

Methods of Data Processing and Communication for a Web-based Wind Flow Visualization

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Keywords: Wind Flow Visualization, Wind Fields, Data Tiles, Data Reduction, Data Compression, Difference-coding.

Abstract: This paper presents methods for the reduction and compression of meteorological data for web-based wind flow visualizations, which are tailored to the flow visualization technique. Flow data sets represent a large amount of data and are therefore not well suited for mobile networks with low data throughput rates and high latency. Using the mechanisms introduced in this paper, an efficient transfer of thinned out and compressed data can be achieved, while keeping the accuracy of the visualized information almost at the same quality level as for the original data.

1 INTRODUCTION

In weather forecasts, the expectable wind in its speed and direction is an important forecast parameter. Wind speeds and directions are therefore common elements on geographical weather maps and are visualized within meteorological applications in the shape of wind barbs or flow vectors. The wind barb indicates the wind direction and speed in a compact form at a specific location on a weather map. Flow vectors depict the same information as wind barbs, but it is harder to discern the magnitude when viewing vectors. Overall, for non-expert users it is difficult to interpret these representations of wind flows and they often cannot decide in which direction the wind is blowing. Moreover, it is also difficult to get an impression of how wind conditions will change during the next hours as both representations do not change the position of the wind elements on the map but modify their direction and speed only.

In the web, wind forecasts are most commonly represented and transferred in form of images. These images do not offer any interactivity, making it difficult for users to get a quick impression of wind flows. Due to this, changes in time are not visible in a proper way. A naive method to approach this issue is to use video in order to play back a sequence of consecutive weather conditions. This would, however, result in a large amount of data required to be delivered to the client causing high delays and costs, especially in mobile contexts. Moreover, such an approach does not

improve anything on the users' comprehension and on the interactivity of the visualization, when it is still based on wind barbs or flow vectors.

In order to solve this problem, a wind flow visualization has been developed that improves the visualization of wind flows on different zoom levels by showing a streamlines movie illustrated by animated particles. Such a wind flow visualization is more attractive and has been designed in a distinctly interactive manner. Based on wind vector fields, the developed wind flow visualization is able to render wind flows in real-time within web browsers without the use of plug-ins, providing the impression of a video. Moreover, this wind flow visualization is executable on mobile devices requiring the transfer of bare meteorological data only. Although this is already much more efficient and resource saving than a video-based approach, the involved meteorological base data is still a large amount of data required to be transmitted to the client. Hence, the goal of this work is to compress and simplify the bare wind data so as to achieve an optimal balance between the amount of data required to be transferred and a still accurate visualization rendered in an acceptable time frame.

The remaining of this paper is organized as follows. Section 2 provides a brief introduction on meteorological wind data structures in order to lay the foundations. Section 3 discusses the related work on reduction and compression methods in respect to meteorological data. In order to achieve the targeted goal of a cost-efficient and accurate animated wind flow vi-

sualization, a combination of distinct data processing methods have to be applied. In Section 4 these methods for reducing and compressing the meteorological data are described in detail. The evaluation results of the proposed scheme are presented and discussed in Section 5. The paper concludes by summarizing the main achievements in Section 6.

2 FOUNDATIONS

The meteorological data have been taken from the Integrated Forecast System (IFS) provided by the European Centre for Medium-Range Weather Forecasts (ECMWF,). For the flow visualization, wind fields at a height of 10 meters above the ground are used. The meteorological data lie on a regular grid with a 0.125° longitude by 0.125° latitude resolution. Wind fields in a forecast are available at 3-hourly intervals and are selected for 17 discrete points in time for a region of Europe (62° north - 33.5° north, 11° west - 35° east) with 369 by 229 grid points as shown in Figure 1.

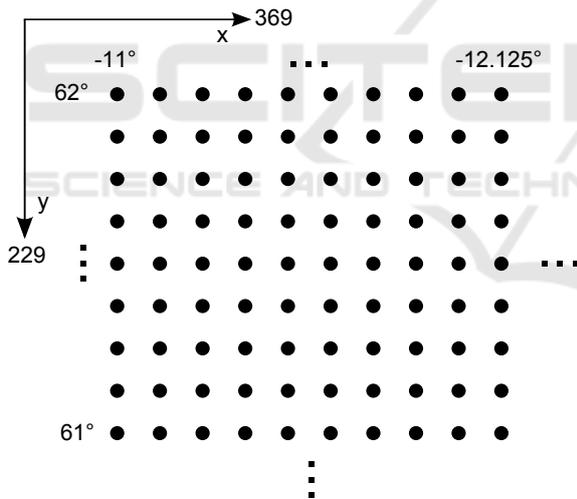


Figure 1: Meteorological data represented in a regular grid.

For the projection of the meteorological data, a rectangular projection has been used as the conversion of a geographical coordinate into an image coordinate is simple and the relations between the directions north-south and west-east are linear. The data is projected on two different layers and four zoom steps and is valid for every zoom step. The layers are available as tiled maps and can be requested as sprites.

The meteorological data has been analyzed with a view to the data structure and exchange format required for them to be transferred to the client. One solution is the transfer of complete vector fields. Be-

cause the wind flows are visualized in a view port, the other solution is the transfer of tiled data. Thus only visible data needs to be load. This data is represented in JSON format (Crockford, 2006). Each point in time within a forecast represents a JSON object, which additionally contains meta-data for the client side's processing and projection. All wind vectors of one wind field are placed in a single linear array. The meta-data object contains a date for each point in time, the grid width and height, the distance between two grid points in x and y direction, a unique Id and one reference pixel for the projection of tiled data mapped as name/value pairs. In order to minimize the amount of data, no position data for the projection is transferred, but only one reference point.

The data can be requested over a REST-ful HTTP (Tilkov et al., 2015) interface as a single file or as a package with a defined amount of points in time and are transferred over HTTP protocol. In addition to HTTP compression, web caching is extremely useful to improve loading time of not modified data. It decrease HTTP traffic, lessen server workload, and reduce the latency perceived by end users (Souders, 2007). Because HTTP runs over a TCP connection not only the amount of data plays an crucial role, but also especially in mobile networks the HTTP performance. By the way how TCP estimates the capacity of a connection leads in high latency in mobile networks. Each connection takes a full round-trip of latency between the client and the server. Using persistent connections and pipelining can reduce this latency. Persistent connections allow for a reuse of connections. When a client and a server have established a TCP connection, the client can send GET requests to the server to retrieve some resources. If the client wants further resources from the server, they will have to issue multiple GET requests, sequentially, on a persistent TCP connection. Before the client can issue an additional request, it has to wait for the previous request to complete. To improve this, request pipelining allows for a parallel request processing. Consequently, the client can send multiple requests simultaneously to the server. Following this, it will incur a minimum of another round-trip of latency (Grigorik, 2013).

3 RELATED WORK

Methods for data compressing can be classified into two classes. The first class includes methods for lossless compression, which reconstruct the original data completely out of the compressed one. In contrast to that, the second class contains lossy compression

methods, which can not fully reconstruct the data after being compressed. Methods of the latter class separate significant from less important information and compress the substantial data only. Due to that, these methods are able to achieve higher compression rates with the disadvantage to only reach an approximation of the original data after reconstruction.

Different lossless data compression techniques exist and are used in many applications, depending on the resource type, such as text, images, videos and so forth. For the compression of data in the web, the most common compression schemes in HTTP are GZIP (Deutsch, 1996b) and DEFLATE (Deutsch, 1996a). The compression can be selected by the HTTP request header field *Accept-Encoding* (Fielding et al., 1999).

Data reduction methods remove a portion of data points or combine various high spatial resolutions to reduce the data volume. Various methods exist to reduce the amount of data, which can be adapted for a reduction of the available meteorological data. In computer graphics and in meteorology, clustering of data is one way to reduce the large amount of data. A large number of wind vectors of the original high-resolution wind field can be combined through a weighted averaging into fewer wind vectors that approximately represent the wind field at a coarser resolution, leading to a visualization of clustered data with similar wind speeds and wind directions (Telea and van Wijk, 1999), (Lodha et al., 2000), (Lazarus et al., 2010).

Furthermore, the most intuitive and most commonly used approach for reducing the data is given by uniform thinning. In this technique, data is retained by systematically selecting one of every N th data point regardless of its relative importance. This subsampling is referred to as non-adaptive thinning, but it is used in many applications due to its simplicity. Although straightforward and intuitive, non-adaptive data thinning can result in a degraded forecast because it does not discriminate between regions of high and low information content. But this method yields robust data reduction anyway. Further non-adaptive strategies are simple thinning, which also includes random data points sampling, and subsampling with averaging, where multiple data points are averaged into a single data point (Hansen and Johnson, 2005), (Lazarus et al., 2010).

Moreover, intelligent thinning algorithms systematically select high regions in a wind field or high wind vectors, which could have a strong effect on the wind flow visualization. Low regions or wind vectors with less information content are subsampled to reduce the amount of data (Ramachandran et al., 2005).

In video compression, different methods are used for reducing data. MPEG involves techniques such as difference coding and motion prediction, where the similarity between consecutive frames in a video stream is used to achieve a higher compression rate. MPEG classifies each frame in a sequence as a certain type of frame, such as an I-frame, P-frame or B-frame. An I-frame (Intra picture) is coded independently without any reference to other pictures and is always the first picture in a video sequence. A P-frame (Predictive picture) is coded based on previous I or previous P pictures, while a B-frame (Bi-directionally predictive pictures) is coded based on either the next and/or the previous pictures (Reimers, 2008). In this context it is possible to use relations between consecutive wind fields in a forecast to minimize the total amount of data to be compressed.

4 DATA REDUCTION AND COMPRESSION

Compression techniques for meteorological data are motivated by the necessity of transferring large flow data sets over networks with low bandwidth and high latency with the goal of producing visualizations of the data in low-end mobile devices. This fact has motivated for reducing and compressing the meteorological data. The aim is a combination of a lossless with a lossy compression to reduce the meteorological data.

4.1 Thinning Procedure

The purpose of data thinning is to reduce the number of characters used to represent meteorological data within JSON format. In this context data thinning reduces the number of grid points. Some techniques maintain a regular grid, which improve the client side processing. For instance clustering of the meteorological data might lead to an irregular grid. In this context, position data for the similar grid points must be calculated for a projection on the client side. However, no position data will be transferred. Besides, a non-linear interpolation must be performed for reconstructing the data. The meteorological data are neither scattered or bundled nor incomplete. Therefore, the use of random subsampling, subsampling with averaging or intelligent thinning algorithms might result in inconsistent distances between the grid points. Because of non-linear interpolation on the client side, the reconstruction of an irregular grid is more costly than the reconstruction of a regular grid.

Given is a discrete vector field as a set of wind vectors. Thus a simple subsampling can be used for

the thinning of the available meteorological data. The aim of the reduction method is to construct a new discrete representation of the vector field containing fewer points. The advantage is that the spatial resolution can be reduced while a regular grid can be maintained. As a consequence, the geographical distance or the pixel pitch between grid points respectively are increased inversely proportional in x and y directions. The more data are thinned, the more data need to be reconstructed on the client side. Figure 2 shows the simple thinning procedure.

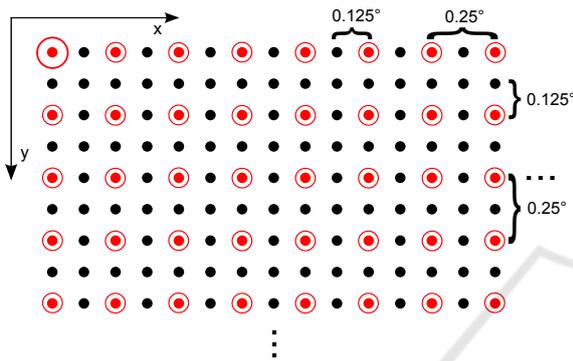


Figure 2: Uniform thinning of a wind field.

The grid points (red circles) are selected in an equidistant distance in x and y directions starting from a reference grid point (red big circle). Unselected grid points are subsampled. In this case, every second grid point is selected. Thus the geographical distance increases from 0.125° to 0.25° . For simple thinning, an equivalent retention rate is obtained by selecting every N th observation in the x and y directions, whereby a thinning factor N can be derived. This factor indicates in which distance a grid point is selected in x and y direction. In this case, the use of the simple thinning can be considered as compression: missing grid points of the thinning procedure are reconstructed on the client side by the interpolation for a high spatial resolution so as to create smooth curves. Thus the meteorological data are an approximation of the original data.

In addition to that, decimal places of the wind vectors get shortened for a further reduction.

4.2 Difference Coding Procedure

The method for a temporal reduction performs a difference coding on wind fields depending on a reference wind field. In this context, each wind vector is considered separately. For the determination of differences in wind speed and wind direction, both have to be considered separately for each wind vector. This difference coding is based on the transfer of refer-

ences instead of differences. Based on the differences, it is decided whether data are transferred or not. This follows from the fact that a wind vector field completely changes in time. Although wind vector fields show differences in temporal direction no further efficient reduction can be achieved. Because meteorological data are transferred in a JSON format, thus it is not possible to achieve a further reduction by transferring differences of wind vectors, because no characters were effeminate to achieve a reduction.

The differences in speed are calculated by an absolute speed deviation between two temporally consecutive wind vectors. Deviations in wind direction are calculated by the angle between two wind vectors. The first wind field in a forecast is always used as the reference wind field, which is independent without any reference to other wind fields.

If deviations between a reference wind vector and a following wind vector are less than a defined threshold for wind speed and wind direction, a reference on this reference wind vector will be transferred instead of the following wind vector. Furthermore, the reference wind vector is maintained and is used for the next wind vector of the next wind field. If the deviations are greater than the threshold for wind speed and wind direction, the following wind vector will be defined and transferred as a new reference wind vector.

The threshold for deviations in speed and direction is determined by the evaluation of the thinned data. Any calculation of differences occurring on all temporally consecutive wind fields always refers to the reference wind field. Figure 3 shows the encoding and decoding procedure on a sequence of a forecast.

In Figure 3, R represents a reference wind field and C represents a coded wind field at a given point of time. (a) Any wind field at a given t is coded by itself and the reference wind field. In the same processing step, a new reference wind field is created which is valid for the following coding steps. (b) Only the first reference wind field and the given coded wind fields of this reference are transferred. (c) On the client side, coded wind fields are decoded. The references within a wind field are replaced by the respective wind vectors of the preceding reference wind field. In the same processing step, a new reference wind field is created which is valid for following wind fields. The reference wind fields are always visualized.

For the transfer of a reference, the vector components are replaced by a 0. An integer takes slightly less memory in a JSON than a double. References are written on the same position where the original wind vector was placed. JSON allows the transfer of *null* values, but it is more meaningful to transfer a

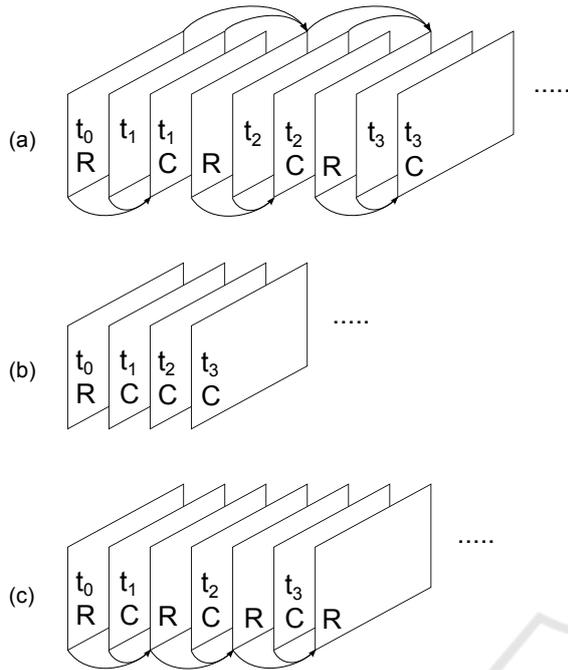


Figure 3: Difference coding procedure: (a) encoding procedure, (b) transfer of coded meteorological data and (c) decoding procedure.

0 to avoid errors on the client side. By that means, the difference coding is optimized to achieve a higher lossless compression rate due to the large number of repeated values.

The compression rate of this method depends on changes of the wind fields in time. An optimal compression rate can be achieved by low temporal changes. If large changes in time are available, a lower compression rate will occur. Due to this method, it is possible to transfer regions in a wind field with strong changes in time only. Thus, a higher compression rate can be achieved.

5 EVALUATION

This section presents experimental results of the proposed reduction and compression strategies, which have been applied to the meteorological data. Table 1 lists the results of the thinning procedure and the data compression for the grid resolutions and the generated JSON file sizes. Additionally, the sum over all wind fields of the available point of times is listed. The results show that the large amount of data can be reduced in an efficient way. By shortening the decimal places, data can be reduced by up to 48%. In addition to that, by thinning and lossless data compression a very high compression rate can be achieved

Table 1: Resolution and file size of reduced and compressed wind fields with different thinning factor N .

N	Grid Size	\varnothing File Size [KB]	\varnothing GZIP [KB]	\varnothing $\Sigma 17$ [KB]	\varnothing GZIP [KB]	Reduction [%]
Reference	369x229	1370	373	23282	6333	-
All	369x229	716	181	12165	3071	87
2	185x115	181	51	3066	859	96
3	124x77	82	24	1378	408	98.25
4	93x58	46	15	788	261	98.88
5	75x47	31	10	531	176	99.24
\vdots						
10	38x24	8	3	142	55	99.76

for a given N .

When thinning-out with a factor of $N = 3$ in conjunction with a lossless data compression, a data reduction of 98.25% has been achieved. Thus the meteorological data can be transferred as single point of time or as package. Table 2 reflects the number and file size of tiled meteorological data based on a thinned wind field with $N = 3$.

Table 2: Tiled data based on a thinned wind field with thinning factor $N = 3$.

Number of Data Tiles	Tile Grid Size	\varnothing File Size [Byte]	\varnothing GZIP [Byte]	\varnothing $\Sigma 17$ [Byte]	\varnothing GZIP [Byte]
126	10x10	1177	643	17190	5141
54	15x15	2036	917	31567	9677
28	20x20	3451	1361	55991	15163

An appropriate number of 28 data tiles with a tile grid size of 20x20 grid points has been exposed. Furthermore, it was investigated which thinning factor provides the most acceptable results to achieve a visualization with acceptable information. The wind fields were evaluated in terms of an absolute mean speed and direction deviation and in terms of a root mean square error in vector differences between the reference wind field and a thinned wind field for every zoom step. Based on deviations and RMS, no meaningful statement can be given on which thinning factor is suitable to achieve a visualization with acceptable information. Because of this, a visual evaluation is required to determine a threshold for the reduction to reach a visualization with acceptable information for the user. In this evaluation, it was investigated from which thinning factor on differences between the original data and thinned data are perceptible. Table 3 shows the results of the statistical evaluation summarized across all zoom steps.

Since the deviations of the thinned data across all zoom steps showed the same results, it is possible to use one version of a wind field for every zoom level. The results of the thinning procedure show that the accuracy of the thinned wind fields generally degrades as more grid points are removed as expected. It has been found that low wind vectors are more affected by the thinning procedure in contrast to stronger wind

Table 3: Statistical evaluation results on deviations in speed and direction.

N	\bar{d} [m/s]	σ_d [m/s]	$\bar{\varphi}$ [°]	σ_φ [°]	RMS
2	0.13	0.19	2.51	7.26	0.29
3	0.23	0.31	4.67	11.46	0.5
4	0.33	0.41	6.57	14.55	0.69
5	0.42	0.51	8.13	16.73	0.86
⋮					
10	0.79	0.86	14.14	23.41	1.53

vectors, but this does not affect the visualization. Figure 4 shows difference images of thinned data in wind directions and in wind speeds with $N = 3$. The results show that strong differences of the reconstructed data can be seen.

Although a thinning factor of $N = 3$ already gives a marginal mean RMS of 0.51, the visual comparison as given by Figure 7 between the original data and the thinned data by $N = 3$ illustrates that hardly any differences can be perceived. Only in regions with very low wind speeds, minimum differences were perceived. When using more thinned data, the results showed more and more perceivable differences. In comparison to that, an $N = 10$ gives a mean RMS of 1.54. Thus it is not possible to achieve a visualization with acceptable accuracy.

In this case, differences are even perceived in regions of strong wind speeds as shown in Figure 5. The limit of the thinning procedure is located at a thinning factor of $N = 3$ to guarantee a visualization with acceptable information.

Based on the deviations of the statistical results, a further efficient compression can be achieved by applying difference coding to the wind fields. The parameters for the difference coding are based on the deviations of the thinning factor of $N = 3$. The parameters were slightly varied to achieve an acceptable result. A still acceptable result with the highest compression can be achieved with parameters of $d_u < 0.5$ m/s and wind direction deviations $d_\varphi < 10^\circ$. Table 4 shows the compression results of a time series for the given parameters wind speed deviation $d_u < 0.5$ m/s and wind direction deviation $d_\varphi < 10^\circ$.

Figure 6 shows a comparison of original data on the left side and decoded data on the right side for t_3 . The results show that hardly any differences can be perceived, so that a further reduction up to 50% can be achieved while an acceptable visualization can still be guaranteed as shown. Furthermore, the lossless compression in the transfer protocol can achieve a higher mean compression rate by up to 9% for the coded data in comparison to the original data.



Figure 4: The image on the top visualizes the differences between the original data set and the thinned-out data set by $N = 3$ in respect to the wind directions. The bottom images visualizes the differences between the original data set and the thinned-out data set by $N = 3$ in respect to the wind speeds.

Furthermore, to determine whether acceptable load times can be reached, the load time of the flow visualization with meteorological data were measured over the mobile networks 2G, 3G and 4G. To measure the load time, three tests have been performed over a persistent connection with pipelining. At this point, a compromise should be found between the amount of data to be transferred and the number of requests the server must handle. For the first test case, the application and unreduced data were requested. For the second test case, the application and complete wind



Figure 5: Comparison between original data (left) and thinned data (right) with $N = 10$.

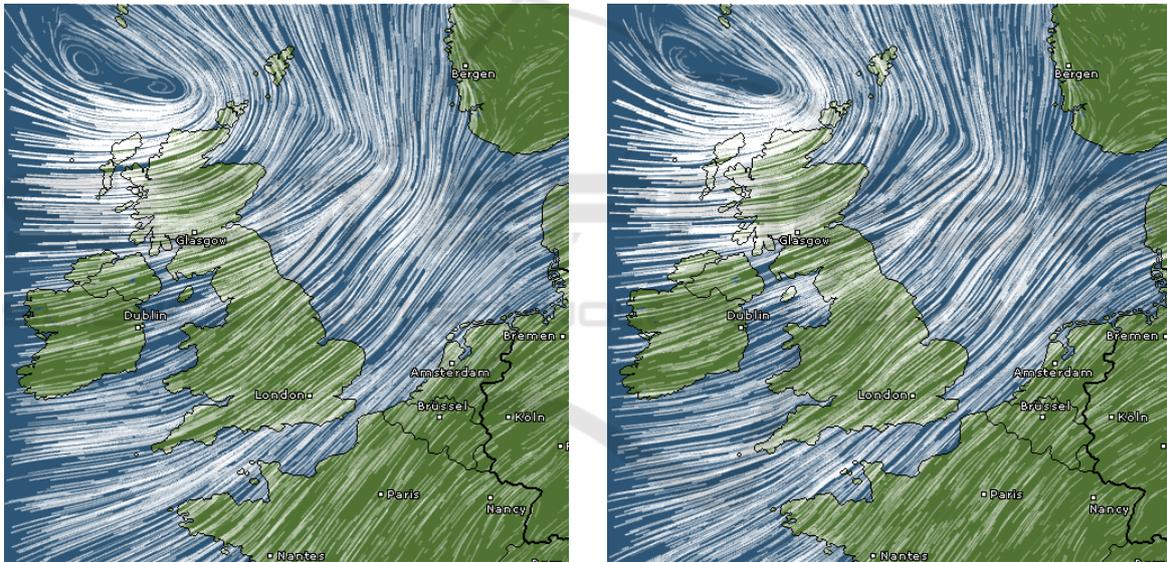


Figure 6: Visual appearance comparison between original data (left) and difference-coded wind field (right) with $d_u < 0.5$ m/s and $d_\phi < 10^\circ$.

Table 4: Data transfer volume reduction with a wind speed deviation $d_u < 0.5$ m/s and a wind direction deviation $d_\phi < 10^\circ$.

t	File Size [KB]	Coded Size [KB]	Reduction [%]	RMS	Original GZIP [KB]	Coded GZIP [KB]
0.5	81.4	42.8	47	0.43	24.2	4.75
1	81.4	52.6	35	0.46	24.3	11.2
1.5	81.4	50.9	37	0.54	24.1	10.8
2	81.4	56.9	30	0.45	24.3	14.1
2.5	81.4	50.4	38	0.53	24.3	10.4
3	98.8	66.2	33	0.44	34.5	19.8

fields were requested which were reduced and losslessly compressed. For the third case, the application and data tiles were requested which were reduced and

losslessly compressed. In addition, four tiled layers were requested and a lossless compression over the transfer protocol is performed for all test cases. Test case one and two had to create 13 requests to load all data for every zoom step for a) one or b) all wind fields in a forecast. In comparison, test case three had to create 14 requests to load all data for a map section of every zoom step for a) one or b) all wind fields in a forecast. In this case, two data tiles were loaded and additionally 26 further requests would have had to be created for the complete map section of every zoom step. Table 5 reflects the measured load times for each test case with 100 repeated measurements re-

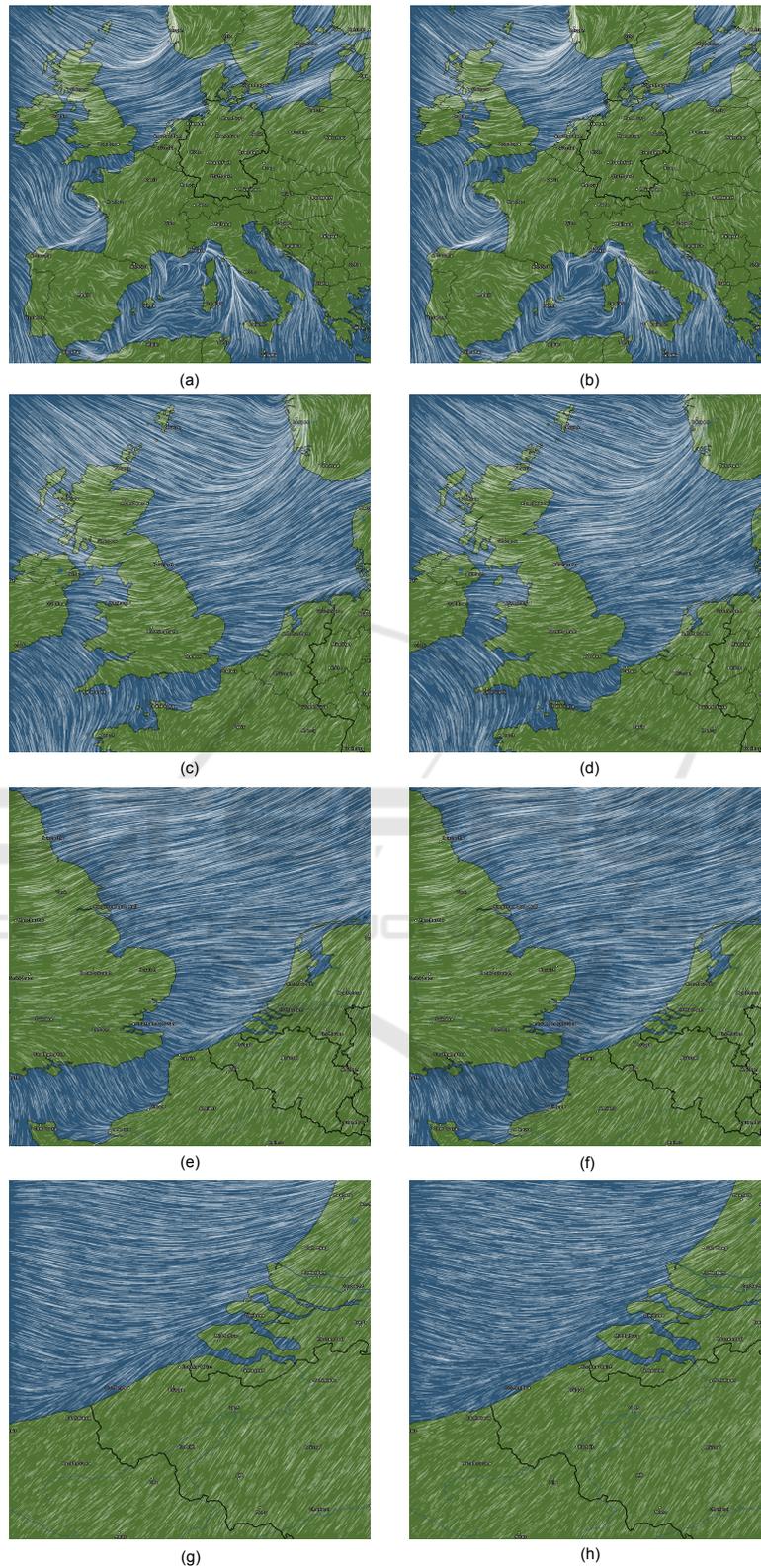


Figure 7: Comparison of original and thinned data with $N = 3$: (a) zoom step 0 with original data; (b) zoom step 0 with thinned data; (c) zoom step 1 with original data; (d) zoom step 1 with thinned data; (e) zoom step 2 with original data; (f) zoom step 2 with thinned data; (g) zoom step 3 with original data; (h) zoom step 3 with thinned data.

Table 5: Transfer times for different mobile networks.

Network	Transfer Time [s]					
	Test Case 1		Test Case 2		Test Case 3	
	a) 527 KB	b) 6487 KB	a) 178 KB	b) 562 KB	a) 156 KB	b) 184 KB
2G	29.38	405.32	11.37	33.24	11.07	15.21
3G	1.69	7.32	1.07	1.63	1.07	1.19
4G	1.49	6.77	0.88	1.45	0.88	1.01

spectively.

The results show that for test case one and generally via any 2G network, no acceptable load times can be achieved. In comparison to that, for the test cases two and three, acceptable load times result in a range, which will be tolerated by the users. A study has shown that a waiting time of approximately two seconds is still tolerated by the users (Nah, 2004). Moreover, the results show faster load times than the current trend of mobile page load times of approximately seven seconds (Jain and Tikir, 2013). Furthermore, with the use of difference-coded data, load times could be further improved.

6 CONCLUSION

This paper introduces the need of a wind flow visualization and the associated effort of transmission over mobile networks. The problem is addressed by the large amount of data. The results show that it is possible to achieve a reduction of up to 98% through the combination of lossy and lossless compressions for a thinning factor of $N = 3$. It is thereby possible to produce an almost constant visualization in comparison to the original data. In this case, minimal non-perceptible differences can occur in regions of low wind speeds. In addition to that, a further reduction can be reached through an appropriated threshold by using difference coding. At this point, no general compression rate can be specified, because difference coding depends on changes in time. In context of the achieved reduction, it is possible to transfer meteorological data within acceptable times over mobile networks. Thus users get a fast first impression of the wind flow visualization. In summary, it is recommended to reduce the data with an $N = 3$ and to use tiled data with difference-coded wind fields for the transfer over mobile networks because of the reduced amount of data to be transferred. For a desktop application, a higher spatial resolution can be used and data can be transferred as complete wind fields. Moreover, in future a performance analysis of HTTP/2.0 in mo-

bile networks might be a treated topic, which unlike operates much better than HTTP/1.1 (de Saxce et al., 2015).

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