

# Modelling and Analysis of Process Execution based on Data Acquired from Sensors Networks

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Abstract: This paper proposes a new approach for the analysis of physical processes. Based on several assumptions regarding the information available regarding the physical processes, we constrain the generation of the transition system. The method is based on the theory of regions that allows for the building compact representations as Petri Nets of transition systems and a set of explicit descriptions for some of the activities. The resulting compact model will exhibit the same behaviour as the input transition system. In order to evaluate the resulting process model, several quality dimensions have been established.

## 1 INTRODUCTION

This paper proposes a new approach for the analysis of physical processes. For this, we employ a technique from the field of process mining – the two step approach (Aalst, 2010) which works by constructing a transition system from an observed event log, followed by its transformation into a Petri Net using an algorithm based on the theory of regions.

We propose a new method of building the transition system based on state variables. In order to achieve this, we make several assumptions about the information available regarding the processes: knowledge of the preconditions and effects of the actions that triggered the events and the initial state of the system.

## 2 RELATED WORK

Process mining is a newly developed research field that provides methods *for analysing* processes starting from their observed behaviour.

This observed behaviour is encapsulated in event logs and it is readily available in most PAIS (Process Aware Information Systems) usually deployed in enterprise environments. Furthermore, the information contained in the event logs, can also be

collected from other types of systems, such as embedded systems, using an array of sensors.

Each event in a log is referring to an activity or action performed in the system (that led to a change in the system's state) and to a process instance or case. An event log contains sequences of events collected from the observed processes instances or cases. Each of these sequences is also called a process trace. For different process instances the same trace may be recorded, but the order in which different cases are logged is not relevant to the analysis. Because of this, the event log is represented as a multi-set or bag of event sequences.

The three main tasks considered in the field of process mining are process discovery, conformance checking and process model enhancement.

The process discovery problem is concerned with finding a process model which best represents an observed behaviour contained in an event log. Usually, a simple event log is considered, one that contains events that only refer to an activity and a process case. (Moisescu, 2013), (Repta, 2013).

Several algorithms have been proposed as solutions to the process discovery problem, such as: the (extended) alpha algorithm, heuristic miner (Weijters, 2003), genetic miner, fuzzy miner, ILP miner (Werf, 2008) and the two-step approach based on state-space theory of regions (Aalst, 2010). An analysis of the proposed process discovery algorithms is beyond the scope of this paper, but

several reviews have been made such as (Tiwari, 2008) in which various approaches to process discovery are comparatively described and evaluated.

Conformance checking is used to evaluate a process model against an event log. Techniques proposed in this subfield of process mining can be used in a variety of scenarios such as assessing a discovered process model or analysing the implementation of a process by comparing the base model with the observations from the production system. Recently, several quality dimensions have been established in order to evaluate process models: fitness, simplicity, precision and generality. Fitness quantifies the amount of observed behaviour that can be generated by the evaluated model. It is desirable for the process model to have perfect fitness, meaning that all the observed traces can be generated by it. This quality metric is evaluated by replaying each collected trace on the process model and penalizing misalignments (Aalst, 2012). The “simplicity” quality dimension refers to the size and complexity of the process model and it is related to the Occam’s razor principle. A metric based on the number of elements in the process model is usually used to evaluate this quality dimension. It should be noted that in some cases, a compact process model will not be the best representation of a process from an analysts’ perspective. Lastly, precision and generality refer to the amount of unobserved behaviour that the process model can generate. They are concerned with the problems of under-fitting (too general) and over-fitting (too precise) process models. A balance must be reached between the amount of behaviour that the resulting model allows and the behaviour expressed in the input event log. On one hand, we cannot expect that all possible behaviour will be found in the observed log. This is particularly obvious in the case of parallel activity sequences, where not all possible instantiations are expected to appear in the log. On the other hand, a process model that allows too much behaviour won’t be useful for the user or analyst as it discards the dependencies / constraints of the real process.

Finally, the task of process model enhancement takes as input an existing process model and event log and aims at improving or extending the model using the information provided in the log. These techniques require more information than what is contained in a simple event log. Decision mining (de Leoni, 2013) – identifying the conditions associated with the decision points in process models – requires additional data attributes associated with the events in the log, based on which classification problems

are instantiated. Social network analysis (Aalst, 2004), (Song, 2008) that aims at identifying the relations between the actors involved in the execution of the process require that each event references the entities that participated in the completion of the activity. Furthermore, timestamp of the events can be used to analyse the execution time of processes and determine performance data or identify bottlenecks.

The ability of the proposed process discovery and enhancement techniques to tackle problems from various domains has been extensively studied. In (Rozinat, 2009), the Heuristic Miner and the Decision Miner are used to analyse and diagnose a multi-agent system composed of soccer playing robots. In (Aalst, 2007) a billing process in a public administration office is analysed using various process mining techniques demonstrating their utility in the case of large organizations. *Finally*, a case study on industrial production systems is discussed and analysed in (Rozinat, 2009) (Gunther, 2010). This last example reveals some of the shortcomings of existing approaches to process discovery in the case of less-structured processes.

The approach presented in this paper belongs to the process discovery task, but requires additional information beyond an elementary event log. Namely, we investigate the use of an explicit state-space representation of the actions associated with the events from the input log, as prior information. This information is used in the two-step process discovery approach (Aalst, 2010) to construct a “more accurate” transition system.

### 3 PROBLEM STATEMENT

We consider that the assumptions we make regarding the availability of the additional prior information are feasible in the considered scenario of physical processes.

In this case, it is conceivable that at least a subset of the events in the log is retrieved using data from sensors deployed in the environment, thus making available at least a part of the real state of the system. This additional information will result in the discovery of a process model that is closer to the reality.

In fig. 1 depicts the example process considered in this paper (the implicit places in the Petri Net are hidden).

The example process can depict two vehicles (A and B) that move independently in an environment partitioned into several areas. The events “Ax” and

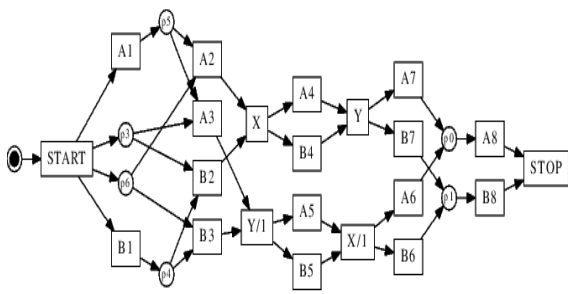


Figure 1: Example process model.

“Bx” correspond to movement actions of vehicle A and B between the areas of the environment. The goal of this process is to perform 2 “work” actions – X and Y - in two separate, pre-determined areas. These “work” action require that both vehicles are in the same area, at the same time.

In this case, the events regarding the movement of the vehicles in the environment can be automatically collected, leveraging an existing access-control system.

#### 4 TWO STEP PROCESS DISCOVERY

In this section we make a short description of the two step method of process discovery, discussed in (Aalst, 2010) with a focus on the impact of various methods of building the transition system on the precision and generality of the discovered model.

The method is based on the theory of regions that provides a method of building compact representations as Petri Nets of transition systems. The resulting compact model will exhibit the same behaviour as the input transition system.

The considered process discovery method first builds a transition system based on the information from the log and then converts it - the second step - in a compact Petri Net representation.

DEF (Transition system) – A transition system  $TS = (S, E, T)$ , in which S represents the set of states, E is the set of transition labels (including the silent transition) and  $T \subset S \times E \times S$  is the transition relation.

The transition system can be viewed as a directed graph in which the initial states are the states with no incoming arcs, while the final states have no outgoing arcs.

In fig. 2 the first step of the process discovery process – the construction of the transition system – is depicted. Each state is constructed using a

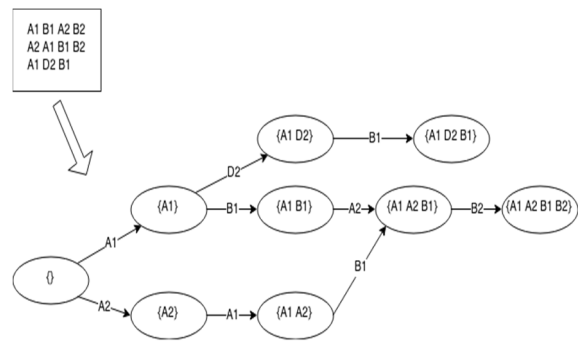


Figure 2.

function “state( $\sigma, k$ )” that takes as arguments a sequence of events and an index k. The state function assigns to each k-length prefix or suffix of the sequence  $\sigma$  a state from the state space of the transition system. In order to build a transition system from the input event log, the state function must be applied on each sequence of events to all of its indexes. In the original approach, the authors propose several method of representing each state – as a set of events, a bag (multi-set) or list. In the example presented in fig.2, each state is constructed by transforming the prefix of each sequence of events into a set.

Beyond these simple transformations, the state generation function can be enhanced through the use several “abstractions” that limit the horizon on which the transformation is applied, the size of the resulting collection, or the labels that are included in the final state representation.

After the creation of the transition system, several operations that can be applied on it in order to improve the quality of resulting process model – removing self-loops or closing “diamond” structures.

The second step of the process discovery approach involves the creation of a Petri Net that exhibits the same behaviour as the transition system. This step is based on the results of the research into the synthesis problem – the problem of synthesising a Petri Net whose behaviour coincides with a specified behaviour.

There are two approaches to this problem – state-based region theory and language-based theory of regions. Although the basic principle is similar, the input – the behaviour specification – is different. While the state-based approach uses as input a transition system, the language-based methods uses a regular language – a finite set of sequences (the log). Naturally, given the generated transition system, a state-based approach will be used in the

second step of the described approach.

A region represents a set of states that fulfil the condition that all transitions having the same label either enter, exit or don't cross the region. In the simplest case, of excitation-closed transition systems (Carmona, 2008), the employed algorithm will identify the minimal, non-trivial (empty set of states) regions, and each one will correspond to a place in the resulting Petri Net. For each place, the events that enter the region correspond to a transition generating tokens in that place and events that exit to transitions that consume tokens. The resulting Petri Net will be able to simulate the specified transition system – “bi-similarity property”. In the case of arbitrary transition system, the “excitation-closure” property must be first enforced. A proposed technique uses “label splitting” (Cortadela, 1998) in which the sets of transitions having the same label are partitioned thus adding new labels to the system.

## 5 EXPLICIT STATE REPRESENTATION

In this section we present a slightly modified procedure of generating the transition system required in order to build the Petri Net.

In order to enable this method that uses an explicit representation of the system's state, we make several assumptions:

- Activity definitions based on state variables can be defined for a subset of the events
- The initial state of the transition system, expressed in terms of state variable values is known
- The explicit description of activities must be accurate and the actors involved in the process use the optimal path in the state-space in order to achieve their goal

We consider these to be feasible assumptions given that the focus of our approach is represented by physical processes. In these scenarios, it is considered that at least some events in the input log are derived from sensor observations – and a subset of the real system state is known.

We redefine the generic definition of state and transition system used in the two-step process discovery technique using state variable.

DEF (State) – A state  $S \in D_1 \times D_2 \times \dots \times D_n$ , where  $D_1 \dots D_n$  are the (finite) domains of the state variable  $v_1 \dots v_n \in V$ , where  $V$  is the set of state variables. Each state variable has a unique index assigned by the function  $idx: V \rightarrow N$ .

DEF (Explicit action definition) – An explicit

action definition is a pair  $(P, E)$  of conditions and effects:

-  $P \subseteq D_1 \times D_2 \times \dots \times D_n$  – the set of states in which the action  $A$  is enabled

-  $E \in \overline{D_1} \times \overline{D_2} \times \dots \times \overline{D_n}$  – the effect of executing the action. For each state variable  $v_i$ , the set  $\overline{D_i} = D_i \cup \{e\}$ , where  $e$  is the null element, signifying that the action doesn't affect the value of the state variable.

In the following sections, we will use a simpler notation of states and actions:  $s_1 = (\text{pos\_vehicle\_1} = \text{gate\_1}, \text{pos\_vehicle\_2} = \text{work\_area}, \text{move\_1\_vehicle\_1} = (\text{pos\_vehicle\_1} = \text{gate\_1}, \text{vehicle\_inactive} = \text{true}; \text{pos\_vehicle\_1} = \text{work\_area}))$

We distinguish between two types of actions – explicit, for which descriptions of the conditions and effects are available and expressed using the state variables and implicit, for which these descriptions are missing.

In order to enable the correct generation of the transition system, for each implicit action a new state variable will be introduced. The state representation of the implicit actions will be automatically generated and will have an empty condition expression and, as the effect, a change of the associated state variable from the initial state to a new value. Although the empty condition expression for the implicit actions means that the action is enabled in any state, when building the transition system, it will be ignored.

Notice that this representation of implicit actions is equivalent to representing states as sets of actions in the original approach. For other ways of representing states, such as multi-sets or lists, a different approach for creating the state definitions of implicit actions is required.

We assume that implicit actions will correspond to events from high-level activities that are logged by human operators or by other information systems, while the explicit events are logged using sensor data.

In the extreme case of an event log that refers only to implicit actions, the resulting transition system will be equivalent to the one generated by the original approach.

The method of generating the transition system will make use the available information regarding the state changes. First, a transition system that contains just the initial state will be created. After that, each trace from the input event log will be processed. Starting by considering the initial state as the current state, for each event, the procedure will insert a new transition labelled with the event name between the current and the next state. The next state



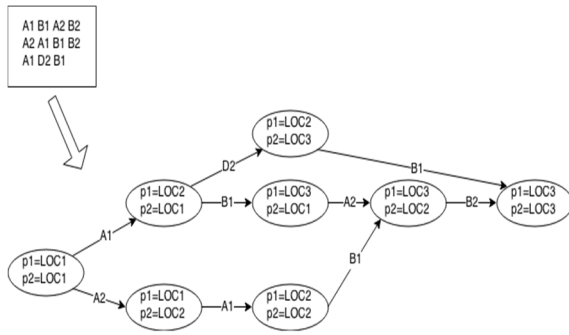


Figure 3.

will be computed using the available information about the effects of the action related to the event. If the next state doesn't exist in the transition system, it will be added. After the transition is added to the system, the next state becomes the current state and the next transition is the sequence of the event trace is considered.

An example of transition system generated using this procedure is depicted in fig. 3. In this case, the state variables "p1" and "p2" are used and they have the save domain  $D_1 = D_2 = \{LOC1, LOC2, LOC3\}$ . Starting from the initial state (p1=LOC1, p2=LOC2), the procedure will fist consider the transition "A1" for which the state description is (p1=LOC1; p1=LOC2). As the initial state validates the action's conditions, the effects are applied and the state (p1=LOC2, p2=LOC1) is added to the system.

Notice that the algorithm will be able to detect inconsistencies in the definitions of the conditions of the explicit actions by checking them against the definition of the current state.

The second part of the proposed approach will leverage the explicit description of the actions to add possible, but missing behaviour to the system.

It is expected that the log will not contain all possible behaviour that can be generated by the system, especially in the case of parallel sequences. This is a major problem to existing process mining algorithms as it prevents the accurate detection of the real causal relations between the activities.

Our approach aims at alleviating this problem by using the state description of the actions to introduce new states and transitions in the system.

In order to achieve this, the algorithm determines the set of goal states for each state of the system. A final state F is a goal state for state S if an optimal path from the initial state to F passes through S. The cost of a path is equal to its length.

Then, for each state S, the procedure will search for new optimal paths towards all the associated goal

states. For this, all explicit action definitions whose conditions match the current state S are considered as the first transition T of the new path. A next state  $S_n$  is created by applying the effects described by the action definition to the state S. If  $S_n$  is already present in the transition system, the currently considered action will be added only if a path that starts with T and passes through  $S_n$  has the same cost as the optimal paths from S to the goal state. Otherwise, the procedure will use a planning algorithm in order to find an optimal path that starts with T towards the final goal. A planning domain will be created that contains all the observed domain values of the state variables as PDDL predicates and all explicit action definitions as PDDL actions. If a valid optimal plan is found and its length is the same as the optimal paths from S to the goal state, the algorithm will embed it the transition system by adding the missing states and transitions.

The updated transition system will then be transformed into the final Petri Net process model using an existing algorithm based on the theory of regions.

In our experiments we used petrify (Cortadela, 1998) to generate the final process model from the transition system and LPRPG planner (Coles, 2011) for searching for new optimal paths in the system.

## 6 EVALUATION

In order to evaluate our approach, we considered 20 types of traces (behaviours) that can be generated by the example process. These traces were compiled into an event log that was used as input to various process discovery algorithms.

We compared the process models generated by various existing process mining algorithms with the ones that were generated from the transition system enhanced using the procedure described in the previous section.

In fig. 4, the process model discovered by the "ILP Miner" plugin from the ProM suite is depicted.

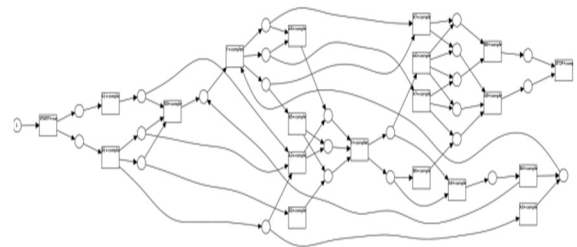


Figure 4: Process model generated using the ILP Miner.

The same log was also processed using the heuristic process discovery algorithm, and the resulting model is presented in fig. 3.



Figure 5: Process model generated using the Heuristic Miner.

Using the original two-step process mining discovery method, with states represented by sets of events with no limit in size, the process model from fig. 6 is generated.

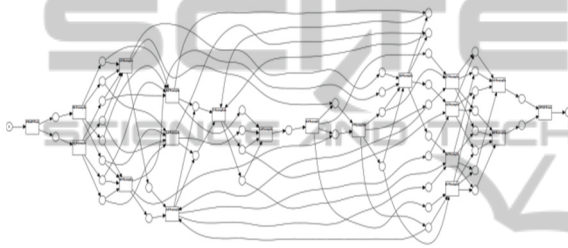


Figure 6.

The process model that corresponds to the transition system generated using the method presented in previous sections is depicted in Fig. 7.

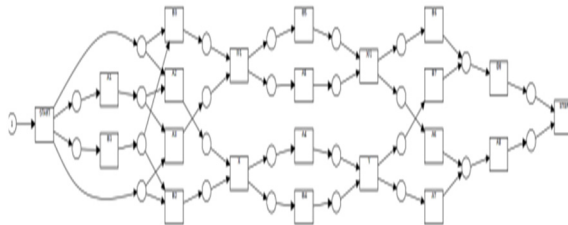


Figure 7.

Excluding the model obtained using the heuristic miner, that can't reproduce all the traces in the input log, from a simple visual inspection it is clear that the last process model is the simplest.

For each of the discovered process models we used the "Replay a Log for Conformance Analysis" and "Measure Precision / Generalization" plugins from ProM to compute metrics for three quality dimensions: fitness, precision and generalization. All three values are computed based on an optimal alignment between the process model and the event log (Aalst, 2012). The fitness value measures how

well the discovered model is able to replay the traces in the event log, with each deviation being penalized. The value for fitness ranges between 0 and 1, with 1(perfect fitness) meaning that all the traces in the log can be generated by the model. The metrics for precision and generalization are computed using empirical formulas, attempting to quantify the problems of "under-fitting" and "over-fitting". An "under-fitting" process model lacks precision by allowing "much more" behaviour than presented in the event log and consequently having a low value for the precision metric. The generalization metric is concerned with the opposite problem, of "over-fitting" models, that are only able to exhibit the behaviour in the event log. Such processes will have a low value for the generalization metric.

The computed values for the 4 process models are depicted in Table 1. All metrics are normalized in the [0, 1] interval.

Table 1.

	Fitness	Precision	Generalization
Heuristic Miner	0.8	0.58028	0.65238
ILPMiner	1	0.83036	0.76173
Transition system	1	0.93304	0.72432
Enhanced transition system	1	0.83185	0.72432

As expected, the precision value for the model generated from the enhanced transition system is smaller than the one of the model obtained using the original approach due to the added states and transitions.

## 7 CONCLUSIONS

In the future, a more detailed analysis of the proposed method is required, one that focuses on event logs collected from real processes.

Another research direction will need to focus on relaxing some of the assumptions regarding the behaviour of the agents involved in the execution of the process and the exact descriptions of the explicit actions. It is expected that at least in some cases, the execution of the process won't follow an optimal trajectory. Furthermore, the state description of the explicit actions may be incomplete, with missing conditions which lead to the creation of imprecise (under-fitting) process models.

It was assumed in this paper that all the available events were correctly partitioned into traces corresponding to process instances. In real systems however, the collection and processing of events may pose an important problem that needs to be addressed in at least a semi-automatic manner. This issue needs to be addressed in the future, starting with existing proposal such as (Rozsnyai, 2011) in which a method of detection correlations between events based on the values of their associated attributes is discussed.

An issue that was not addressed in this paper concerns the discovery of process models that contain loops. In order to handle this case, a different approach for the representation of state is required.

Finally, the proposed method is based on a set of explicit descriptions for some of the activities. Although for simple actions, such as moving from one area to another, the descriptions can be easily created, situations in which more complex actions can occur should be investigated.

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