

# Limitations of Super Resolution Image Reconstruction and How to Overcome them for a Single Image

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**Abstract:** Super resolution image reconstruction (SRR) is a typical super resolution (SR) technology that has been researched with varying results. The SRR algorithm was initially proposed for still images. It uses many low-resolution images to reconstruct a high-resolution image. Unfortunately, in practice, we rarely have a sufficient number of low-resolution images for SRR to work. Usually, there is only one (or a few) blurry images. On the other hand, there is a need to improve blurry images in applications ranging from security and photo restoration to zooming functions and countless other examples related to the printing industry. Recently, SRR was extended to video sequences that have many similar frames that can be used as low-resolution images to reconstruct high-resolution frames. In normal SRR, one reconstructs a high-resolution image from low-resolution images sampled from one high-resolution image, but in the video application, the low-resolution video frames are not taken from higher resolution ones. This paper proposes a novel resolution improvement method that works without such a high-resolution image. Its algorithm is simple and can be applied to a single image and real-time video systems.

## 1 INTRODUCTION

Methods of creating high-resolution images from low-resolution images have been researched for many years. These image restoration methods were initially applied to still pictures. They were later extended in scope and are now called super resolution (SR) (Sung et al., 2003). One SR technique is super resolution image reconstruction (SRR) (Farsiu et al., 2004) (Adam et al., 2010) (Katsaggelos et al., 2007) (Panda et al., 2011). SRR is at present the only SR method among the many proposed to be incorporated in commercial products (Matsumoto and Ida, 2008) (Matsumoto and Ida, 2010) (Matsumoto and Ida, 2010) (Toshiba). However, the practical limitations of SRR have not been discussed especially in regard to real-time applications.

Display devices, such as LCDs, and ink jet printers have advanced to such an extent that their resolutions exceed those of pictures taken with film cameras. Moreover, although most photographs are taken with digital cameras these days, they are prone to being blurred because of focusing mistakes or the camera being shaken while in operation. SRR is not a good way to improve the resolution of individual pho-

tographs since it requires many low-resolution images; typically, only one blurry photograph is available. In contrast, video would seem to be a very good application for SRR, since video consists of numerous frames and adjacent frames that look similar. Not surprisingly, therefore, many papers have been published on the subject citeSR:Face (Katsaggelos et al., 2007) (Protter et al., 2009). However, the methods proposed so far are complex. Recently, SRR functions with self congruency characteristics in a frame have been incorporated in HDTV sets and BluRay players (Matsumoto and Ida, 2008) (Matsumoto and Ida, 2010). However, before we can evaluate the efficacy of SRR for these devices, we must bear in mind that video frames have different characteristics than those of still images taken with still cameras.

A common form of video content is TV broadcasting. Analogue broadcasting has been around for more than 60 years, but it is being replaced with digital HDTV broadcasting in many countries. The initial cost of digital HDTV broadcasting is high for most broadcasting companies. SRR for video would be very useful if it could improve the resolution of analogue video that has been converted into HDTV; broadcasters could continue showing analogue pro-

ductions and thereby reduce their costs. Viewers who own HDTVs with SRR functions for converting analogue video into HDTV would be able to view potentially all their programming at an HDTV level of resolution. For manufacturers, this would mean that HDTV receivers with SRR could be sold all over the world. In fact, HDTV sets with SRR functions are now on the market, and SRR has been deemed a practical technology (Toshiba). However, despite there having been many studies, no HDTVs equipped with SRR functions for converting analogue broadcasting have been developed. Recently, it was proven that the resolution of HDTV with SRR is inferior to the HDTV without SRR (Gohshi and Echizen, 2013). This suggests that SRR cannot improve the resolution of general TV content.

SRR has another issue. To improve resolution of a still image, we need many low-resolution images with different phases. This presents a problem if there is only one low-resolution image. Although some technologies can improve resolution with a single image (Glasner et al., 2009)(Panda et al., 2011), they need iterations and the processing time depends on the characteristics of the image. In practice, the effectiveness of SRR technologies should not be image dependent.

This paper is organized as follows. First, the limitations of SRR are discussed in the frequency domain. Second, a non-linear signal processing (NLSP) method that is free of the issues of SRR is introduced. The basic idea behind this method was recently described (Gohshi, 2012). However, the theoretical background of NLSP in the frequency domain was not discussed in detail. This paper proposes another non-linear function that gives better results and discusses the algorithm of NLSP in the frequency domain. As just one image simulation result is not sufficient for practical applications, we give several simulation results to prove the validity of the method. In the same way it is applied to still images, the NLSP method can improve resolution of video sequences using a single frame at a time, which is something that SRR cannot do.

## 2 ISSUES OF SRR IN FREQUENCY DOMAIN

SRR is usually discussed with regard to an original image and the reconstructed image. Image quality is a subjective assessment, and it is not easy to tell the difference in image quality between similar images printed on sheets of paper or in pdf files. Image quality can, however, be discussed in an objective way by referring to spectra in the frequency domain. To see

how this is done, let us consider Figure 1. One of LRIs shown in Figure 2 is created from Figure 1 by subsampling. Figure 3 is the corresponding SRR image generated from 16 LRIs and 100 iterations (Farsiu et al., 2004). The sizes of the LRIs in this case were a quarter that of the original HRI. Such a still image is the best condition of SRR signal processing since the still image has sufficient sharp edges for SRR. More than 16 LRIs would be necessary to get a comparable result for video since motion blur would smear out such sharp edges (Gohshi, 2007). Although Figure 1 and Figure 3 look the same, their two-dimensional fast Fourier transforms (FFTs) are different (Figure 4 and Figure 5). In Figure 5 showing the FFT of the SRR, there is a rectangular null area without any frequency components and the same repeated frequency characteristics. This sort of phenomenon is due to sub-sampling and the null area does not exist if SRR can reconstruct the HRI perfectly.



Figure 1: Original image.



Figure 2: LRI.



Figure 3: SRR image.

Figure 6 shows the two-dimensional FFT of one of the quarter-size LRIs from Figure 2. All the LRIs have the same null areas in the frequency domain due to the sampling theory. The white rectangle in Figure 6 is the Nyquist frequency (vertical and horizontal) of

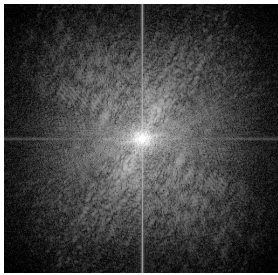


Figure 4: 2D FFT of Fig.1.

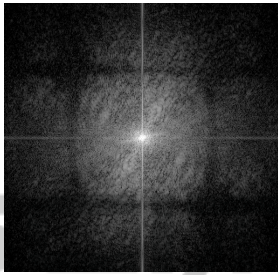


Figure 5: 2D FFT of Fig. 3.

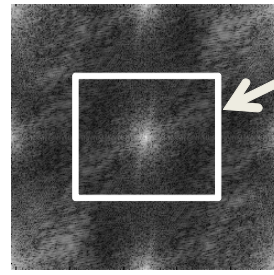
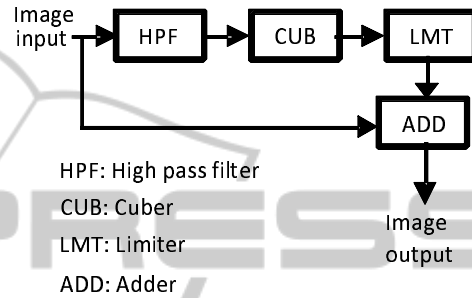


Figure 6: 2D FFT of one of 16 LRIs.

the LRIs, and it is clear that the same frequency spectra spread outside of the white rectangle. Compared with Figure 5 and Figure 6, both of the vertical and horizontal Nyquist frequencies are half those shown in Figure 4. There are repeated frequency spectra in Figure 5, and the repetition cycle is the same value in cycles as the frequency of the white rectangle shown in Figure 6. Although Figure 3 is reconstructed from 16 LRIs, Figure 5 has the same shape cycle as Figure 6. This means that SRR cannot reconstruct the original image completely, and the SRR result is affected by the size of the LRIs. Figure 3 was reconstructed from 16 LRIs over 100 iterations. It was made under the ideal conditions for SRR but it is not the same as the original image. The rectangular null area shown in Figure 5 appears at any factor of enlargement. The null areas in Figure 5 are exactly the same as the Nyquist frequencies of LRIs. The difference between the two-dimensional frequency characteristics of Figure 4 and Figure 5 causes the difference in resolution between in Figure 1 and Figure 3.

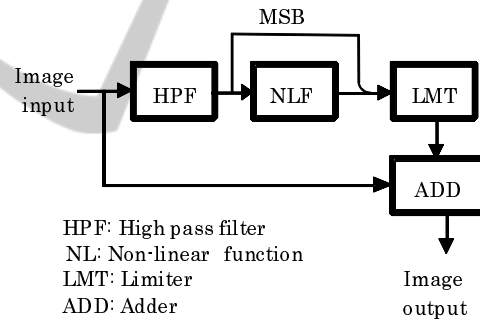
### 3 NON-LINEAR SIGNAL PROCESSING METHOD

The non-linear signal processing (NLSP) algorithm is simple (Figure 7). The basic idea is similar to Unsharp Mask or Enhancer (Schreiber, 1970)(Lee, 1980)(Pratt, 2001). The difference between the proposed method and Enhancer is the cubic function in Figure 7. Enhancer detects edges with a high pass filter (HPF) and a limiter (LMT) restricts the level



HPF: High pass filter  
 CUB: Cuber  
 LMT: Limiter  
 ADD: Adder

Figure 7: NLSP algorithm.



HPF: High pass filter  
 NL: Non-linear function  
 LMT: Limiter  
 ADD: Adder  
 MSB: Most significant bit (sign)

Figure 8: New NLSP algorithm.

of edges so as not to emphasize noise in the images. However, Enhancer cannot create frequency elements that the input image does not have. The proposed method uses a non-linear cubic function (CUB). CUB can generate higher frequency elements that the input image does not have as follows.

In Figure 7, edges are detected with the HPF and are added to the input image. It uses  $y = x^3$  as the non-linear function.

In Figure 7 edges are detected with HPF and are added to the input image. It uses  $y = x^3$  as the non-linear function. However,  $y = x^3$  creates three times higher frequency elements than the original frequency elements. The output of the high pass filter has plus and minus elements. Although  $y = x^3$  can hold positive and negative values, it may create unnecessarily high frequency elements. There is no feedback



Figure 9: NLSP image.

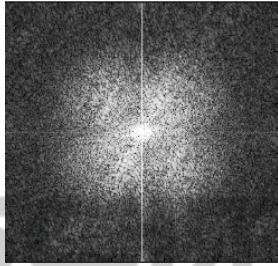
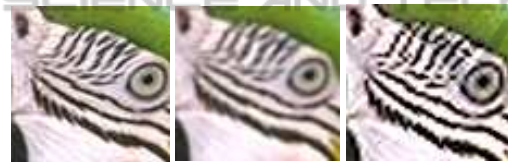


Figure 10: 2D FFT of Fig. 9.



(a) Original (b) RSR (c) NLSP

Figure 11: Comparison.

loop in Figure 7, which means that the NLSP is just straightforward signal processing and iterations are not necessary. NLSP uses just one LRI for the input. The image is input at the left top and is enlarged with a linear digital filter such as a Lanczos filter or bicubic filter. The enlarged image is distributed to the high pass filter (HPF) and the adder (ADD). The HPF detects the edges in the image and the edges are cubed. The cubed edges can create high-frequency elements that the input image does not have. It is well known that an image expanded by a Fourier series consists of  $\sin$  and  $\cos$  functions. Edges are represented with  $\sin n\omega_0$  and  $\cos n\omega_0$  functions. Here,  $\omega_0 = 2\pi f_s : f_s$  is the sampling frequency, and  $n$  is an integer number ( $n = 0, \pm 1, \pm 2, \dots$ ). The edge cuber (CUB) generates  $\sin^3 n\omega_0$  and  $\cos^3 n\omega_0$  from  $\sin n\omega_0$  and  $\cos n\omega_0$ .  $\sin^3 n\omega_0$  and  $\cos^3 n\omega_0$  generate  $\sin 3n\omega_0$  and  $\cos 3n\omega_0$ . This means three times higher frequency elements are generated and these high-frequency elements are edges that the original image does not have. The edges are added to the input image by ADD, and the resulting high-resolution image is output. A new algorithm shown in Figure 8 is proposed in this paper. The output of HPF is the edge information that has

signs, which means plus or minus for each pixel. After the HPF, the edges are processed with a non-linear function (NLF). If an even function such as  $x^2$  is applied, the sign information, plus or minus, is lost. The most significant bit (MSB) is separated from the edge information before NLF and restored to them after NLF. Using this method, we can use even non-linear functions. This method gives much more flexibility than the previous algorithm shown in 7. A simple non-linear function  $y = x^2$  is used in this paper. Generally, non-linear functions can generate harmonics that can create higher frequency elements, which the original image does not have. NLSP with other non-linear functions should also be able to create high-frequency elements. Here, we propose  $y = x^2$  for plus edges and  $y = -x^2$  for minus edges. They create two times higher frequency elements and are for enlarging images twice horizontally and vertically, such as in the conversion from HDTV to 4K TV. The processed image is shown in Figure 9. In this process, just one LRI shown in Figure 2 is the input image. In spite of the simple signal processing, the resolution is not worse than that of Figure 1 and Figure 3. Figure 10 shows the two-dimensional FFT result of Figure 9. Figure 10 does not have the null in-band areas shown in Figure 5, and it means that the NLSP does not generate null areas. Although the size of the input image is just a quarter that of the output image shown in Figure 1, NLSP can create the higher frequency elements beyond the Nyquist frequency of the input image. Figure 11 shows enlarged parts of the original image, SRR image, and the NLSP image. They are enlarged images and help to understand the resolution difference of (b)SRR and (c)NLSP.

Three other simulation results are shown from Figure 12 to Figure 29. Each simulation result shows the original image (512x512), the quarter size (256x256), enlarged and NLSP processed image (512x512) and their two-dimensional FFT results. Figure 17, Figure 23, and Figure 29 show two-dimensional FFT results of NLSP processed results. These simulations show that NLSP produces good results even with enlarged images. There are no null areas in the frequency domain characteristics. This means NLSP does not have the issues that SRR has.

#### 4 COMPARISON OF NLSP WITH SRR

Figure 30 illustrates the signal processing of SRR. The top and bottom images in Figure 30 are those of Figure 1 and Figure 3. It is necessary to create 16 LRIs and iterate the procedure 100 times. The





Figure 12: (512X512).



Figure 13: (256X256.)

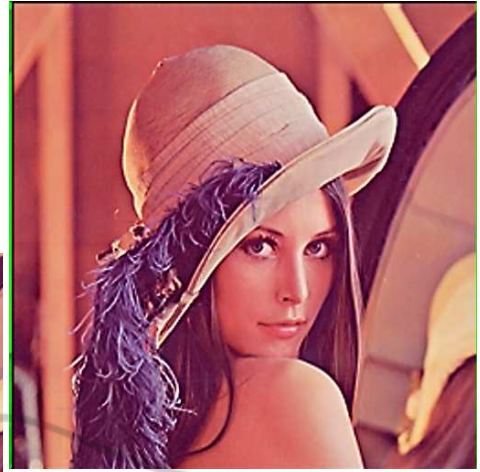


Figure 14: Lenna (512x512 NLSP image processed from Fig. 13).

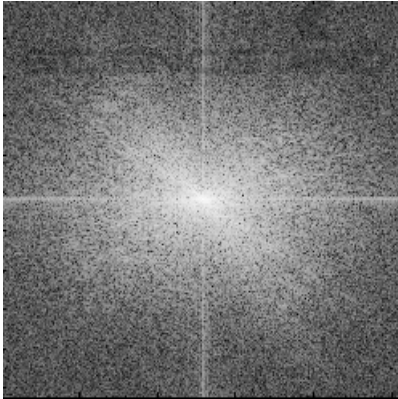


Figure 15: 2D FFT of Fig. 12.

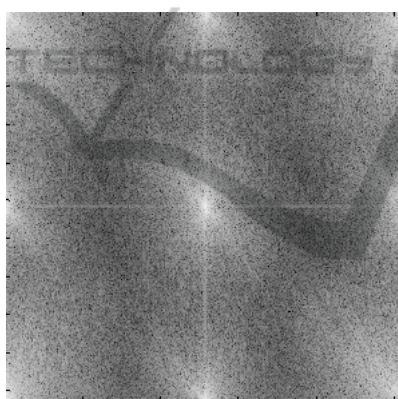


Figure 16: 2D FFT result of Fig.13.

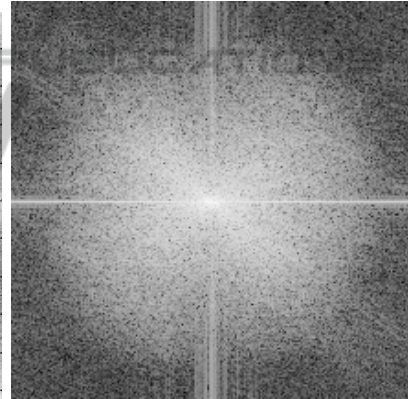


Figure 17: 2D FFT of Fig. 14.



Figure 18: (512X512).



Figure 19: (256X256).

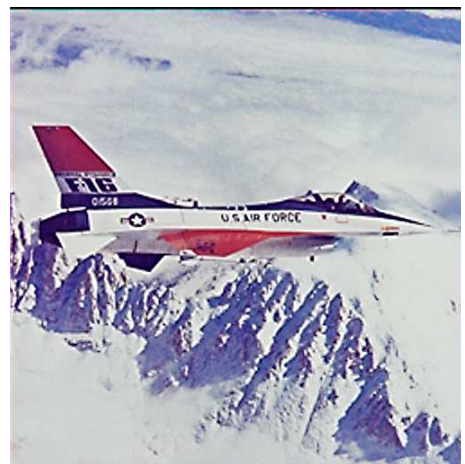


Figure 20: (512x512 NLSP image processed from Fig. 19).



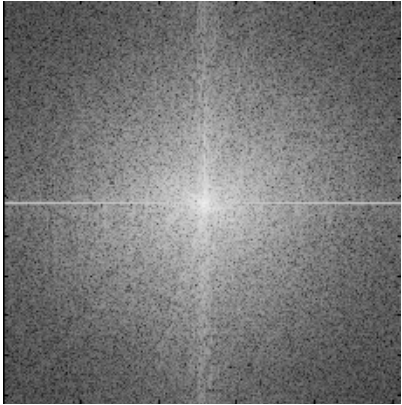


Figure 21: 2D FFT of Fig. 18.

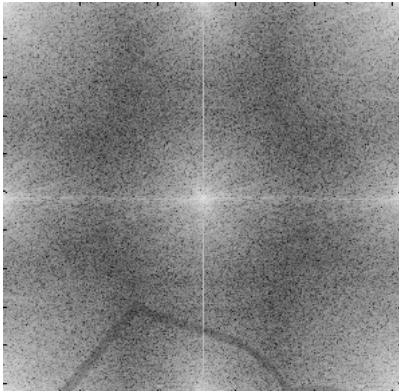


Figure 22: 2D FFT of Fig. 19.

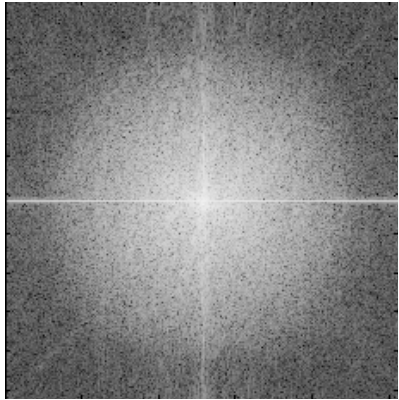


Figure 23: 2D FFT of Fig. 20.

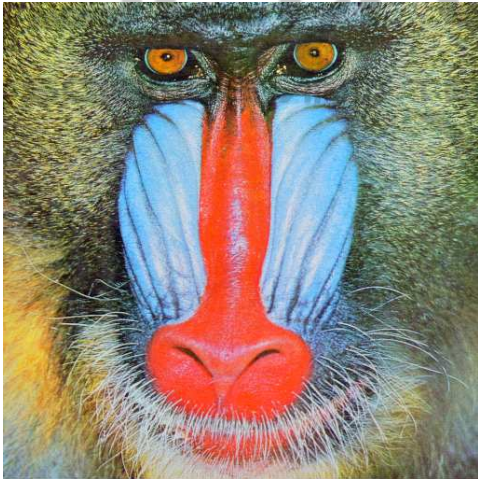


Figure 24: (512X512).



Figure 25: (256X256).

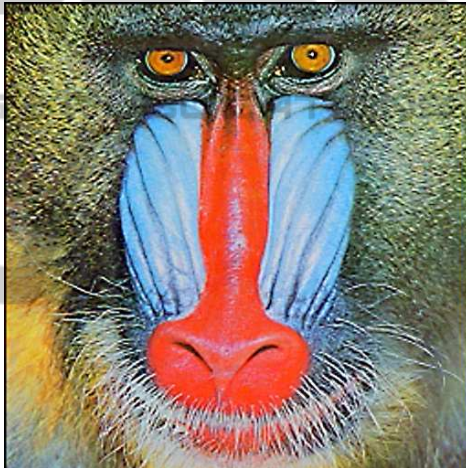


Figure 26: (512x512 NLSP image processed from Fig. 25).

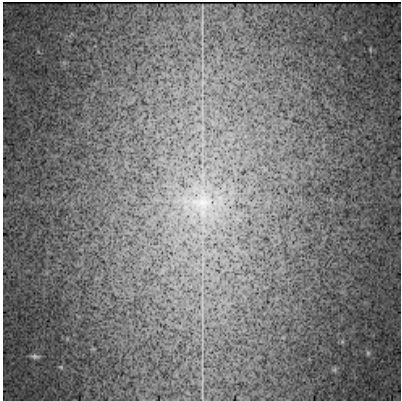


Figure 27: 2D FFT of Fig. 24.

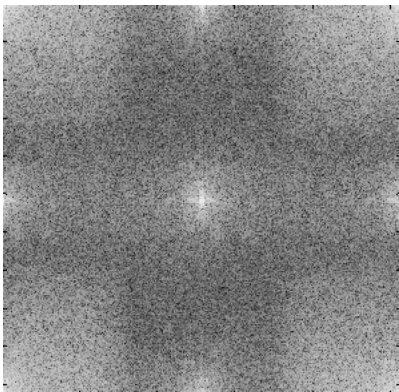


Figure 28: 2D FFT of Fig. 25.

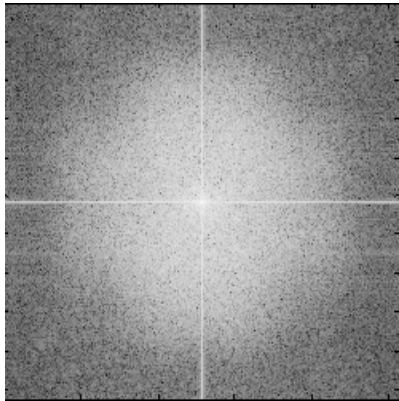


Figure 29: 2D FFT of Fig. 26.

16 LRIs contain the same amount of information as four original images, so the amount of information in the 16 LRIs is four times the original image. The reconstructed HRI image is stored in the frame memories. SRR thus uses five times the memory needed to store the original image. Moreover, 100 iterations are needed to create the SRR image. This means SRR consumes a lot of resources in reconstructing the image and its resolution is still not the same as the original image because of the null in-band frequency shown in Figure 4 and Figure 5.

On the other hand, the NLSP signal processing is very simple: just straightforward signal processing and no feedback processing, as shown in Figure 8. Moreover, NLSP needs only one quarter-size LRI. The HPF part is just a digital filter in the frame, the NLF part can be replaced by a look up table, and the ADD part is very simple, which all means NLSP has negligible frame delay when it is applied to video. It is not difficult to embody a real-time NLSP method in an inexpensive FPGA. Although a single frame memory type of SRR has been proposed for TV (Matsumoto and Ida, 2008)(Matsumoto and Ida, 2010) and there are HDTV sets equipped with it, the resolution of HDTV sets with it is inferior to the HDTV sets without it. The simulation results presented in this paper show that SRR cannot give sufficient resolution for enlarged images even if it is used under the ideal condition, which means one high-resolution image is reconstructed from all of the LRIs. In the simulation results, the size of the LRIs was a quarter that of the reconstructed image, which is the same ratio as the image conversion from HDTV to 4K TV, and 16 LRIs were necessary to create one HRI from a still image. Hence, it seems that an SSR technique would need 16 HDTV frames to convert HDTV into 4K TV. Besides that, SRR faces other difficulties with motion vector detection, motion blur, etc.

## 5 CONCLUSIONS

SRR is a useful tool only as long as the LRIs have aliasing in them. That is, SRR can remove aliasing and create beautiful images, but it is useless if the LRIs do not have aliasing in them. This means SRR will not work if all we have is a single low-resolution image. Moreover, SRR only works for certain kinds of video sequences such as infrared-ray video sequences with block noise and does not work for general video TV and BluRay content. The problem is that most video sequences do not have aliasing, except for interlaced aliasing or block noise, and SRR cannot create higher frequency elements than what

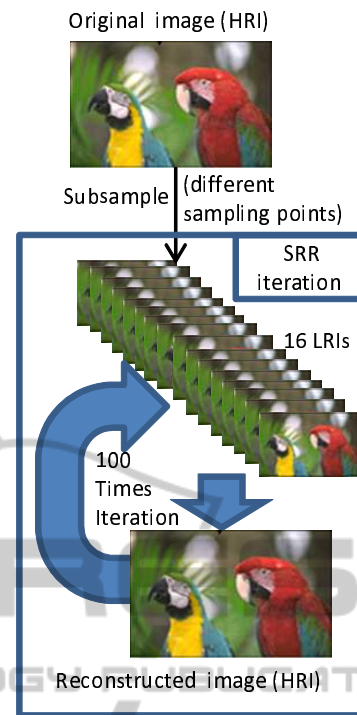


Figure 30: SRR algorithm.

are in the original HRI. This means it is very difficult to find video sequences taken with commercial video cameras that would benefit from SRR. Although SRR has been widely researched and has been touted as a means of improving resolution for HDTV content, its ability to improve video under practical circumstances turns out to be very limited.

The new NLSP method was compared with SRR, and it was found to have better frequency characteristics than those of SRR. NLSP can improve the resolution of a single low-resolution image and can create frequency elements higher than the Nyquist frequency of the original image. The four simulation results and their frequency characteristics presented in this paper prove that NLSP can create frequency elements higher than the Nyquist frequency of the original image.

The complexity and processing loads of NLSP and SRR were also compared, and NLSP was found to be light enough to be embodied in an FPGA. This means it is possible to design a real-time NLSP device for a real-time video system. There are many potential applications of NLSP including broadcasting, cinema, security and medical fields. Two-dimensional FFTs show that the resolution of NLSP is better than that of SRR. However, subjective assessments with NLSP and SRR with HDTV or 4K TV will have to be made in the future. Several SR ideas have been proposed for still images, and signal processing of



still images is much more flexible in the sense that real-time signal processing is not required. Thus, a comparison of SR and NLSP for still images should also be done. Further analysis is necessary before this method can be implemented in an FPGA. An analysis of the high-frequency components generated by the non-linear function used in the proposed method and the original high-resolution image should also be conducted.

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