$), provided the noise covariance matrix is known or can be estimated. The Unitary factor U may be thought of as a unitary matrix that simultaneously diagonalizes a set of covariance matrices considered at various time lags. A detailed analysis of SOBI algorithm can be found in (Belouchrani et al., 1997). Though SOBI has not been implemented in hardware before, (Huang et al., 2008; Shyu et al., 2008; Li and Lin, 2005 and Du and Qi, 2004) can be good references for literature on hardware implementation of other BSS algorithms.

3 DESIGN AND IMPLEMENTATION

3.1 Design Methodology

Fig 2 illustrates the basic flow of the SOBI Algorithm. As is evident, Whitening i.e. Singular Value Decomposition, Correlation i.e. determining the correlation matrices and Joint Diagonalization of the correlation matrices; comprise of the major part of the algorithm. Firstly, a SIMULINK model was developed and the results were compared to those obtained from the MATLAB code. The SIMULINK model was built in order to be able to perform Hardware Co-simulation, which is an intermediate stage between software and hardware implementation. This intermediate approach is expected to gauge the benefits of both software and hardware and thus could provide a better solution. This is based on the belief that it is not always prudent and economical to implement the entire system in hardware. Instead, implementing only those blocks which allow certain amount of parallelism and / or for which the computational

time is to be reduced, could turn out to be more economical and better solution.

The three approaches to develop a Co-simulation between SIMULINK/ MATLAB and XILINX ISE are as mentioned below:

- 1) Using System Generator
- 2) Using HDL Coder and EDA Simulator Link
- 3) Using EDA Simulator Link and a Black Box containing the hand coded VHDL code.

In the first two approaches, the VHDL code is automatically generated from a MATLAB code or a SIMULINK model. However, there are several restrictions on what all MATLAB functions can be directly mapped onto a VHDL code. In view of these limitations and after several failed attempts with the first two approaches, it was decided to hand code the VHDL code. Also, hand coded VHDL code offers the advantage that it can be optimized as per the need.

Thus, VHDL code for three of the most important blocks – Singular Value Decomposition, Correlation and Joint Diagonalization - of the SOBI model were written and simulation results were obtained for the same. The next step was to synthesize the blocks. The code for which simulation results were obtained was written using real data type, which is not synthesizable. Thus, the code for Correlation block was rewritten using Floating point representation and simulation results were obtained for the same. However, as the floating point package (Bishop, 2005), (that need to be used since floating point was not an inbuilt data type until VHDL 2008) integrated in VHDL 2008 is not yet officially supported by Xilinx XST13.4, several synthesis issues were encountered. Thus, the correlation Block was finally synthesized using signed number representation. Finally, the synthesis report was generated and the parameters were modified so as to optimize the performance.

3.2 Proposed Architecture for Correlation Block

The Figure 3 denoted below represents the process to determine a single Correlation matrix. n such processes may be run in parallel to determine the n correlation matrices at various time lags. However, running the processes in parallel would imply more hardware resources being used.

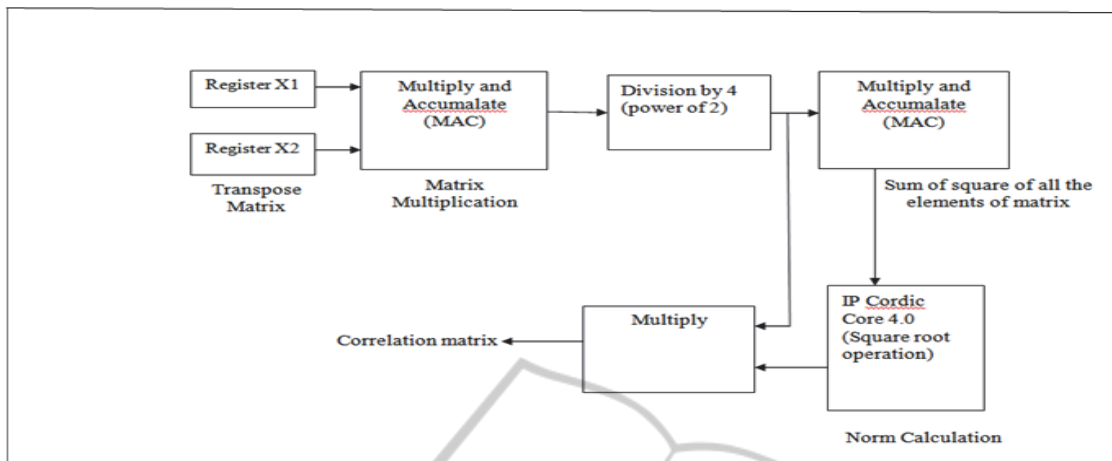


Figure 3: Proposed architecture for implementation of Correlation Block.

4 RESULTS

4.1 Simulation Results

As mentioned earlier, the simulation results for SVD block (using real data type), correlation Block (using real, floating point and signed numbers data type) and Joint Diagonalization block (using real and floating point data type) were obtained considering a 2 x 4 input matrix, that is, 2 channels and 4 data points. The parameter p which determines the number of correlation matrices to be considered, was set to 2. Several observations were made which are listed below.

If it is intended to write a synthesizable code, real data type should not be used. The use of Logic cores to implement mathematical functions such as square root, does introduce a bit of latency and thus some hand coded functions should be developed instead. Also, though it is easy to program in Floating Point it is certainly not a hardware Engineer's choice as it utilizes a lot of hardware resources.

Both the Joint Diagonalization and SVD block involved the calculation of eigen values and vectors. Based on the simulation results, it was concluded that the power method should be used only when the largest eigen value and the corresponding eigen vector is to be calculated. While it worked well in the Joint Diagonalization block, it didn't produce accurate results for the SVD block which involved calculation of eigen values and vectors of a 2 x 2 matrix. Thus, the Jacobi method should be used instead.

4.2 Synthesis Results

Using the signed integer data type, the synthesis of the correlation block was made possible and the synthesis report was generated. The mapping procedure failed due to the over utilization of IOBs (Bounded input output). However, the synthesis report generated does provide some insight into the synthesis of the code. The timing report shows a minimum delay of 12.795 ns which corresponds to a Maximum frequency of 78.155 Mhz. This is higher than the maximum frequency of 64 MHz achieved in (Huang et al., 2008). Although, in (Huang et al., 2008) the entire algorithm was implemented while in our case only a part of it is implemented. As observed by changing a few parameters, it may be concluded that there is a lot of scope for optimization.

5 CONCLUSIONS

Thus, the synthesis results obtained for the Correlation Block, do verify that the computation time could be reduced by implementing the SOBI algorithm in FPGA. Also, there is scope for a lot of optimization that can be done to achieve higher speed. Also, as was observed while working on the codes, SOBI does offer a lot of scope for parallelism and pipelining as there are a lot of matrix operations involved and thus it seems only wise to implement it in FPGA. Once, the major blocks of Correlation, Joint Diagonalization and Singular Value Decomposition are made synthesizable, it might be

interesting to perform Co-simulation between MATLAB - Xilinx and make a comparison between Software, Hardware and Hardware Co-simulation. Based on the results, it can be decided as to what actually to implement in FPGA. This way an economical use of Hardware resources can be made. In the near future, when the floating and fixed point packages are officially supported by Xilinx XST for synthesis purpose, the same work can be implemented using Fixed or Floating point representation, which unlike integers is a descent way of representing real life EEG data.

This work is the first initiative taken to implement SOBI to perform BSS in Real time and thus is just at a preliminary stage. The project provides a global view of the implementation, while considering the Correlation block in-depth. This work could be used to make a choice of the methods to implement various blocks, as an analysis of the methods for each block has been made in this project. A lot of work needs to be done further. However, the work does provide hope that SOBI could serve as a potential candidate for real time BSS. Thus, it could pave a way for on-line processing required in applications like Brain Computer Interface.

ACKNOWLEDGEMENTS

SIGMA Laboratory, ESPCI, Paris Tech
ISEP, Paris
Gerard Drefus, ESPCI, Paris
Yohei Tomita, SIGMA Lab, ESPCI, Paris
Parvaneh Adibpour, SIGMA Lab, ESPCI, Paris
Antoine Gaume, SIGMA Lab, ESPCI, Paris

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