

# Semantic Relatedness with Variable Ontology Density

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**Keywords:** Semantic Relatedness, Wikipedia Categories, Ontological Entities, Taxonomical Density.

**Abstract:** In a previous work, we proposed a semantic relatedness measure between scientific concepts, using Wikipedia categories network as an ontology, based on the length of the category path. After observing substantial differences in the arc density of the categories network, across the whole graph, it was concluded that these irregularities in the ontology density may lead to substantial errors in the computation of the semantic relatedness measure. Now we attempt to correct for this bias and improve this measure by adding the notion of ontology density and proposing a new semantic relatedness measure. The proposed measure computes a weighed length of the category path between two concepts in the ontology graph, assigning a different weight to each arc of the path, depending on the ontology density in its region. This procedure has been extended to measure semantic relatedness between entities, an entity being defined as a set of concepts.

## 1 INTRODUCTION

The *semantic relatedness* between two concepts indicates the degree in which these concepts are related in a conceptual network, by computing not only their semantic similarity but actually any possible semantic relationship between them (Ponzetto and Strube, 2007) (Gracia and Mena, 2008).

Computational semantic relationship techniques can be placed into one of two categories:

- Distributional measures that rely on unstructured data, such as large sets. The underlying assumption is that if similar words appear in similar contexts, then they should have similar meanings.
- Measures based on structured databases, such as taxonomies or ontologies, where semantic relationships are captured.

This work focuses on the second relationship measuring category, and uses Wikipedia page categories as a taxonomy.

The proposed measure considers not merely the number of arcs in the graph between the nodes that represent each concept, but also their relationship in the taxonomy. In our work we used the English version of Wikipedia<sup>1</sup>, based on which we analyzed relationships between concepts by building paths from start to destination nodes in the category network.

<sup>1</sup><http://en.wikipedia.org>

This procedure has been extended to measure semantic relatedness between entities, an entity being defined as a set of properties, i.e. concepts.

Since the Wikipedia ontology is in constant development, it was observed that some regions are far more developed than others. In this paper we propose to add to our previously developed measure of semantic relatedness (Medina et al., 2012) the notion of density, as a function of the number of incoming and outgoing links to/from a node in the conceptual graph. This means that the semantic relatedness between concepts needs to be inversely weighed by the density of the region of the path between concepts. We will propose a technique to compute the density of this region.

The remaining sections of this document are organized as follows: in Section 2 we describe related work in this area; Section 3 presents the proposed measure of semantic relatedness with the inverse density ponderation and in section 4 are presented the results obtained after applying this measure to a set of entities. Finally, in Section 5 we draw the main conclusions and identify opportunities for future work.

## 2 RELATED WORK

Given two words or expressions represented in a taxonomy, the computation of the semantic relatedness

between these two objects may be transformed into the evaluation of their conceptual distance in the conceptual space generated by a taxonomy (Jiang and Conrath, 1997), being that each object is represented by a node in the resulting graph.

Semantic relatedness measures in hierarchical taxonomies can be categorized into three types (Slimani et al., 2006):

1. **Information Content or Node-based:** evaluation of the information content of a concept represented by a node such as described in (Resnik, 1999). The semantic relatedness between two concepts reflects the amount of shared information between them, generally in the form of their least common subsumer (LCS).
2. **Path or Edge-based:** evaluation of the distance that separates concepts by measuring the length of the edge-path between them (Wu and Palmer, 1994) (Rada et al., 1989). A weight is assigned to each edge, being that the weight computation must reflect some of the graph properties (network density, node depth, link strength, etc.) (Jiang and Conrath, 1997)
3. **Hybrid:** a combination of the former two (Jiang and Conrath, 1997) (Leacock and Chodorow, 1998).

Lexical databases, such as WordNet, have been explored as knowledge bases to measure the semantic similarity between words or expressions. However, WordNet provides generic definitions and a somewhat rigid categorization that does not reflect the intuitive semantic meaning that a human might assign to a concept.

In this paper we use the english version of the Wikipedia<sup>2</sup>, a web-based encyclopedia which has approximately 4 million articles edited and reviewed by volunteers. The contributors are asked to assign these articles to one or more categories: Wikipedia may be thus viewed as either a folksonomy (Nastase and Strube, 2008) or a Collective Knowledge Base (Zesch et al., 2008), where human knowledge and human intuition on semantic relationships emerges in the form of a category network. It is then natural that this web-resource has been increasingly explored as a conceptual feature space, such that articles and categories are represented as nodes in the Wikipedia graph.

Techniques such Explicit Semantic Analysis (ESA) (Gabrilovich and Markovitch, 2007) represent texts in the high-dimensional concept space of Wikipedia as weighted vectors. A textual fragment is thus considered as a weighted mixture of a predetermined set of "natural" concepts. Wikipedia Link-

<sup>2</sup><http://en.wikipedia.org>

based Measure (WLM), first described in (Milne and Witten, 2008), uses its hyperlink structure, rather than the category hierarchy or textual content to compute semantic relatedness. In (Gouws et al., 2010) semantic relatedness is computed by spreading activation energy over the aforementioned hyperlink structure.

Measurement of semantic similarity between concept sets can provide particular value for tasks concerning the semantics of entities (Liu and Birnbaum, 2007). An entity may represent, for instance, (1) an author, by means of his/her research interests, (2) a publication, such as a scientific journal, by means of its main topics, (3) a conference, by means of its submission topics. In Information Retrieval, the similarity between documents is generally estimated by means of their Vector Space Models. Each feature vector represents the bag-of-words of the respective document, assigning a weight to each feature/term that reflects its importance in the overall context of either the document or the document set. The definition of entity can also be extended to represent a document, where instead of a weighted feature vector, we have a set of terms that can be related to other entities (which may also be documents or other types of entities) by means of a semantic relatedness measure between entities, such as the one presented in this paper.

### 3 SIMILARITY RELATEDNESS MEASURE

The implementation of the proposed measure is based on the assumption that each pair of concepts is connected by a category path.

The proposed relatedness measure is computed from the following sequence of steps

#### Distance between Concepts - Weighted Edges

**Sum.** Let  $c_1$  and  $c_2$  be two concepts represented in the Wikipedia categories network. Find the shortest category path between the concepts. Compute the edge-based semantic relatedness between  $c_1$  and the LCS node, which is the sum of the weights of the edges that link  $c_1$  to the LCS node. Repeat this procedure to find the edge-based semantic relatedness between  $c_2$  and the LCS node.

The overall edge-based relatedness measure between the two concepts is given by

$$d(c_1, c_2) = \frac{\sum_{i=0}^L w_i^1 + \sum_{i=0}^R w_i^2}{\sum_{i=0}^L w_i^1 + \sum_{i=0}^R w_i^2} \quad (1)$$

where  $w_i^1$  is the weight of the edge with index  $i$  in

the category path between  $c_1$  and the LCS category,  $w_i^2$  is the weight of the edge with index  $i$  in the category path between  $c_2$  and the LCS category,  $I$  is the depth of the last edge of the path that connects  $c_1$  to the LCS and  $J$  is the depth of the last edge of the path that connects  $c_2$  to the LCS category, with  $R$  denoting the index of the last edge in the path between the root node and a concept node, with the restriction that this path must include the LCS.

**Edge-based Similarity between Entities.** Given two entities  $E_1$  and  $E_2$  represented by discrete sets of concepts  $C_1 = \{c_1^1, \dots, c_n^1\}$  and  $C_2 = \{c_1^2, \dots, c_m^2\}$ , respectively, we define the edge-based distance between sets  $D(E_1, E_2)$  is

$$D(E_1, E_2) = \frac{\sum_{i=1}^n \sum_{j=1}^m d(c_i, c_j)}{n \times m} \quad (2)$$

Finally, we have the following similarity measure between entities

$$S(E_1, E_2) = 1 - D(E_1, E_2) \quad (3)$$

### 3.1 Computation of Shortest Paths in the Wikipedia Graph

Several versions of the Wikipedia maybe be accessed at <http://dumps.wikimedia.org/backup-index.html>. For the results presented in this paper, we used a recent english version. To store all the Wikipedia pages and links we used the MySQL structure provided by the Java Wikipedia Library API (available at <http://www.ukp.tu-darmstadt.de/software/jwpl/>), further described in (Zesch et al., 2008). This API also helps us to determine if a page is of the "Disambiguation pages" type. We did not, however, used the API to build category paths, having specifically devised procedures for this task.

Each Wikipedia object of the type CATEGORY is assigned a level within the current search and a list of its nearest neighbors, when examined for shortest path computation. By regarding this shortest-path

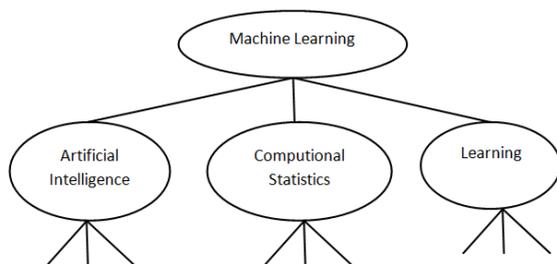


Figure 1: Instatiation of the concept "Machine Learning".

search as a tree-search, each instance of the object category will be a leaf of the tree.

```

1 Category nextLevel(Category c)
2   Begin
3   ForEach Category in c.List
4     Begin
5     If (IteratedCategory.List = null)
6       ->leaf node
7     Begin
8     WikiList=wikipedia.
9     GetAboveLevelCategories
10      ();
11     c.List=newList;
12   End
13   Else
14   Begin
15   NextLevel (IteratedCategory);
16   ->recursive method
17   End
18 End
19 End

```

Listing 1: Procedure to examine the upper level of a node.

After the instantiation of concept *Machine Learning* (see Figure 1), all of its parent categories ("Artificial Intelligence", "Learning" and "Computational Statistics") will have a level attribute of two. The instantiation of each of these categories will return their corresponding list of parent categories and a level attribute of 3 and so on. The pseudo code in Listing 1 illustrates this procedure.

For each computation of a category path between two concepts, two trees are built, one for each concept. The level attribute will grow until the algorithm finds a common ancestor (the LCS).

```

1 Void Main ()
2   Begin
3   List c1 = wikipedia.
4   GetAboveLevelCategories ("concept1")
5   ;
6   List c2 = wikipedia.
7   GetAboveLevelCategories ("concept2")
8   ;
9   While (ExistMatch (c1, c2) )
10  Begin
11  nextLevel (c1);
12  nextLevel (c2);
13  End
14 End

```

Listing 2: Procedure to find a path by means of a least common subsumer search.

The pseudo code in Listing 2 illustrates this procedure for example concepts "concept1" and "concept2".

These procedures were implemented with Java. Java is not the most adequate technology for this type of tree search, since it lacks tail call elimination for security reasons, as further detailed in the Bugs section of Oracles website<sup>3</sup> but it was sufficiently effective to accomplish our goals.

### 3.2 Density

The general idea behind the proposed improvement to the measure can be introduced with some generic mathematics concepts. In graph theory, a dense graph is a graph in which the number of edges is close to the maximal possible between all the vertices contained.

The maximum density is 1 and the minimum is 0 for a very sparse graph (Coleman and Moré, 1983).

In our case, we do not intend to calculate the complete density of the Wikipedia category ontology. Instead, we propose to analyse all the nodes in the shortest path and find all the degrees. Then it is necessary to find a way of discover the approximate level of density with the degrees as a clue.

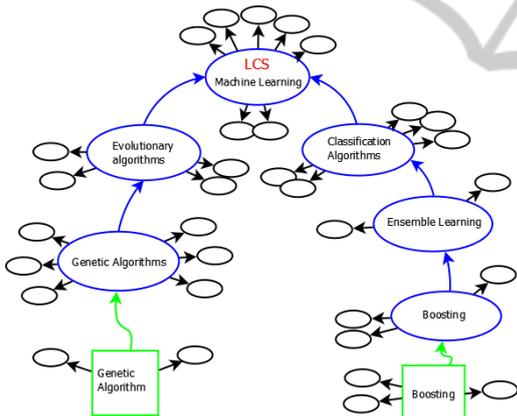


Figure 2: Example of an High Density path.

In the figure above, the larger circles represents Wikipedia categories in the path, the small ones represent the neighbors and the squares represents the Wikipedia pages. As it can be observed, Figure 2 represents a situation of higher density than Figure 3 and as we can conclude, the number of degrees for each node follows the tendency.

When path calculation occurs, the degrees of all vertices in the calculated path are saved, even the number of categories at the original pages. The objective is to save as much information as possible about the number neighbors of the calculated path. As it was previous explained, the properties of our entities were mapped to the correct page that represents the

<sup>3</sup>See [http://bugs.sun.com/view\\_bug.do?bug\\_id=4726340](http://bugs.sun.com/view_bug.do?bug_id=4726340)

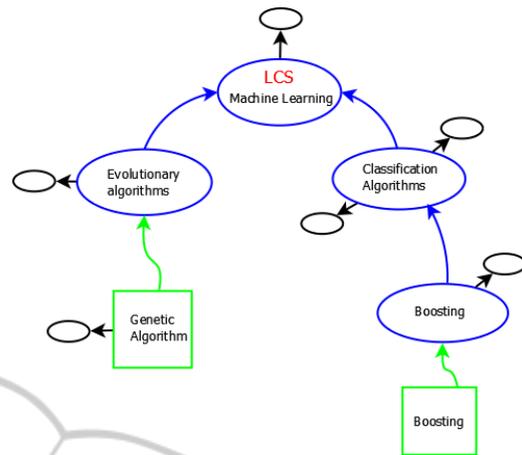


Figure 3: Example of a Low Density Path.

concept in Wikipedia. Figure 2 aims to find the distance between the property generic algorithm and the property boosting. These two concepts are contained in two different sets of properties, each one representing its own entity.

For every path explored between the entity properties the average number of neighbors is calculated. This means that information about the average number of nodes that are between the two entities is kept across the paths calculations, and based on that, allows to understand if the universe that we are working at the moment is more or less dense.

$$PathDensity(p1, p2) = \frac{\sum_1^n |E| (i)}{n} \quad (4)$$

$$PropertyDensity = \frac{PathDensity(p1, p2)}{PathDensity(p1, p2) + RootDensity(lcs, root)} \quad (5)$$

On top of that, as we saw before, the LCS node is very important to us. In a previous work it was concluded that it is very helpful to calculate how deep is this node (Medina et al., 2012). Now we propose to use additional information, by taking into account the density of the path between a given LCS and the root. The strategy is similar to the density calculation property, with the difference that now our path is between our LCS and the Wikipedia root category. We count the neighbors at each vertex and calculate the average at the end.

## 4 RESULTS AND DISCUSSION

With test result tracking in mind, we decided to use the same battery of entity tests from last paper (Medina et al., 2012). The results can be consulted on table

Table 1: Entities represented as sets of scientific topics. The first three entities represent actual conferences (CVPR, KDD and RECOMB respectively). The other three entities represent authors.

E1	E2	E3	E4	E5	E6
Computer Vision	Knowledge Discovery	Molecular Biology	Computer Vision	Information Extraction	Genetics
Object Recognition	Data Mining	Gene Expression	Robotics	Machine Learning	Human Genome
Structure from Motion	Web Mining	Computational Biology	Object Recognition	Natural Language Processing	Gene Expression
Image Segmentation	Recommender Systems	Genomics	Structure from Motion	Information Retrieval	Systems Biology
Image Processing	Cluster Analysis	Population Genetics	Human Computer Interaction	Data Mining	Clinical Medicine
Object categorization	Text Mining		Virtual Reality	Graphical Model	Bioinformatics
Optical Flow	Data Analytics		Facial Expression	Social Network	
Pattern Recognition	Structure Mining			Reinforcement Learning	
				Web Mining	

Table 2: Proposed similarity measure results.

Pair	$(E_1, E_4)$	$(E_1, E_5)$	$(E_1, E_6)$	$(E_2, E_4)$	$(E_2, E_5)$	$(E_2, E_6)$	$(E_3, E_4)$	$(E_3, E_5)$	$(E_3, E_6)$
S Eq.3	0.948	0.931	0.912	0.869	0.954	0.826	0.786	0.862	0.989
S Den	1.0	0.958	0.682	0.812	1.0	0.724	0.847	0.826	1.0

2, where the first row contains the values previously obtained on our first paper, and the second row contains the results achieved by the new method. The set is composed by six entities: three of them represent well known conferences (CVPR<sup>4</sup>, KDD<sup>5</sup> and RECOMB<sup>6</sup>). These conferences were chosen because each one corresponds to a distinct scientific research area: CVPR to Computer Vision and Pattern Recognition; KDD to Data Mining and Knowledge Discovery; RECOMB to Computational Molecular Biology. The other three entities represent well known authors. Each of these authors was chosen based on the strong correspondence of their research interests with one of the three conferences:

- **Author  $E_4$ :** from computer vision area, which matches CVPR represented by  $E_1$ .
- **Author  $E_5$ :** from data mining and machine learning areas, which are more related to the KDD, represented by  $E_2$ .
- **Author  $E_6$ :** from genetics and bioinformatics areas, which is more closely related to RECOMB (represented by  $E_3$ ).

Some concepts listed here do not have a direct correspondence with a Wikipedia page, so it lead us to a disambiguation problem. A quick solution for the first case was to replace the concept with a similar concept. For instance, the concept Image Segmentation of  $E_1$  had to be replaced with the page Segmentation (image processing). We will propose a technique to automation this kind of tasks in a future work.

From these results, as before, we observed a high value of similarity for the following entity pairs:

<sup>4</sup><http://www.cvpr2012.org/>

<sup>5</sup><http://kdd2012.sigkdd.org/>

<sup>6</sup><http://bioinfo.au.tsinghua.edu.cn/recomb2013/>

$(E_4, E_1)$ ,  $(E_5, E_2)$ , and  $(E_6, E_3)$ , but at this time, there is even stronger. This is expected due to the semantic overlapping of properties in the sets. It was also expected that the similarity values for  $(E_1, E_5)$  would be much lower than the value found for  $(E_1, E_4)$ . It was observed that in many cases this distance continues to return very high similarity values that are not quite differentiated. We believe this is due to the proximity of a single pair of features, among many features. The fact that similarity between entities is determined by the maximum value of the similarity between all combinations of pairs of entities features introduces "bias" to 1. Hence it is needed, eventually, in the future to introduce mechanisms to extend the dynamic range of the similarity between entities. However, the high similarity  $E_1$ - $E_5$  is explained due to some very similar features, such as Pattern Recognition vs. Machine Learning, for example.

## 5 CONCLUSIONS AND FUTURE WORK

In this paper we continue our journey to find a more balanced semantic relatedness measure between entities. As before, we believe that the use of Wikipedia and the hierarchy of scientific categories contained in it, is the most promising way to accomplish your goal.

The devised measure examines the Wikipedia category paths between all the possible concept pairs of two distinct entities, assigning weights according to the category's relevance. With this new attempt, we improve this measure by adding the notion of ontology density. We examined and compared new results with the old ones and concluded, by observing, that these matches are a step in the right direction. Although

there is room for future developments, mainly regarding the range of result values, the differentiation of values and eventually the introduction of a threshold. The issue is to determine where to place the threshold to make the right decision. Usually the threshold is set "half-way", however, for this test case, it should be placed above 0.73, which is a high value.

Future work includes continuing exploration of the measure for other contexts as well as a comparison of our measure with other state-of-the-art metrics. It is also very important the effort to make the process as much autonomous as possible, by giving to the process the ability of automatic disambiguation.

## ACKNOWLEDGEMENTS

The authors wish to acknowledge the support of the Escola Superior de Tecnologia, Instituto Politécnico de Setúbal (EST-IPS) and Instituto de Telecomunicações (IT-IST).

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