

GP-based Methodology for HW/SW Co-synthesis of Multiprocessor Embedded Systems with Increasing Number of Individuals Obtained by Mutation

Adam Górski¹ and Maciej Ogorzałek²

¹*Department of Information Technologies, Jagiellonian University in Cracow, Reymonta 4, Cracow, Poland*

²*Department of Information Technologies, Jagiellonian University in Cracow, Cracow, Poland*

Keywords: Embedded Systems, Genetic Programming, Genetic Algorithm, Architecture, Hardware/Software Co-Design, Multiprocessor System.

Abstract: In this work, a genetic programming methodology for co-synthesis of multiprocessor systems is presented. Genotype is a tree which nodes include system construction procedures. Thus the design methodology is evolving. Next generations are obtained using genetic operators: mutation, reproduction and crossover. Unlike other algorithms in presented methodology number of individuals obtained by mutation operator is not const. Therefore number of individuals in each population is increasing. The size of final generation is found by the algorithm.

1 INTRODUCTION

Nowadays embedded systems (Acasandrei and Barriga 2012) can be found almost everywhere: mobile phones, digital cameras, modern cars, etc. Embedded systems are also used to help coordination of different teams in crisis management (Mahdjoub and Rousseaux 2014). First embedded systems were not too much complicated. Therefore it was not necessary to find special methodologies for designing them. While complexity of embedded systems was increasing (Kopetz 2008) more effective design methodologies were needed (Martin 2006, Henzinger, Sifakis 2006). Co-synthesis is a process which automatically generates an architecture of embedded system using specification contained in a task graph. The goal of the process is to optimize parameters such cost, time or power consumption. Most of existing solutions (eg. Jiang, Eles and Peng 2012) assume distributed target architecture. The architecture consists of many processing elements (PEs). PEs can be divided into two groups: programmable processors (PPs) and hardware cores (HCs). PPs can execute more than one task thus their cost is low but they are not very fast. HCs can execute only one task thus the time of task execution is reduced, but cost of the resource is relatively high.

Co-synthesis process consists of three phases: 1. resource allocation – selection of number and types of PEs and communication channels; 2. task assignment – choice of PE for each task and transmission between resources; 3. task scheduling – determining when each task should begin its execution.

Existing methodologies can be divided on two basic groups. The most popular are iterative improvement algorithms (Deniziak 2004, Yen and Wolf 1995, Górski and Ogorzałek 2014a) which start from sub-optimal solution and refine systems by making local changes (moving task between PEs, allocating or removing PEs from system). Usually, as the initial solution, the fastest architecture is selected. Unfortunately the results obtained by most of these methodologies are still sub-optimal.

The second group includes constructive algorithms (eg. Dave, Lakshminarayana and Jha 1997). In those methodologies system is built by choosing PE for each task separately. Therefore those algorithms are tend to stop in local minima of optimizing parameters.

Probabilistic solutions, especially genetic algorithms (Chehida and Auguin 2002; Purnaprajna, Reformat and Pedrycz 2007) can escape from local minima. This group of algorithms contains for example simulated annealing (Eles, Peng, Kuchciński and Doboli 1997). Especially good

results were obtained using developmental genetic programming (Deniziak and Górski 2008). In this algorithm genetic programming evolves design methodology to obtain the best system.

Adaptive algorithms are also more and more popular in computer system design process (Shankaran, Roy, Schmidt, Koutsoukos, Chen, and Lu, 2008, Górski and Ogorzałek 2014b).

Genetic programming (Koza, Bennett III, Lohn, Dunlap, Keane and Andre, 1997) extends genetic algorithms (Holland, 1992). In genetic programming there is a strong the difference between phenotype and genotype. The genotype is a tree which consists of computer programs. The phenotype is the final solution. Genetic programming is wildly used amount other things in: machine learning (Krawiec 2002), design problems like synthesis computational circuits (Koza, Bennett III, Lohn, Dunlap, Keane and Andre, 1997) and in medicine for example in prediction survival in cancer (Giacobini, Provero, Vanneschi and Mauri 2014).

In every genetic methodology number of individuals obtained in every population is constant. Therefore large number of individuals have to be generated to make the algorithm effective. In the environment the situation is completely different. The number of individuals in most of species increases.

In this article a new approach based on developmental genetic programming (Koza 2010) is presented. Unlike other methodologies in presented algorithm the number of individuals obtained by mutation operator in each generation is increasing. In section 3 the methodology is described. Sections 4 and 5 present experimental results (obtained using set of benchmarks with 10, 20 and 30 nodes) and conclusions.

2 PRELIMINARIES

Like in many works (eg. Engelhardt, Dallou, Elhossini and Juurlink 2014) we assume, that the behaviour of embedded system is described by an acyclic, directed graph called the task graph $G = \{V, E\}$. Each node $v_i \in V$ represents task, and edge $e_i \in E$ presents dependence between tasks. Label d_{ij} describes the amount of data that has to be transferred between two connected tasks (v_i and v_j). Transmission t_{ij} is defined as follows:

$$t_{ij} = \frac{d_{ij}}{b_{CL}} \quad (1)$$

where: b_{CL} is a bandwidth which characterises communication link (CL).

As an example we use task graph proposed by Górski and Ogorzałek (Górski and Ogorzałek 2014). It is presented on fig. 1. The graph includes 7 tasks.

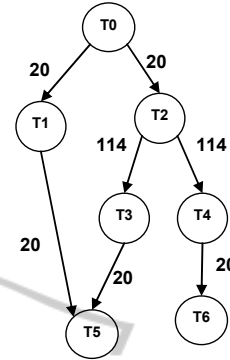


Figure 1: Example of task graph.

An example of a resource database for the system described by the graph above is presented in table 1. It contains two communication links (CL1 and CL2) and four PEs: two programmable processors (PP1 and PP2), two Hardware cores (HC1 and HC2). Every task is defined by area occupied by this task (s) and a time of execution (t). Areas occupied by the tasks mean the size of memory needed to execute these tasks. Communication links are defined by a bandwidth (b) and an area (s) occupied by the link connected to PE. Table 1 also includes the area (S) occupied by each PE. The area of the tasks implemented in HC includes the area occupied by the core.

Table 1: Resource database.

Task	PP1 S=200		PP2 S=300		HC1		HC2	
	t	s	t	s	t	s	t	s
T0	150	4	120	6	50	180	30	250
T1	40	3	35	2	14	100	10	140
T2	-	-	320	17	250	200	150	650
T3	235	10	220	15	140	160	90	200
T4	165	8	150	10	65	100	40	140
T5	70	4	40	5	25	100	-	-
T6	23	2	20	1	5	40	2	80
CL1, b=6	s=2		s=2		s=10			
CL2, b=15	-		s=2		s=15			

Task T2 is not compatible with PP1, and task T5 cannot be implemented in HC2. Communication link CL2 is not compatible with PP1.

The final architecture of designing system contains p communication links and m programmable processors and hardware cores, (selected from table 1.) which execute n processes. Overall area (S_o) of the system is described by the following formula:

$$S_o = \sum_{i=1}^m S_{PE_i} + \sum_{j=1}^n S_j + \sum_{k=1}^p \sum_{l=1}^{P_k} S_{CL_k, PC_l} \quad (2)$$

The goal of co-design is to find an architecture with the lowest S_o value. The value must satisfy time constrains.

3 INITIAL POPULATION

In genetic programming it is strong difference between genotype and phenotype. According to genetic programming rules in this methodology genotype is a system construction tree, which evolves. The phenotype is the final solution. At the beginning embryo is created. The embryo is a randomly implementation of the first task. The number of possible embryos is the number of possible PEs in the database. Every next node in the genotype describes system constructing decision. To ensure that system executes all tasks the structure of genotype has to be based on the task graph. Each node in the tree must correspond to equal system constructing function. The options for constructing system are presented in table 2. To check the efficiency of proposed methodology we decided to use the same system constructing function as were proposed by Denziak and Górski in DGP08 algorithm (Denziak and Górski 2008). However there are differences in evolution process. Therefore we are certain that quality of obtained solutions is a result of using presented methodology. The last column includes probability of selection of system-construction options. The initial population contains of randomly generated genotypes. Π_0 is the size of initial population:

$$\Pi_0 = \alpha * n * p \quad (3)$$

where: n – number of tasks in task graph, p – number of possible embryos, α – control parameter which determines the number of individuals in populations; it is set manually.

The system is constructed by executing functions in order corresponding to the level of the node in the genotype tree. Then solutions are sorted by the lowest cost.

Table 2: Options for constructing system.

Step	Option	Probability
PE	a. Used PE	0.6
	b. The smallest area	0.1
	c. The fastest	0.1
	d. Min ($s*t$)	0.1
	e. The least used	0.1
Used PE	a1. The smallest area	0.2
	a2. The fastest	0.2
	a3. The lowest utilization	0.2
	a4. Idle for the longest time	0.2
	a5. The same as a predecessor	0.2
CL	a. Used CL	0.5
	b. The highest b	0.2
	c. The last used	0.2
	d. The smallest area	0.1
Used CL	a1. The smallest area	0.3
	a2. The fastest	0.3
	a3. The lowest utilization	0.2
	a4. Idle for the longest time	0.2
Task scheduling	list scheduling	1

4 EVOLUTION

To obtain new population we used standard genetic operators: crossover, mutation and reproduction. The number of individuals obtained by using genetic operators is given:

- $\Phi = \beta * \Pi$ – individuals obtained by reproduction;
- $\Psi = \gamma * \Pi$ – individuals obtained by crossover;
- $\Omega = \delta * \Pi$ – individuals obtained by mutation;

Parameters β , γ , δ are used to control the evolution process. They are set manually.

Unlike other methodologies number of individuals in each population is not const. Thus:

$$\beta + \gamma + \delta > 1 \quad (4)$$

Reproduction randomly copies the Φ genotypes from the current population. Individuals are chosen randomly but with different probability P . The probability depends on the position q in rank list. It is described as follow:

$$P = \frac{\Pi_c - q}{\Pi_c} \quad (5)$$

Π_c in formula above is a size of current

population. It can be defined as follows:

$$\Pi_c = (\beta + \gamma + \delta) * \Pi_{c-1} \tag{6}$$

Crossover chooses randomly the Ψ solutions. The crossing point is selected randomly. It is the same for both genotypes. Afterwards the sub-trees are substituted.

Mutation is responsible for providing fresh genes to the environment. Thus we decide to increase number of individuals obtained using mutation operator. The operator randomly selects one individual and one node, than changes option in this node to a different one from the option list.

Figure 2 shows an example of genotype for the task graph of figure 1.

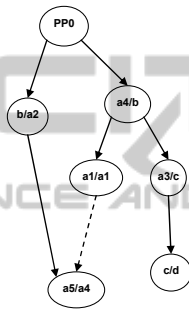


Figure 2: Example of genotype.

After generating new population new rank list is created. The process is stopped when cheapest solution which satisfies time constrains wasn't found in next ϵ steps (last ϵ generations). Parameter ϵ is set manually.

5 EXPERIMENTAL RESULTS

Because of very large computational complexity of the co-design problem, the best way to check effectiveness of proposed methodology is to compare the performance with other existing methods. All experiments were carried out on

benchmarks with 10, 20 and 30 nodes. We compared presented methodology with algorithm DGP08 (Deniziak and Górski, 2008) and algorithm Ewa (Deniziak, 2004). DGP08 is genetic programming algorithm for co-synthesis. It was compared with algorithm Yen-Wolf (Yen and Wolf 1995) for co-synthesis. Algorithm Ewa was proved to be more effective than MOGAC (Dick and Jha, 1998). MOGAC is a genetic algorithm for co-synthesis. Therefore we believe that this comparison is the best to check effectiveness of the proposed methodology. Because of probabilistic nature of the methodologies, for each graph 30 tries were made.

In table 3 the comparison results are presented. In the table the best and average values of cost and execution time for the algorithms are presented. For both genetic methodologies parameters $\alpha=100$, $\beta=0,2$, $\gamma=0,7$ and $\epsilon=5$. For algorithm DGP08 $\delta=0,1$. The time constrains were set as follow: 350 for graph with 10 nodes, 500 for graph with 20 nodes, 800 for graph with 30 nodes. In table 4 values of δ parameter for algorithm GP 2015 are given. We decided to check efficiency of proposed algorithm with δ values 0,2 and 0,3. In all of the experiments parameter $\alpha=100$.

For graph with 10 nodes the best result obtained for all of the genetic methodologies has cost 1590 and time 326. However average cost is lower for the methodology presented in this paper. For DGP08 average cost is 1602. In our algorithm average costs are: 1594 when parameter $\delta=0,2$ and the lowest 1593 when $\delta=0,3$. The same situation can be observed for the rest of graphs. Best average results were obtained when parameter $\delta=0,3$. For graph 20 average cost was: 2652 when $\delta=0,2$ and 2649 when $\delta=0,3$, while for DGP08 it was 2669. For both genetic methodologies the best obtained cost was 2649. For bigger graph (with 30 nodes) the results indicates on high efficiency of proposed solution.

The average cost for DGP08 was 3130, while for presented approach was 3107 (when $\delta=0,2$) and 3074 (when $\delta=0,3$). What is worth to underline the

Table 3: Experimental results.

Graph	T_{max}	Ewa		DGP08				GP 2015				δ
		time	cost	time	cost	average time	average cost	time	cost	average time	average cost	
10	350	204	2975	326	1590	296	1602	326	1590	308	1594	0,2
								326	1590	316	1593	0,3
20	500	457	3020	396	2649	396	2649	396	2649	396	2652	0,2
								396	2649	396	2649	0,3
30	800	789	5330	792	3081	793	3130	792	3081	792	3107	0,2
								792	3056	792	3074	0,3

average cost obtained by presented algorithm for graph with 30 nodes when $\delta=0,3$ (3074) is lower than the best obtained result using DGP08 (3081). For presented methodology, when $\delta=0,2$, the best obtained solution is the same as for DGP08 (3081). Results obtained by algorithm Ewa was: time 204, and cost 2975 for graph 10, for graph with 20 nodes the execution time was 457 while cost was 3020. Also for bigger graph (with 30 nodes) the results were much worse that obtained by DGP08 and GP2015 – obtained time was 789 and cost was 5330.

6 CONCLUSIONS

In this paper we present a new methodology based on genetic programming for hardware/software co-synthesis. Unlike other genetic programming approaches the number of individuals in populations is not const. Moreover the number of individuals increases in each population. This is achieved by increasing number of individuals obtained using mutation operator.

First obtained results indicates that the results obtained by proposed methodology are better than obtained using other algorithms. In every genetic approach number of individuals in each population has to be large. Presented methodology allows to generate less individuals in initial population and obtain good solutions during evolution process. The size of final population will be found by the algorithm.

Some test like t-test, Mann-Whitney test or Wilcoxon test (Ruxton, 2006) can be made to compare DGP08 and GP 2015, but we were afraid that they may underestimate the true significance of obtained results.

The future work will concentrate on examining the influence of another genetic operators on quality of the results and different representation of genotype tree. We will also test different genetic operators and chromosomes.

ACKNOWLEDGEMENTS

This work is supported by the Foundation for Polish Science, under grant “Mistrz 2012” No. 9/2012: “New computational approaches for solving next generation microelectronic design problems”.

REFERENCES

- Acasandrei, L., Barriga, A., 2012. FPGA implementation of an embedded face detection system based on LEON3. In *Proceedings of the International Conference on Image Pro-cessing, Computer Vision, and Pattern Recognition*.
- Mahdjoub, J., Rousseaux, F., 2014. Planning and Optimization of Resources Deployment: Application to Crisis Management. In *Proceedings of the 11th IEEE International Conference on Embedded Software and Systems*.
- Kopetz, H., 2008. The complexity challenge in embedded system design. In *Proceedings of the 11th IEEE International Symposium on object Oriented Real-Time Distributed Computing*.
- Martin, G., 2006. Overview of the MPSoC Design Challenge. In *Proceedings of the 43rd annual Design Automation Conference*.
- Henzinger, T.A., Sifakis, J., 2006. The Embedded Systems Design Challenge. In *Lecture Notes in Computer Science, vol. 4085, pp 1-15*.
- Jiang, K., Eles, P., Peng, Z., 2012. Co-design techniques for distributed real-time embedded systems with communication security constrains. *Design Automation and Test in Europe (DATE 2012)*.
- Deniziak, S., 2004. Cost-efficient synthesis of multiprocessor heterogeneous systems. In *Control and Cybernetics, vol. 33, No. 2*.
- Yen, T., Wolf, W., 1995. Sensivity-Driven Co-Synthesis of Distributed Embedded Systems. In *Proceedings of the International Symposium on System Synthesis*.
- Górski, A., Ogorzałek, M., 2014a. Iterative Improvement methodology for hardware/software co-synthesis of embedded systems based on genetic programming. In *Proceedings of the 11th IEEE International Conference on Embedded Software and Systems (Work in Progress session)*.
- Dave, B., Lakshminarayana, G., Jha, N., 1997. COSYN: Hardware/software Co-synthesis of Embedded Systems. In *Proceedings of the 34th annual Design Automation Conference (DAC'97)*.
- Cehida, K., B., Auguin, M., 2002. HW/SW Partitioning Approach for Reconfigurable System Design. In *Proceedings of the International Conference on Compilers, Architectures and Synthesis for Embedded Systems, CASES 2002*.
- Purnaprajna, M., Reformat, M., Pedrycz, W., 2007. Genetic algorithms for hardware-software partitioning and optimal resource allocation. In *Journal of Systems Architecture, 53(7)*.
- Eles, P., Peng, Z., Kuchciński, K., Doboli, A., 1997. System Level Hardware/Software Partitioning Based on Simulated Annealing and Tabu Search. In *Design Automation for Embedded Systems, vol. 2, No 1*.
- Deniziak, S., Górski, A., 2008. Hardware/Software Co-Synthesis of Distributed Embedded Systems Using Genetic programming. In *Proceedings of the 8th International Conference Evolvable Systems: From*

- Biology to Hardware, ICES 2008*. Lecture Notes in Computer Science, Vol. 5216. Springer-Verlag.
- Shankaran, N., Roy, N., Schmidt, D. C., Koutsoukos, X. D. C., Chen, Y., Lu, C., 2008. Design and performance evaluation of an adaptive resource management framework for distributed real-time and embedded systems. *EURASIP Journal on Embedded Systems*.
- Górski, A., Ogorzałek, M., 2014b. Adaptive GP-based algorithm for hardware-software co-design of distributed embedded systems. In *Proceedings of the 4th International Conference on Pervasive and Embedded Computing and Communication Systems*.
- Koza, J. R., Bennett III, F. H., Lohn, j., Dunlap, F., Keane, M. A., Andre, D., 1997. Automated synthesis of computational circuits using genetic programming. In *Proceedings of the IEEE Conference on Evolutionary Computation*. IEEE.
- Holland, J. H., 1992. An Introductory Analysis with Applications to Biology, Control, and Artificial Intelligence. IN *MIT Press, Cambridge, MA*.
- Krawiec, G., 2002. Genetic programming-based construction of features for machine learning and knowledge discovery tasks. In *Genetic Programming and Evolvable Machines*, vol. 3, No. 4., pp. 329–343.
- Giacobini, M., Provero, P., Vanneschi L., Mauri, G. 2014. Towards the Use of Genetic Programming for the Prediction of Survival in Cancer. In *Evolution, Complexity and Artificial Life*, pp177-192.
- John R. Koza. 2010. Human-competitive results produced by genetic programming. In *Genetic programming and evolvable machines*, vol. 11, issue 3-4. Springer-Verlag.
- Engelhardt, N., Dallou, T., Elhossini, A., Juurlink, B 2014. An Integrated Hardware-Software Approach to Task Graph Management. In *Proceedings of the 16th IEEE International Conference on High Performance and Communications*.
- Dick, R., P., Jha, N., K., 1998. MOGAC: a multiobjective Genetic algorithm for the Co-Synthesis of Hardware-Software Embedded Systems. In *IEEE Trans. on Computer Aided Design of Integrated Circuits and systems*, vol. 17, No. 10.
- Ruxton., G., D., 2006. The unequal variance t-test is an underused alternative to Student's t-test and the Mann-Whitney U test. In *Behavioral Ecology*, 17(4). doi:[http:// dx.doi.org/10.1093/beheco/ark016](http://dx.doi.org/10.1093/beheco/ark016).

