

A Parity-based Error Control Method for Distributed Compressive Video Sensing

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Abstract: A novel framework called distributed compressive video sensing (DCVS), combining distributed video coding (DVC) and compressive sensing (CS), directly capture the raw video data as measurements with low-complexity and low-cost process. It meets the requirements of distributed system very well, because of its resource consumption shifting from encoder to decoder. Nevertheless, the issue of measurements transmission in bit error channel has not been considered yet in the previous work of DCVS. This paper improved the existing DCVS codec scheme by adding the quantization and inverse quantization process, and proposed a parity-based error control (PEC) method. This method is simple enough, and has high coding efficiency. The proposed method is shown to increase video recovery quality greatly under binary symmetric channel.

1 INTRODUCTION

In the framework of Wireless Media Sensor Network (WMSN) (Akyildiz et al., 2007), the sensor nodes must work under some resource constraints, such as lower computational capability and limited energy supply, so the problem of how to process the considerable video information efficiently has been brought into attention.

Compared with traditional compression standard like H.264/MPEG, distributed video coding (DVC) (Girod et al., 2005), which is developed from the principle of distributed source coding (DSC) (Wyner et al., 1976), was proposed to reduce the encoding complexity via shifting the complicated motion estimation work as the major encoding cost to decoder.

Another popular theory, compressive sensing (CS) (Candès and Wakin, 2008) also can shift the encoder burden to decoder, which has the similar structure to DVC. The CS theory, which combined sampling with compression, captures the abundant raw image information efficiently with a small amount of incoherent measurements at encoder, and recovers the image faithfully via linear programming at decoder. CS is particularly fit for the distributed systems because of the significant cost reduction of

data acquisition.

Motivated by the common principle of the two aforementioned theories, the framework of distributed compressive video sensing (DCVS) (Kang et al., 2009); (Do et al., 2009) was proposed. However, the previous researches just focus on the codec scheme without much concerning about compressed signal transmission problem. Based on the CS theory, the structure of compressed signal, which is composed of some incoherent measurements, differs a lot from the conventional source coding signal which is represented by the signal coefficients in frequency domain. Therefore, the transmission problem of CS signal in DCVS deserves our attention. There already has been some research on quantization of CS signal (Dai et al., 2009). And measurements rate allocation for DCVS (Chen et al., 2010) was also proposed to enhance the recovered video quality. Moreover, we also do some work on video quality evaluation for DCVS (Chen et al., 2012). Main work in this paper is displayed as follows: 1, provided a suitable quantization for measurements of DCVS; 2, proposed a parity-based error control method for DCVS; 3, employed the proposed method for quantized measurements to alleviate the affect of binary symmetric channel.

The organization of this paper proceeds as

follows. Section 2 gives the basic aspects of DVC and CS, section 3 describes the specific example of DCVS and proposed parity-based error control (PEC) method for DCVS, section 4 discusses the simulation results and section 5 is the conclusion and future directions of research.

2 RELATIVE WORKS

2.1 Distributed Video Coding (DVC)

In distributed source coding (DSC), assumed that W and S are two statistically dependent discrete signals, which are encoded independently but decoded jointly. Slepian-Wolf theorem (Wyner et al., 1976) asserted the achievable rate region for lossless coding is defined by $R_w \geq H(W/S)$, $R_s \geq H(S/W)$, and $R_w + R_s \geq H(W, S)$, where R_w and R_s are the encoding rates for W and S , respectively, $H(W/S)$ and $H(S/W)$ are the conditional entropy of W and S , respectively, and $H(W, S)$ is the joint entropy of W and S . Additionally, S is known as the side information (SI) of W .

In distributed video coding (DVC) (Girod et al., 2005), the kinds of frames in a group of pictures (GOP) are divided into Key frame and WZ frame (Wyner-Ziv frame). The Key frames are intra-coded an intra-decoded like I-frame in conventional video compression standards. And some information derived from Key frame is viewed as side information (SI) at decoding end. At encoder, without motion estimation, the compression of WZ frame is achieved as parity bits (also called Wyner-Ziv bits) by channel-encoding like turbo coding or LDPC coding. Decoder receives the parity bits of WZ frame viewed as W , and uses the SI S viewed as noisy version of W to perform channel decoding for reconstruction of WZ frame.

2.2 Compressive Sensing (CS)

In recent years, compressive sensing (CS) (Donoho, 2006); (Candès, 2006); (Candès and Tao, 2006) provides a theory about broadband analog signals sampling. The CS as a new research focus gives a novel set of theoretical framework about signal representation, signal sampling and signal reconstruction. It points out that, if the signal x is sparse in time domain or sparse in some transform basis Ψ , then we can employ global measurement instead of local sampling with sampling speed far below the Nyquist frequency, get measurements y less than original sampling number through the

measurement matrix Φ which is not coherent with sparse transform basis Ψ . After that, original high-dimensional signal x can be recovered accurately with appropriate reconstruction algorithm from low-dimensional measurements y . Unlike Nyquist sampling theory, the sampling rate is not dependent on bandwidth of signal, but on two basic criteria: sparsity and the restricted isometry property (RIP) (Candès and Tao, 2006). Theoretical framework of compressive sampling is shown in Figure 1.



Figure 1: Compressive sampling framework.

CS contains the following four steps based on the study of theory, shown as Figure 1.

- Assume that the original N -dimensional signal can be sparse on the basis Ψ ($N \times N$), then get the sparse signal θ . If the original signal is sparse already, skip this step.

$$x = \Psi\theta \quad (1)$$

- Devise the measurement matrix Φ ($M \times N$) to acquire measurements y , where $A = \Phi\Psi$ called the sensing matrix.

$$y = \Phi x = \Phi\Psi\theta = A\theta \quad (2)$$

- Solve the problem of minimum l_0 norm as follows known Φ , Ψ and y , and reconstruct θ from measurements y .

$$\hat{\theta} = \arg \min \|\theta\|_0 \text{ s.t. } A\theta = y \quad (3)$$

- Obtain the original signal \hat{x} using the inverse transform of basis Ψ .

$$\hat{x} = \Psi\hat{\theta} \quad (4)$$

Sparsity, measurement matrix and reconstruction algorithm in the above steps are three key parts of CS theory.

Sparse signal in compressive sampling is defined as follows: if a signal only has finite number of non-zero sample point (the number is K), and other sample point is zero or similar to zero, this signal is claimed as K -sparse and the sparsity is K . Ref (Baraniuk, 2007) shows that the original signal may be reconstructed accurately in large probability under the condition that the relation between measurements M and sparsity K should satisfies $M \geq K \cdot \log(N)$, in other words, the signal recovery quality will be affected quite if the measurements M is less than a certain number.

According to the above characteristics of compressive sensing, it has following advantages for video transmission: (1) The correlation of adjacent signal sampling points obtained by traditional method is robust, on the contrary, the redundancy of measurements observed by CS is in a very low state, it is in favor of large amount of data information processing like video transmission to avoid the waste of a lot of redundant information (Barakat et al., 2008); (2) The CS is suitable for distributed or portable terminal video transmission particularly due to resource consumption of computing and storage transferred from sender to receiver; (3) Because CS signal is unstructured presentation of image, and reconstruction algorithms leave far from the statistical radio channel interference constraints, so it possesses good characteristics of resistance to random channel errors.

3 IMPROVED DCVS SCHEME AND PROPOSED PEC METHOD

3.1 DCVS Codec Scheme

In the Kang's DCVS codec scheme (Kang et al., 2009) shown in Figure 2, a video sequence consists of several GOPs, where GOP consists of a key frame and some followed CS frames. At the encoder, each frame x_t , including Key frame and CS frame, is compressed via CS measurement process as:

$$y_t = \Phi x_t \quad (5)$$

where y_t is the measurement vector with size M_t , and Φ is the scrambled block Hadamard ensemble (SBHE) matrix described in (Do et al., 2008). The sparse basis matrix Ψ used in the scheme is DWT. The significant difference between Key frame and CS frame is that the measurement vector size M_t of Key frame should be larger than that of CS frame, to guarantee the recovery video quality at decoder. The measurement rate for each frame can be defined as:

$$MR_t = M_t / N \quad (6)$$

where N is the size of video frame.

At the decoder, each Key frame x_t is reconstructed via Gradient projection for sparse reconstruction algorithm (GPSR) (Figueiredo et al., 2007), which solve the convex unconstrained optimization problem described as:

$$\min_{\theta_t} \frac{1}{2} \|y_t - A\theta_t\|_2^2 + \tau \|\theta_t\|_1 \quad (7)$$

where y_t is a vector with size M_t , $y_t = \Phi x_t$, $A = \Phi \Psi$ is a $M_t \times N$ matrix, and τ is a non-negative parameter. GPSR is essentially a gradient projection algorithm applied to a quadratic programming formulation of Eq.(7), in which the search path for each iteration is acquired by projecting the negative-gradient direction onto the feasible set, and the default initial solution for θ_t is a zero vector.

Before reconstructing a CS frame x_t , the decoder will generate its SI S_t by motion-compensated interpolation from the reconstructed neighboring Key frames first, which can be viewed as a noisy version of x_t . In the same scene, the successive frames should have a certain similarity. Hence, the SI derived from the neighboring Key frame, should be similar to this CS frame. So, each CS frame is reconstructed via the modified GPSR with the initial solution set by SI. To get a good quality for CS frame, it is required to have a good initialization derived from Key frame which is served as reference frame. That is why the measurement vector size M_t of Key frame should be much larger than that of CS frame.

3.2 Quantization for Measurements

The measurements of DCVS frame is discrete in time but continuous in amplitude. Hence, the quantization is the indispensable part of codec scheme. In order to improve the above-mentioned DCVS codec scheme, the uniform quantization and inverse quantization are added to the system for digital transmission. Scale quantization is employed on account of complexity of encoder. Quantizing process is described as:

$$z_t = \frac{\text{round}(2^{Q-1} y_t)}{2^{Q-1}} \quad (8)$$

where y_t is the measurements vector of a frame, z_t is the quantized measurements vector, Q bits refers to the number of bits per measurement, also implies the quantitative accuracy, and $2^{(Q-1)}$ refers to quantization step. Define the quantization noise as:

$$e = z_t - y_t \quad (9)$$

In addition, we need one bit to represent the sign of measurement. Then we can get the number of bits ratio per frame of DCVS, shown as:

$$R_t = (Q + 1) \times MR_t \times N \quad (10)$$

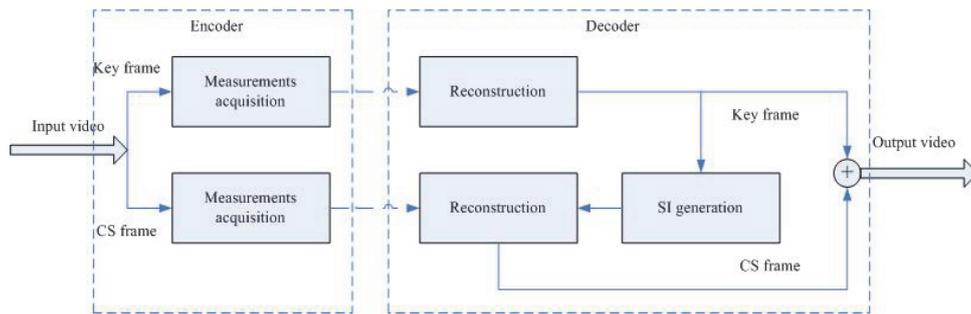


Figure 2: DCVS codec scheme.

where R_t is the number of bits ratio per frame, MR_t is the measurement rate for each frame, and N is the size of a frame.

Currently, we only know the value of Q is just the trade-off between reconstructed video quality and compression ratio, and how to quantize the measurements more efficiently, which will be left for our future work.

3.3 PEC Method for DCVS

The dequantized measurements y_t constitute a random and incoherent combination of the original frame pixel, which has been already studied in (Chen et al., 2012). That is also to say, no individual measurement is more important than any other measurement for frame reconstruction. This means that, the number of correctly received measurements is the main factor in determining the quality of video recovery. For this characteristic of measurements, discarding a small amount of measurement will not cause quality decline greatly, which will be shown in next section. There will be badly impact on quality if the measurements containing some error bit are used for the reconstruction.

With the limitation of channel resource and energy constraint, traditional ARQ (Automatic Repeat re-Quest) error control scheme can't be adopted. And other FEC (Forward Error Correction) methods such as LDPC, Turbo coding are also inapplicable to the DCVS due to the additional encoding complexity, even though the FEC scheme shows stronger error correction capabilities. For the above reasons, we proposed a simple parity-based error control (PEC) method for resistance of random channel error in DCVS. It is realized by using an even parity bit added after each measurement at encoder. If the parity check is failed, than dropped this measurement immediately at receiver or at an intermediate node. This method has the following two benefits: 1, it is simple enough to adapt to the requirements in the codec; 2, parity-based coding

efficiency is high extremely with low coding redundancy. The coding efficiency of a frame can be defined as:

$$P = \frac{(Q+1) \times MR_t \times N}{(Q+1) \times MR_t \times N + MR_t \times N} \quad (11)$$

where $MR_t \times N$ presents the number of parity bits.

Improved DCVS system is shown in Figure 3.

4 SIMULATIONS RESULTS

In this paper, we choose the 'coastguard' CIF video sequence with frame size 352×288 as the test video, and GOP size is set to 3. The MR_t of Key frame equals to 70%, and MR_t of CS is 30%. In the CS measurement process, SBHE matrix is used as sensing matrix Φ , and DWT is employed as sparse basis matrix Ψ . GPSR algorithm is used for video reconstruction at decoder. Quantitative accuracy Q is set to 8 bit. Random channel error is simulated by Binary Symmetric Channel (BSC). Ultimately, we choose conventional Peak Signal to Noise Ratio (PSNR) to evaluate the quality of recovery video.

Figure 4 shows the first Key frame of video sequence in DCVS. (a) is the original frame, (b) is the recovery frame without channel error. (c) is the recovery frame which employ our PEC method under channel bit error rate (BER) 10^{-2} . (d) is the recovery frame without any error control method under BER 10^{-2} .

We pick up 1-7 frames in the video sequence to present the video reconstruction quality under channel BER $10^{-2}, 10^{-3}, 10^{-4}$, and the ideal channel without error, which is shown in Figure 5 and Figure 6. 1st, 4th, 7th frame are Key frames and 2nd, 3rd, 5th, 6th frame are CS frames. Figure 5 shows the quality with our proposed method, and Figure 6 shows the quality without error control. Figure 7 shows PSNR of recovery the 4th frame which is Key

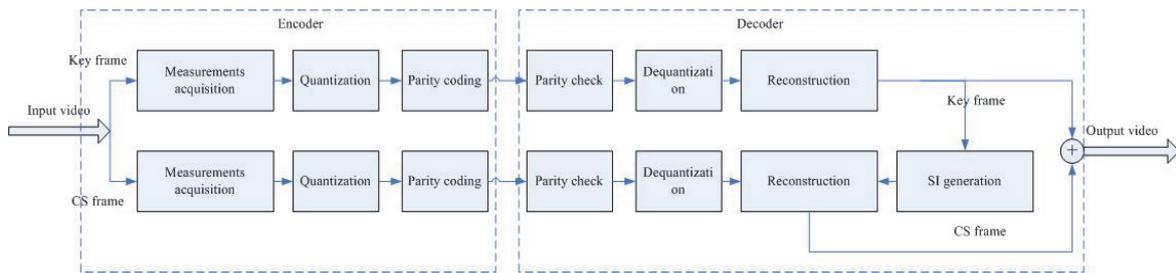


Figure 3: Improved DCVS codec scheme.



Figure 4: 1st Key frame of test video sequence: (a) original frame; (b) the recovery frame without channel error; (c) the recovery frame under 10^{-2} BER with our PEC method; (d) the recovery frame under 10^{-2} BER without any error control method.

frame under the different BER and Figure 8 shows PSNR of recovery the 3rd frame which is CS frame under the different BER. For all reasonable BER, our proposed method achieved the better performance. Figure 9 shows that under different BER, the true measurement ratio of Key frame and CS frame in fact are received at decoder end.

5 CONCLUSIONS AND FUTURE WORKS

Nowadays compressive sensing is on its growing stage and we still have long way to go before putting it into practice. How to convert analog information into digital compressive information (Analog-Information Converter) by the method of compressive sensing is a tough issue. But compressive sensing system has already been proved to be feasible technically, and we firmly believe that it shall be another important way for information acquisition in the near future. In this paper, we described a whole framework of DCVS, proposed a parity-based error control method for CS measurement of DCVS frame. Its good performance has been shown in simulation results. Next, in DCVS, we will focus on the measurement quantization and entropy coding, alterable measurement rate allocation, and video recovery quality evaluation. These also attracted a lot of attentions of many researchers in this field.

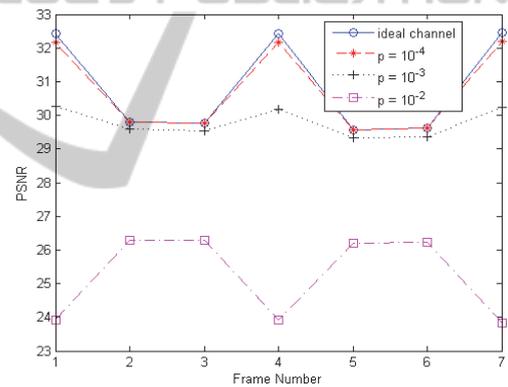


Figure 5: Recovery quality of 1st-7th frame in test video under different BER with our PEC method.

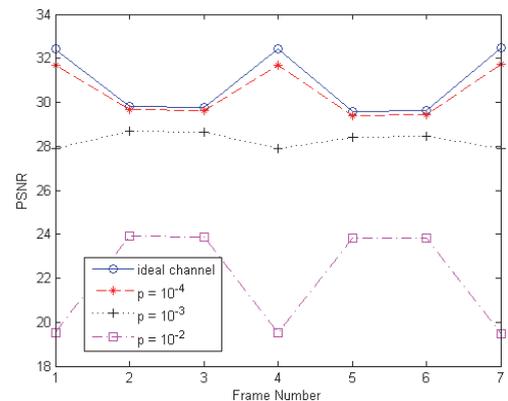


Figure 6: Recovery quality of 1st-7th frame in test video under different BER without error control method.

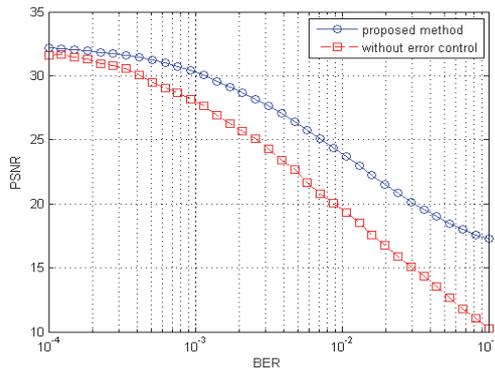


Figure 7: PSNR of recovery the 4th frame (Key frame) under the different BER.

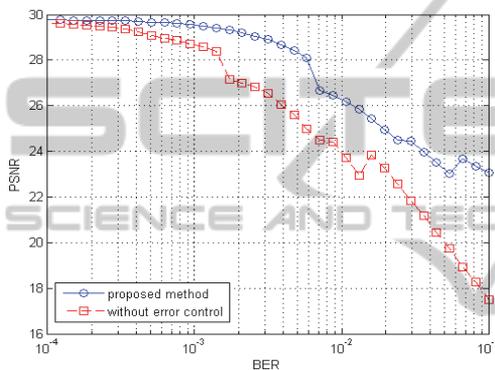


Figure 8: PSNR of recovery the 3rd frame (CS frame) under the different BER.

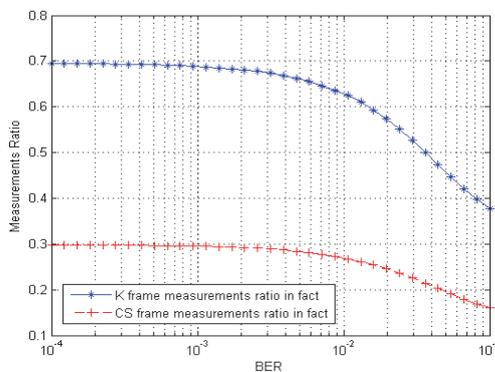


Figure 9: the true measurement ratio of Key frame and CS frame in fact under different BER.

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