

# Correlation-Model-Based Reduction of Monitoring Data in Data Centers

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**Abstract:** Nowadays, in order to observe and control data centers in an optimized way, people collect a variety of monitoring data continuously. Along with the rapid growth of data centers, the increasing size of monitoring data will become an inevitable problem in the future. This paper proposes a correlation-based reduction method for streaming data that derives quantitative formulas between correlated indicators, and reduces the sampling rate of some indicators by replacing them with formulas predictions. This approach also revises formulas through iterations of reduction process to find an adaptive solution in dynamic environments of data centers. One highlight of this work is the ability to work on upstream side, i.e., it can reduce volume requirements for data collection of monitoring systems. This work also carried out simulated experiments, showing that our approach is capable of data reduction under typical workload patterns and in complex data centers.

## 1 INTRODUCTION

As data centers need to handle large amounts of service requests, in order to optimize efficiency of resource usage, energy consumption and  $CO_2$  emissions, data centers exploit various monitoring systems currently available in industry and as open-source components to understand the dynamic operating conditions. These monitoring systems provide sensing services both on the physical environment and on computing resources, monitoring variables like CPU usage, memory usage, and power consumption as indicators to measure working conditions of virtual machines and host servers.

Even though monitoring systems aim to improve efficiency, the workload for data collection and data utilization can become a heavy burden because the number of virtual machines and hosts in a data center is always large and values of indicators are continuously changing. Furthermore, in the era of Big Data, the size and energy consumption of data center are also increasing owing to expansion of the Internet. Future growth of data centers will doubtlessly raise several challenges to the monitoring systems, such as efficiency and cost of data acquisition, data transmission, data storage and so on. In short, the increasing size of data is becoming a key problem.

As a proposal in the direction of reducing this problem, we explore data reduction technologies to

reduce data quantity and keep abundant informative values. This work focuses on monitoring data of data centers, and most data are numerical time-series data, namely, the representation of a collection of values obtained from sequential measurements over time (Esling and Agon, 2012). While other reduction techniques try to bring down costs of data storage or data transmission, this paper looks at the data reduction problem from a different point of view: indicators of data center are not standalone, their correlations reflect characteristics of system behaviors somehow. We consider the common data correlations between indicators as important clues to large amount of data redundancy, which can be reduced at low cost, so reducing only correlated data could avoid much aimless computation and achieve reduction result at a good level. Thus, we introduce a novel approach to exploit correlations between indicators and predict values of some indicators with regression formulas, aiming to decreasing workloads of data collection in monitoring systems. Compared to other reduction techniques, this prediction method could work on the upstream side (namely, data collection) of data streams. Furthermore, for monitoring systems and other information systems driven by massive data, reducing the upstream means reducing workloads, including data acquisition, data transmission, data storage and so on.

The paper is organized as follows. In Section 2, we introduce related work of time series data reduc-

tion. In Section 3, we introduce the concept of correlation model and structure of our framework, and details on the predictor and regression models. We analyze the prediction power of regression formulas in simple controlled conditions in Section 4, involving several typical workload patterns. In Section 5, we study the predictor performance in a complex simulated data center under daily workloads.

## 2 RELATED WORK

Time series data are collected in various domains, and how to reduce the massive data size has become a main line of research. Dimension reduction techniques have been proposed in past few decades, such as PCA (Principal Component Analysis) (Jolliffe, 2002), PAA (Piecewise Aggregate Approximation) (Keogh et al., 2001), and many projects also used signal transformations like DFT (Discrete Fourier Transform), DWT (Discrete Wavelet Transform), etc.

Some projects also used common statistical methods. In (Ding et al., 2015), a clustering method for large-scale time series data called YADING exploits random sampling and PAA to simultaneously reduce multivariate data in both time and dimension directions. The Cypress framework (Reeves et al., 2009) substitutes the single raw data stream with several sub-streams which can support for archival and simple statistical query of massive time series data.

Even though those techniques give solutions to the reduction problem of time series data in information theory, they still have very limited usage in real projects of many domains, because their lack of semantic information cause much aimless computation. Furthermore, in the WSN (Wireless Sensor Network) domain, some projects exploit correlation-based methods to reduce data traffic in networks, the work of (Carvalho et al., 2011) improves prediction accuracy of sensing data based on multivariate spatial and temporal correlation, and (Zhou et al., 2015) presents an adaptation scheme using sensors of different types to enhance the system fault tolerance. However, those two methods assumes that the correlations between variables are static, while the reality is not.

CloudSense (Kung et al., 2011) propose a switch design on the data center network topology, which exploits compressive sensing to lower monitoring data transmission. CloudSense aggregates status information in each switch level and finally provides a general status report of the whole data center, allowing early detection of relative anomaly. However, this work is not able to reduce data collection volume, and only

the applications of relative anomaly detection can use the compressed outputs, ruling out other possibilities.

An initial version of Correlation-Model Based Data Reduction (CMBDR) framework was proposed in (Peng, 2015), to reduce data by building piecewise regression models for correlated data on the basis of priori knowledge. Based on that proposal, this work elaborates CMBDR further and develops techniques to enable the application of this approach in data centers. Aimed to reduce upcoming data streams, we exploit indicators relation networks of data center to adapt CMBDR to the specific scenario, and design an online predictor based on CMBDR for dynamic streams.

## 3 DATA REDUCTION METHOD

This section illustrates the correlation-based approach of data reduction, which uses regression formulas between correlated indicators, to reduce sampling rate of some indicators, and to reconstruct monitoring data stream with formulas and other indicators. Section 3.1 introduces the data center indicator network proposed in the literature (Vitali et al., 2015), based on which we build our initial correlation model to provide guidance to reduction process. In Section 3.2, the correlation model based data reduction method is presented. Then Sections 3.3 and 3.4 give details on the stream predictor design and regression techniques respectively.

### 3.1 Data Center Indicators Relation Network

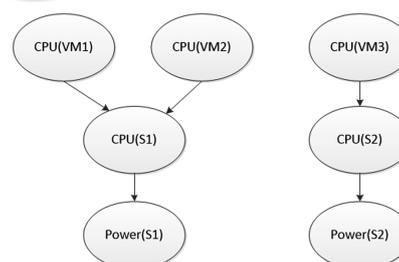


Figure 1: The indicators relation network (Vitali et al., 2015).

In (Vitali et al., 2015), an indicator network is proposed to understand the behavior of monitoring variables in data centers. The indicator network model aims to illustrate relations among indicators and provide adaptation actions that lead data center to a better state. The model consists of two layers: goal

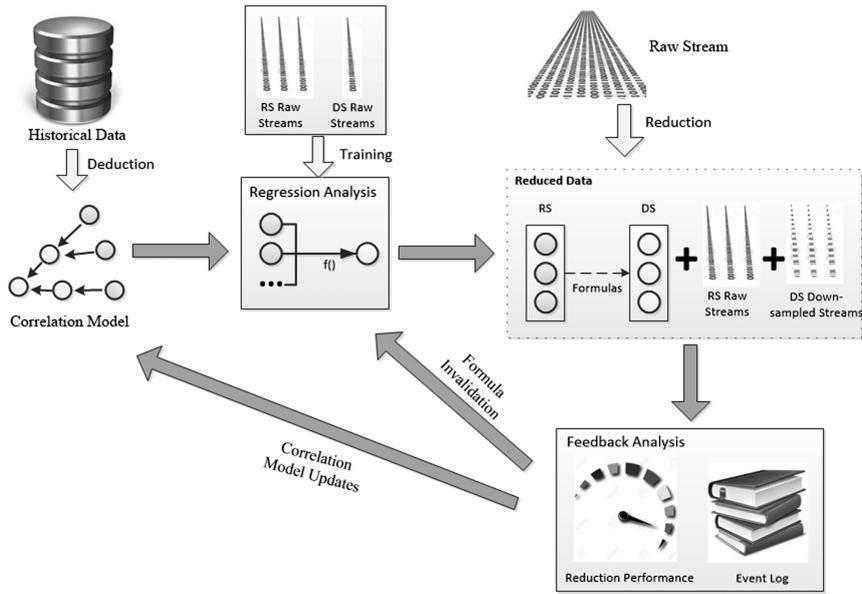


Figure 2: CMBDR prediction framework.

layer and treatment layer, but this paper only introduces the goal layer as depicted in Figure 1, because it indicates the knowledge of data correlations. Instead of using a human expertise, the indicators network automatically learns from historical data. First, possible relations between indicators are learned by putting a threshold over their Pearson correlation coefficients; then a MMHC-like algorithm (Tsamardinos et al., 2006) is applied to orient all network edges; finally a Bayesian Network is derived from monitored data, depicting relations among indicators. Thus, as the starting point of this paper, this Bayesian Network model (a DAG) provides correlations between indicators learned from historical data and it gives an initial input to the data reduction. This paper only takes advantage of the DAG to serve as a model illustrating correlations, called correlation model, and a directed edge from indicator  $A$  to indicator  $B$  in the model implies that values of  $B$  are conditionally dependent on  $A$ , thus we could make predictions of  $B$  based on the value of  $A$ .

### 3.2 CMBDR Framework

Data centers monitor a variety of variables continuously, so values of each variable are in time-series, among which most are numerical values. In this paper, we refer those numerical variables as indicators, and we consider the reduction problem of multiple indicators streams. Denoting the set of all indicators as  $S$ , this reduction method proposes to use a subset of  $S$ , referred as *Regressor Indicators Set (RS)*, to predict values of other indicators, denoted as *Dependent In-*

*dicators Set (DS)*. We try to find a function  $F$  to quantify the relation between  $DS$  and  $RS$  as Equations 1, 2 show, so that data of dependent indicators can be reduced. Namely on the micro level, each dependent indicator  $di_m \in DS$  requires a formula  $f$  to reproduce itself based on values of several regressor indicators  $ri_n \in RS$ , called *Correlated Regressor Set (CRS)*, as Equations 3, 4 show. This work achieves two goals:

- Identify appropriate  $RS/DS$  and  $CRS$ , derive accurate prediction formulas for dependent indicators;
- Reduce data volume of dependent indicators in data collection.

$$DS = S - RS \quad (1)$$

$$DS = F(RS) \quad (2)$$

$$di_m = f(ri_1, ri_2, \dots, ri_l) \quad (3)$$

$$CRS[di_m] = \{ri_1, ri_2, \dots, ri_l\} \quad (4)$$

With known correlations provided by the correlation model and  $RS/DS$  configuration, CMBDR recurses correlations in the DAG to identify  $CRS$ , and performs regression analyses on values of correlated indicators in a short period (called training window), to find a formula fitting the quantitative relations of these variables. Thus values of the dependent indicator  $di_m$  can be reproduced by the formula and correlated indicators  $CRS[di_m]$ , achieving data reduction. This framework conducts model-based reduction in an online manner, which adjusts the correlation model and the reduction process based on performance feedback. Depicted in Figure 2, CMBDR separates reduction process into several iterations of the following four main steps.

- *correlation Model Deduction*: Derive the indicators correlation model for the data center as Section 3.1 illustrated, assign  $RS/DS$  and select the correlated regressor indicators  $CRS[di_m]$  for each dependent indicators  $di_m$ ;
- *Regression Formula Learning*: Train a formula for each dependent indicator to quantify their relations with regressor indicators.
- *Dependent Indicators Reduction*: Reduce sampling rate of dependent indicators, and adopt predictions of the formulas to replace lost samples.
- *Feedback Analysis*: Evaluate the performance of the reduction process, and try to find possible problems and solutions to improve it.

The correlation model deduction is based on the indicator relation network illustrated in Section 3.1, which specifies highly-correlated indicators. We generate this indicators network under a variable workload, in order to find workload independent correlations. We consider the correlations as a consequence of interconnections of data center modules, for instance, the CPU usage of a virtual machine is always correlated to the CPU usage of its host. So we extract the DAG of the relation network as correlation model, and with help of this model, we can identify several indicators capable of predicting dependent indicators. Then we assign the nodes of DAG to  $RS/DS$ , and select correlated regressor indicators  $CRS[di_m]$  of  $di_m$  by algorithm 1. This algorithm selects regressor indicators  $ri \in RS$  to predict the dependent indicator  $di \in DS$  if  $ri$  has a directed path  $p$  to  $di$  in the DAG, and no other regressor indicators exist on the path  $p$ . The selection of  $RS/DS$  and  $CRS$  has obvious impacts on reduction performance, so in order to minimize the size of  $RS$ , we select root nodes of the DAG as regressor indicators of the first loop, and select other nodes as dependent indicators. And if the reduction performance is poor under current  $RS/DS$  configuration, we update the  $RS/DS$  in the following loops according to feedback analysis results. In addition, the correlation model is not static in the framework, we need to recompute it if some indicators are added or removed in the monitoring system.

In the regression formula learning step, in order to quantify relations between indicators, we exploit regression techniques on correlated indicators. A training window of streaming data is fetched for each group of indicators as selected in the first step, then linear regression analysis is carried out, deriving a prediction formula  $f$  that can reproduce values of the dependent indicator.

Then in the dependent indicators reduction step, formulas make predictions to replace raw samples of

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Algorithm 1: Select regressor set for each dependent indicator  $di_m$ .

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**Require:**  $RS, DS, DAG(V, E)$

**Ensure:**  $CRS$  {the set of correlated regressor indicators of each  $di_m$ }

**Function** *SelectCRS*

Stack  $stack := \emptyset$

**for**  $ri$  in  $RS$  **do**

$stack.push( neighbors(ri) )$  {find neighbors that are linked by an edge from current node  $v$ }

**while**  $stack \neq \emptyset$  **do**

$v := stack.pop$ ;

**if**  $v$  is in  $DS$  **then**

$CRS[v].add(ri)$

$stack.push( neighbors(v) )$

**else**

continue

**end if**

**end while**

**end for**

**return**  $CRS$

**End Function**

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the dependent indicators partially. As Figure 2 depicts, sampling rates of dependent indicators are reduced to a lower level, and the lost samples are replaced by the formula predictions, which are derived out of the values of regressor indicators. Furthermore, we compare samples of the dependent indicators to prediction results, providing a glimpse of accuracy performance. Therefore, the final reduced data is composed of several parts, namely, all raw samples of regressor indicators, training samples and checking samples of dependent indicators, and formulas parameters.

Finally, the framework performs feedback analyses, in which reduction performance and the event log of the data center are analyzed to generate feedbacks, helping to improve the next loop. Reduction performance is evaluated with combined-criteria, covering compression ratio, execution time and informative value. By spotting the indicators and formulas with poor performance, we identify problems in each loop iteration, so we can update the corresponding regression formula and correlation model to improve performance. In addition, events in the log can also guide reduction process to adapt to the changes of the data center environment. For instance, in the feedback analysis, if we found a virtual machine is added to or removed from a host server in feedback analysis, then we need to recompute the correlation model before running the next loop. Details will be discussed in Section 5.

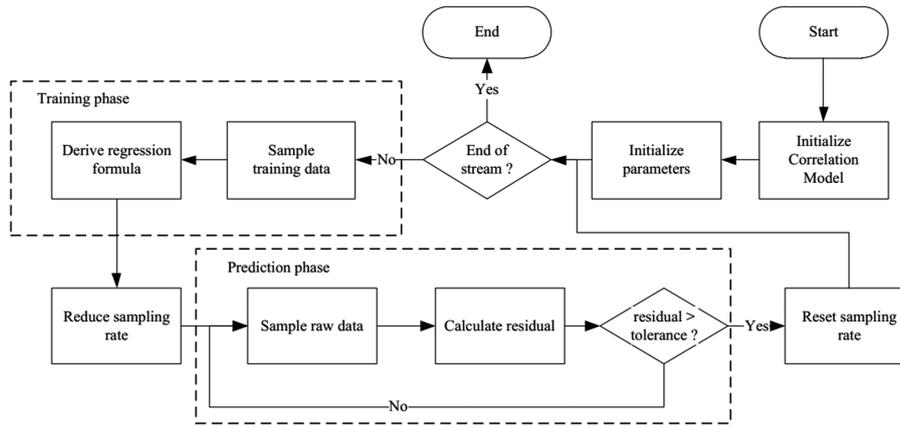


Figure 3: Predictor workflow.

### 3.3 Indicators Stream Predictor

This section explains the design of the indicators stream predictor in detail, which is a first implementation of the CMBDR framework. Based on the correlation model, the predictor tries to figure out formulas of indicators by regression analysis on training dataset, and reduces their sampling rate to a low level to serve as check items. Its working procedures mainly include two phases: training phase and prediction phase, the predictor always trains the formulas in training phase, and then verifies the formulas in prediction phase. If a prediction result does not match the sample result, then a prediction failure is generated as feedback and the corresponding formula needs to be recomputed in the next training phase. The predictor workflow is depicted in Figure 3. Before predictor running, the correlation model is initialized and some parameters are configured. Afterwards training phase starts, predictor carries out regression analysis for each formula which involves the dependent indicator  $di_m$  and also correlated regressor indicators  $ri \in CRS[di_m]$ . Subsequently, we cut down sampling rate of dependent indicators in the prediction phase. Then we compare each sample with prediction results, and if their difference (residual) exceeds predefined tolerance, the prediction will be considered as a failure and the prediction phase of this formula will be terminated. Finally, a new training phase starts unless the predictor has reached the end of the stream. In order to control efficiency and accuracy of the reduction process, we introduce three important parameters to the predictor:

- *Length of Training Data Set*: the number of samples required to train a formula, denoted as  $LT$ ;
- *Prediction Tolerance*: the range for prediction errors (or residuals) within which the prediction will

not be considered as a failure, denoted as  $PT$ ;

- *Prediction Sampling Rate*: sampling rate for dependent indicators in prediction phase, denoted as  $SR$ , which should be generally smaller than the original sampling rate.

### 3.4 Linear Regression Method

To achieve our goal, the adopted reduction methods should have the competence to derive quickly the quantitative relationship between indicators in a time slot, and to predict future values of some indicators. In this approach, we explore methods of regression analysis to discover formulas quantifying the relationships and predicting values of dependent indicators based on regressor indicators. Considering the time to find fitting regression models of streaming indicators, the computation complexity of regression analysis must be limited. Thus, CMBDR should give preference to the regression model with the least time complexity, namely, the linear regression model.

Generally, linear regression is an approach modeling linear formulas between scalar dependent variables and independent variables. While multiple linear regression attempts to model the relationship between two or more independent variables and a response variable by fitting a linear equation to observed data (see Equation 5), simple linear regression is a special case of multiple linear regression having only one independent variable (see Equation 6). In the two equations, suppose data consists of  $n$  observations  $\{y_i, x_{i1}, \dots, x_{ip}\}_{i=1}^n$ , then  $x_{ij}$  means the  $j^{\text{th}}$  independent variable measured for the  $i^{\text{th}}$  observation,  $y_i$  means the response variable measured for the  $i^{\text{th}}$  observation,  $\alpha$  is called intercept,  $\beta_j$  are called slopes or coefficients,  $\epsilon_i$  are an unobserved random variable that adds noise to the linear relationship.

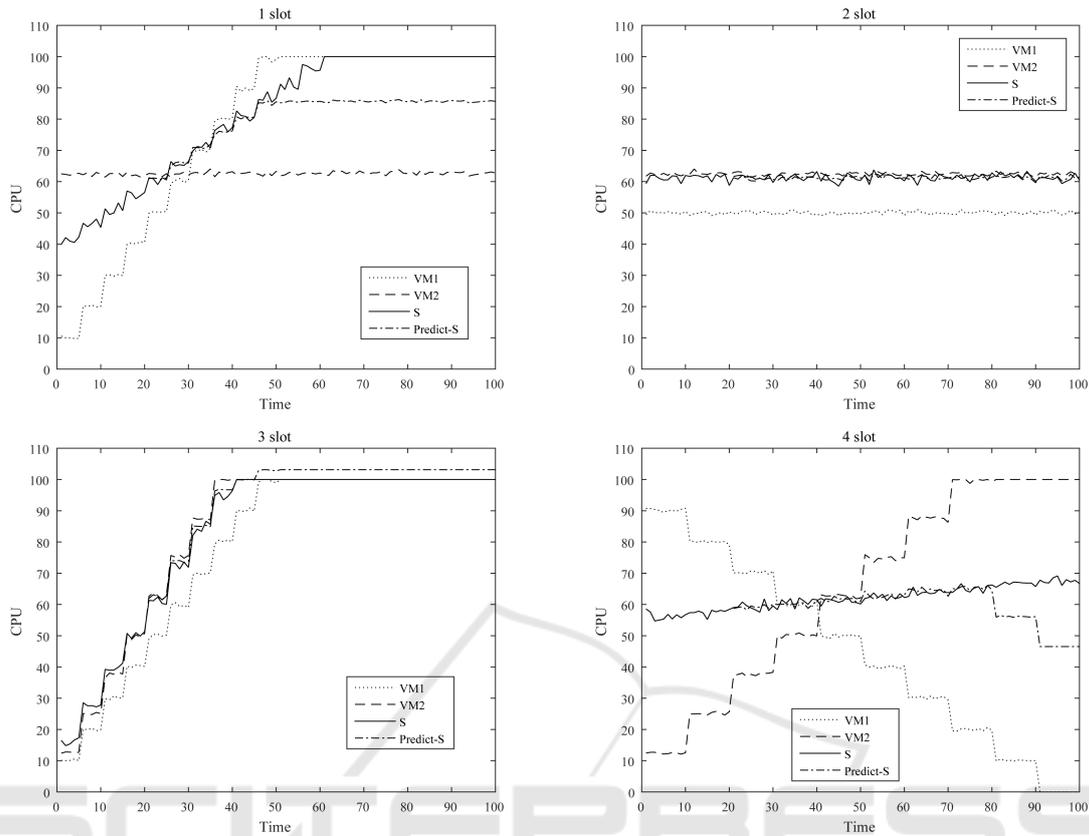


Figure 4: CPU ratios in four patterns ( $VM_1$  - dotted lines,  $VM_2$  - dashed lines,  $S$  - solid lines, Prediction of  $S$  - dash-dot lines).

$$y_i = \alpha + \beta_1 x_{i1} + \dots + \beta_p x_{ip} + \epsilon_i \quad (5)$$

$$y_i = \alpha + \beta_1 x_i + \epsilon_i \quad (6)$$

If  $X$  (the matrix of  $x_{ij}$ ) is full column rank, CMBDR uses OLS (Ordinary Least Squares) regression method to estimate parameters of the formula minimizing  $SSR$  (sum of squared residuals) over all possible values of the intercept and slopes, as shown in Equation 7. Details of OLS method can be found in (Hayashi, 2000). If  $X$  is not full column rank, then some column vectors must be linearly dependent, thus CMBDR applies Gaussian Elimination to get the full column rank matrix and then applies the OLS method.

$$SSR = \sum_i (y_i - \alpha - \beta_1 x_{i1} - \dots - \beta_p x_{ip})^2 \quad (7)$$

#### 4 PREDICTION FORMULA VALIDATION

Regression analysis derives the prediction formula that best fits training datasets. Therefore, this formula could maintain a high prediction rate on following testing data until the quantitative relation changes

and prediction rate dramatically decreases. So understanding when the relation will change is quite important for predictor performance. In this section, in order to get insights into behaviors of the predictor, we study prediction failures of the regression formulas under certain controlled conditions, by designing several particular patterns to model typical situations in data centers and validating prediction formulas in each situation.

Experiments are conducted in MATLAB with a data center simulation framework (Vitali et al., 2013). With proper settings of the simulated data center, we are able to control the framework to generate monitoring data under specific workload, thus we can evaluate performance of the predictor on various conditions.

We prepare a simple data center environment with 2 virtual machines (VM) deployed on 1 host server (S), and CPU usages of VMs are and S are all 3 indicators, in which  $CPU(VM_1)$  and  $CPU(VM_2)$  are regressor indicators and  $CPU(S)$  is dependent indicator. Furthermore, 4 slots of monitoring data are generated under different workload patterns of VMs, as Figure 4 illustrates, to simulate possible workload conditions of the data center. In the first slot, workload of  $VM_1$  increases while  $VM_2$  remains the same, but

Table 1: Indicators configurations in the first loop.

Indicator	Description	Unit	Indicator set	Regressor Indicators
$CPU(VM_{ij})$	CPU ratio of $j_{th}$ VM deployed on $S_i$		RS	
$R(VM_{ij})$	Response time of $j_{th}$ VM deployed on $S_i$	ms	DS	$CPU(VM_{ij})$
$P(VM_{ij})$	Instant power consumption of $j_{th}$ VM deployed on $S_i$	watt	DS	$CPU(VM_{ij})$
$CPU(S_i)$	CPU ratio of $S_i$		DS	$CPU(VM_{i1}) \cdots CPU(VM_{i6})$
$P(S_i)$	Instant power consumption of $S_i$	watt	DS	$CPU(VM_{i1}) \cdots CPU(VM_{i6})$

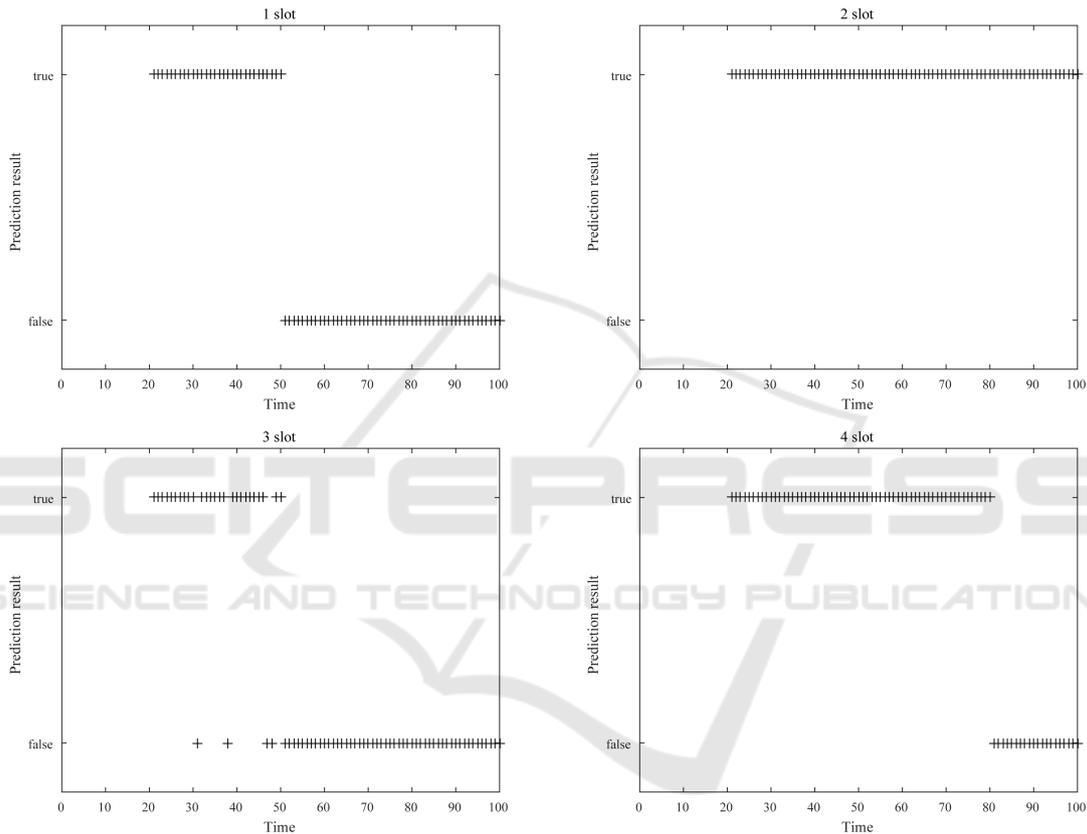


Figure 5: Prediction results in four patterns.

due to the resource limits, the indicators  $CPU(VM_1)$  and  $CPU(S)$  stop increasing when CPU ratios reach 100%, which means the workload requests have exceeded the processing power. In the second slot, two VMs workloads remain unchanged, so all indicators remain stable. In the third slot, both VMs increase their workloads at almost same speed; in the last slot,  $VM_1$  increases workload while  $VM_2$  decreases, and the CPU usage of the host  $CPU(S)$  grows slowly.

Each slot consists of 100 samples, and the starting 20 samples are used to train a prediction formula, which will be tested by all samples left. Applying the threshold (Prediction Tolerance) to the residual between sample and prediction, a boolean result is gen-

erated, as Figure 5 depicts. In the beginning, all prediction formulas perform well since most predictions are accurate. Nevertheless, in pattern 1, 3, 4, the prediction accuracy decreases suddenly afterwards and it reveals a significant change of indicators relation. This happens when CPU ratio of a VM reach 100% so it has to stop the previous trend.

These sudden relation changes can be explained by overload conditions of VMs and the server. When a VM get overloaded, the real CPU consumption of the VM is still increasing even if monitored indicator  $CPU(VM)$  remains at 100%, because VM can acquire additional resource from the host server. Thus, the previous prediction formula cannot explain cur-

rent overload situations, for instance, from the middle part of the first slot, the prediction remains stable since  $CPU(VM_1)$  and  $CPU(VM_2)$  remain unchanged, but the indicator  $CPU(S)$  is still increasing because the real workload request of  $VM_1$  does not stop increasing.

This experiment demonstrates two outcomes. First and most importantly, the regression formula of correlated indicators is capable of making accurate predictions in certain conditions. Secondly, the quantitative relations between indicators are not static, and they evolve with dynamic data center environment. Considering these two outcomes, in CMBDR framework, we exploit regression formula to capture temporary quantitative relation between correlated indicators, and model feedback loops to adapt to dynamic changes of formulas and correlations.

## 5 EXPERIMENTAL STUDY

In this section, we discuss experimental results of the described approach to assess the performance of CMBDR framework. We conduct experiments in the same simulation tool of data center, which creates a virtualized data center environment and allows the collection of simulation data at different workload rates. This tool emulates VMs resource allocation on servers and generates monitoring data such as resource usage and power consumption under certain workload rates. It also estimate power consumption of a VM based on the amount of CPU it consumes.

### 5.1 Experiment Setting

To reveal the performance of CMBDR predictor, we test it in a larger data center. This data center consists of 100 servers with 6 VMs deployed on each server. Monitoring data stream includes 2000 indicators that cover CPU usage, response time and power consumption of both VMs and servers. As Table 1 depicts, in the initial reduction loop of CMBDR framework, we select root nodes (namely,  $CPU(VM_{ij})$ ) of the correlation model as regressor indicators, and take other nodes as dependent indicators. Testing data are generated by the simulation tool under simulated daily workloads, with sampling rate of 1 per minute (1440 samples in one day).

As an important parameter of the predictor, prediction tolerance  $PT$  defines the threshold for prediction errors and has a great influence on reduction results. In this work, the value of  $PT$  is directly based on the measurement error of raw monitoring data. We first put the data center in a stable work-

load conditions, and collect values of indicators for a period. Therefore, the multiple samples are repeated measurements on the same state of the data center, they should follow normal distribution around the true value  $\mu$  and variance is  $\sigma^2$ , as Equation 8 depicts. Therefore, we exploit the 95% confidence interval (approximately  $1.96 \times \sigma$ ) as a criteria for error behavior of raw samples, and assign it to  $PT$  as Equation 9 shows. We consider the raw sample and the corresponding prediction as two observations on the same indicator, and if the difference between these two observations is within the 95% confidence interval, this prediction could be viewed as an accurate measurement, namely, a true prediction.

$$measurement \sim N(\mu, \sigma^2) \quad (8)$$

$$PT = 1.96 \times \sigma \quad (9)$$

### 5.2 Evaluation Criteria

In order to evaluate the indicator stream predictor comprehensively, this work proposes combined evaluation criteria covering operation speed, reduction volume and informative values of reduced data. Information value is a general term describing the ability of reduced data for supporting target applications; it could be distinct for wide varieties of applications. Thus, we exploit multiple metrics instead of a single criterion to measure informative values. Details of the combined evaluation metrics are as follows.

- *Execution Time*: processing time for the predictor to reduce prepared data stream.
- *Reduction Volume*: the difference between raw data size and reduced data size.
- *Hit Rate*: Consider the prediction within the error range of raw data as a hit, thus the hit rate is the percentage of accurate predictions, which reflects informative values of reduced data.
- *Relative Error*: this metric measures information loss of data reduction process, as shown in equation 10, for each indicator,  $\eta$  is relative error,  $\epsilon$  is absolute error and  $v$  is the interval of the values in the test dataset.

$$\eta = \frac{\epsilon}{v} \quad (10)$$

- *Weighted mean of  $R^2$* :  $R^2$  is often used to measure total goodness of fit of linear regression models, as equation 11 depicts,  $y_i$  is raw value and  $f_i$  is prediction value. and  $R^2 = 1$  indicates that the regression line perfectly fits raw data. In this work,  $R^2$  is used to measure accuracy in each prediction phase, and length-based weighted average of

Table 2: Prediction performance of formulas in the same category.

	$R(VM)$	$P(VM)$	$CPU(S)$	$P(S)$	$P(S)revision$
Relative error	3.45E-03	1.97E-03	4.82E-02	4.86E-02	1.19E-04
Average $R^2$	0.889	0.917	0.220	0.208	1.000
Hit rate	95.96%	98.57%	82.01%	81.85%	100.00%
Reduction volume	1241.46	1304.32	900.37	893.20	1339.25
Execution time sec.	0.144 s	0.070 s	0.680 s	0.690 s	0.029 s

those  $R^2$  on data stream will be used as a metric to evaluate how well predictions fit raw data.

$$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - f_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2} \quad (11)$$

### 5.3 Formulas Revisions

In the experiment, we monitor the reduction process, and measure performance of each formula using the aforementioned criteria. One interesting point we found is that the variability of prediction ability is significant between formulas. Some formulas can make very accurate predictions in a short execution time while some formulas fail frequently and cost more time to train new formulas. The reason for this discrepancy lies in the correlation model. In the reduction process, if a prediction formula does not meet accuracy requirements, then the predictor needs to learn a new regression formula to replace it, thus the formula could be always up-to-date. However, some dependent indicators may be hard to predict by selected regressor indicators, if their correlations are not high enough. Thus, the framework would take much time to update those formulas frequently, even though the general performance increases very little.

Therefore, in order to solve the problem, the predictor need to revise those inefficient formulas in the next reduction loop. We denote dependent indicators of those foot-dragging formulas as *slowDS*, and we need to expand *RS* to include a subset of *slowDS* to enhance prediction ability, since results have proved current *RS* is not capable of making accurate predictions on those indicators. Among all possible solutions, adding the complete set of *slowDS* to *RS* can solve the issue all at once, but obviously it can only achieve minimal data reduction. This work reconsiders correlations between indicators of *slowDS* in the correlation model, it obtains several disconnected subgraphs of the *DAG* containing only the *slowDS* nodes, and add the root nodes of subgraphs to *RS*. For instance, if any indicators of *slowDS* are correlated, they must exist in the same subgraph, thus the corresponding root node would serve as the regressor indicator for other nodes in the next loop; otherwise

all *slowDS* will serve as regressor indicators. By this gradual means of expanding *RS*, appropriate *RS/DS* could be identified in iterations of reduction loops.

In this experiment, CMBDR framework selects the root nodes of correlation model as *RS* in the first loop. Individual performance of indicators in the first loop are evaluated in the first 4 columns of Table 2, each column representing the average performance of indicators in the same category. Under initial *RS/DS* configuration, the indicators of  $R(VM_{ij})$  and  $P(VM_{ij})$  outperform evidently  $CPU(S_i)$  and  $P(S_i)$ , with higher reduction volume, better prediction accuracy and much less execution time. To acquire better performance in the second loop iteration, we need to update *RS/DS*. By querying in the correlation model, we find  $CPU(S_i)$  and  $P(S_i)$  are highly correlated. Then we just move one indicator  $CPU(S_i)$  from *DS* to *RS*, and then call Algorithm 1 to update regressor set *CRS* for  $P(S_i)$ , thus  $CPU(S_i)$  would be used to predict  $P(S_i)$  in the second loop. The performance are also measured, as the fifth column in Table 2 shows, both accuracy and execution speed are improved dramatically and the relative error is at the same level with  $P(VM_{ij})$ .

We also measure overall reduction performance of monitoring data in reduction process, to verify the validity of this predictor and to assess the improvement offered by *RS/DS* updates. As Figure 6 depicts, in both first and second loops, the predictor reduces the raw monitoring data to slightly above one-third of original volume, and reduction of 2 loops are nearly the same although the predictor involves more regressor indicators in the second loop. However, these new regressor indicators improve processing speed and accuracy performance of the predictor dramatically. As Figure 7 and Figure 8 show, the second loop doubles processing speed of the first loop, and increases average prediction accuracy by almost an order of magnitude. Results of the second loop in Figures 7, 8 also illustrate that, for a data center of 2000 indicators, this predictor is able to reduce daily monitoring data within 100 seconds, ensuring the average relative error at  $10^{-3}$ .

Above all, this predictor could cut down the volume of data collection in monitoring systems, while

still maintaining fast speed and a good quality of informative values.

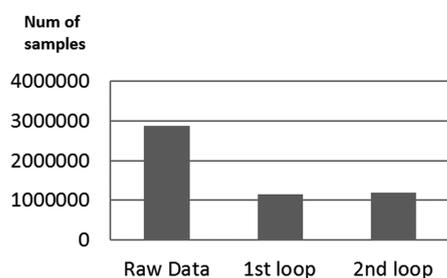


Figure 6: Data volume before and after reduction.

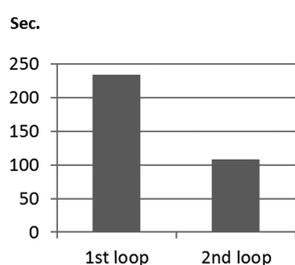


Figure 7: Execution time of CMBDR loops.

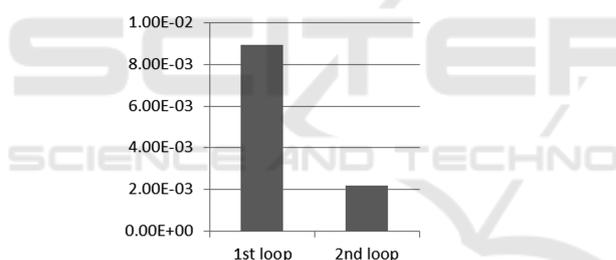


Figure 8: Average relative error of the predictor.

## 6 CONCLUSIONS

In this work, we developed and implemented a data reduction framework for a data center monitoring system. We derived the correlation model of indicators, and based on correlations, we built a stream predictor to decrease sampling of raw data by deducing quantitative relations between indicators. We have also designed the feedback loop in the reduction process, which evaluates and optimizes reduction performance in iterations, enhancing adaptability of the correlation model and formulas in a dynamic environment. Validation results show that regression formulas can predict indicators under typical workload patterns, and predictor test results demonstrate that this approach is capable of reduction in a simulated data center. This mechanism could provide an extension to other

solutions in terms of upstream data reduction, and it serves as a practical solution for monitoring data streams in which variables are commonly correlated. Future work may be carried on data center anomaly detection, or fault-tolerant mechanisms of monitoring data, which also exploits data correlations to establish standby channels in monitoring systems, as in (Zhou et al., 2015).

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