A Linear-dependence-based Approach to Design Proactive Credit Scoring Models

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Abstract: The main aim of a credit scoring model is the classification of the loan customers into two classes, reliable and unreliable customers, on the basis of their potential capability to keep up with their repayments. Nowadays, credit scoring models are increasingly in demand, due to the consumer credit growth. Such models are usually designed on the basis of the past loan applications and used to evaluate the new ones. Their definition represents a hard challenge for different reasons, the most important of which is the imbalanced class distribution of data (i.e., the number of default cases is much smaller than that of the non-default cases), and this reduces the effectiveness of the most widely used approaches (e.g., neural network, random forests, and so on). The Linear Dependence Based (LDB) approach proposed in this paper offers a twofold advantage: it evaluates a new loan application on the basis of the linear dependence of its vector representation in the context of a matrix composed by the vector representation of the non-default applications history, thus by using only a class of data, overcoming the imbalanced class distribution issue; furthermore, it does not exploit the defaulting loans, allowing us to operate in a proactive manner, by addressing also the cold-start problem. We validate our approach on two real-world datasets characterized by a strong unbalanced distribution of data, by comparing its performance with that of one of the best state-of-the-art approach: random forests.

1 INTRODUCTION

The actions related to a lending process typically involve two entities: the institution that provides the loan, and the customer that benefits from it. Such process starts from a loan application and it ends with the repayment (or not repayment) of the loan. If, on the one hand, the retail lending represents one of the most profitable source for the financial operators, on the other hand, the increase of the loans is directly related to the increase of the number of defaulted cases, i.e., fully or partially not repaid loans.

Briefly, the *credit scoring* is used to classify the loan customers into two classes, *accepted* or *rejected*, on the basis of the available information. It is therefore an important tool for the financial operators, since it allows them to reduce the financial losses, as stated in (Henley et al., 1997). More formally, *credit scoring* can be defined as a statistical technique aimed to predict the probability that a loan application (from now on named as *instance*) leads toward a default (Mester et al., 1997), thus it is used to decide if a loan should be granted to a customer (Morrison, 2004).

The analysis performed by the *credit scoring* is also useful to evaluate the *credit risk* (i.e., probability of loss from a customer's default), because it takes into account all the factors that contribute to determinate it (Fensterstock, 2005). It presents some other advantages, such as the reduction of the credit analysis cost, a quick response time in the credit decisions, and the possibility to perform a punctual monitoring of the credit activities (Brill, 1998).

indent Such as it occurs in other similar contexts, e.g., *fraud detection* (Pozzolo et al., 2014), the development of effective approaches for *credit scoring* comes up against a big problem: the unbalanced distribution of data. It happens because the number of negative cases (i.e., default instances) is typically much smaller than the positive ones (i.e., non-default instances), configuring a highly unbalanced distribution of data (Batista et al., 2004) that reduces the effectiveness of the machine learning strategies (Japkowicz and Stephen, 2002).

The vision behind this paper is to represent the instances as a vector space, and to define a metric able to evaluate, in this space, the correlation between a new instance and the other previous non-default ones,

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in order to evaluate its level of reliability.

This metric is based on the concept of linear dependence between vectors, considering that a set of vectors is linearly independent if no vector in it can be defined as a *linear combination*¹ of the other ones, we believe that *if the vector representation of a new instance is linearly dependent to the vector representations of the previous non-default ones, we can consider it as reliable.*

We perform this process by calculating the determinant of the matrix composed by the vector representation of the past non-default instances and that of a new instance to evaluate, by placing its vector representation as the last row of the matrix. Whereas the determinant does not exist for the non-square matrices, we introduce a criterion that allows us to extend this calculation even to these cases.

Given that in most of the cases reported in the literature (Lessmann et al., 2015; Brown and Mues, 2012; Bhattacharyya et al., 2011) the *Random Forests* approach outperforms the other ones in this context, we will compare the proposed approach only to this one.

The main contributions of this paper to the state of the art are the following:

- (i) formalization of the Average of Sub-matrices Determinants (*ASD*) criterion used to evaluate the linear dependence of the vector representation of an instance in a vector space, also when
- it configures a non-square matrix that not allows us to calculate its determinant;
- (ii) calculation of the *Reliability Band* β , which gives us information about the linear dependence variations in an *ASD* process that only involves non-default instances;
- (iii) definition of the *Linear Dependence Based* (*LDB*) approach of evaluation of new instances, performed by exploiting the β information to classify them as *accepted* or *rejected*;
- (iv) demonstration of how the *LDB* approach is able to achieve very similar (or better) results in terms of performance, when compared to a state-of-the-art approach such as *Random Forest*, by working in a proactive manner (i.e., without using default cases), overcoming the *cold-start* and the imbalanced class distribution problems.

This paper is organized as follows: Section 2 discusses the background and related work; Section 3

¹When one of the vectors is a scalar multiple of the other.

provides a formal notation and defines the problem faced in this paper; Section 4 describes the implementation of our *credit scoring* system; Section 5 provides details on the experimental environment, the adopted datasets and metrics, as well as on the used strategy and the experimental results; Some concluding remarks and future work are given in Section 6.

2 BACKGROUND AND RELATED WORK

A large number of *credit scoring* classification techniques has been proposed in literature (Doumpos and Zopounidis, 2014), as well as many studies aimed to compare their performance on the basis of several datasets, such as in (Lessmann et al., 2015), where a large scale benchmark of 41 classification methods has been performed, across eight *credit scoring* datasets.

The problem of choosing the most suitable approach of classification, and tuning its parameters in the best way, has been faced in (Ali and Smith, 2006), which also reports some interesting considerations about the canonical metrics of performance used in this context (Hand, 2009).

2.1 Credit Scoring Models

Most of the statistical and data mining techniques at the state of the art can be used in order to build *credit scoring* models (Chen and Liu, 2004; Alborzi and Khanbabaei, 2016), e.g., linear discriminant models (Reichert et al., 1983), logistic regression models (Henley, 1994), neural network models (Desai et al., 1996; Blanco-Oliver et al., 2013), genetic programming models (Ong et al., 2005; Chi and Hsu, 2012), k-nearest neighbor models (Henley and Hand, 1996) and decision tree models (Davis et al., 1992; Wang et al., 2012).

These techniques can also be combined (Wang et al., 2011) to create hybrid approaches of *credit scoring*, as that proposed in (Lee and Chen, 2005), based on a two-stage hybrid modeling procedure with artificial neural networks and multivariate adaptive regression splines, or that presented in (Hsieh, 2005), based on neural networks and clustering methods.

2.2 Imbalanced Class Distribution

A complicating factor in the *credit scoring* process is the imbalanced class distribution of data (He and Garcia, 2009), caused by the fact that the default classes (default instances) are much smaller than the other ones (non-default instances). Such distribution of data reduces the performance of the classification techniques, as reported in the study made in (Brown and Mues, 2012).

Another study about the introduction of misclassification costs during the processes of scorecard construction and classification was performed in (Vinciotti and Hand, 2003), where the authors have also discussed the possibility of preprocessing the dataset of training, by performing an *over-sampling* or an *under-sampling* of the classes. The application of the *over-sampling* and *under-sampling* processes has been studied in depth in (Marqués et al., 2013; Crone and Finlay, 2012).

In this paper we do not perform any class balancing, since our intention is to evaluate the proposed approach in the context of an unaltered real-world dataset.

2.3 Cold Start

The *cold start* problem (Zhu et al., 2008; Donmez et al., 2007) arises when there are not enough information to train a reliable model about a domain (Lika et al., 2014; Son, 2016; Fernández-Tobías et al., 2016).

In the credit scoring context, this happens when there are not many instances related to the creditworthy and non-credit-worthy customers (Attenberg and Provost, 2010; Thanuja et al., 2011).

Considering that, during the model definition, the proposed approach does not exploit the data about the defaulting loans, it is able to reduce/overcome the aforementioned issue.

2.4 Random Forests

Random Forests represent an ensemble learning method for classification and regression that is based on the construction of a number of randomized decision trees during the training phase and it infers conclusions by averaging the results. Since its formalization (Breiman, 2001), it represents one of the most common techniques for data analysis, because it offers better performance in comparison with the other state-of-the-art techniques.

It allows us to face a wide range of prediction problems, without performing any complex configuration, since it only requires the tuning of two parameters: the number of trees and the number of attributes used to grow each tree.

2.5 Matrices, Linearity, and Vector Spaces

The concepts of matrix determinant, linearity, and vector spaces, cover a primary role in this paper, since we use them to formalize and prove the correctness of the proposed similarity metric based on the linear dependence between vectors.

The matrix determinant (*det*) is a mathematical function that assigns a number to every square matrix, so its domain is the set of square matrices, and its range is the set of numbers; more formally, we can write that $det : \Re^n \times \ldots \times \Re^n \to \Re$.

Regardless of the method used to calculate the determinant of a square matrix $N \times N$ (e.g., by the *Leibniz* formula shown in Equation 1, where *sgn* is the sign function of permutations σ in the permutation group S_N , which returns +1 and -1, respectively for even and odd permutations), its value is related to the relation of linear dependence between the vectors that compose the matrix.

$$det \begin{vmatrix} m_{1,1} & m_{1,2} & \dots & m_{1,N} \\ m_{2,1} & m_{2,2} & \dots & m_{2,N} \\ \vdots & \vdots & \ddots & \vdots \\ m_{N,1} & m_{N,2} & \dots & m_{N,N} \end{vmatrix} = \sum_{\sigma \in S_N} sgn(\sigma) \prod_{i=1}^N m_{i,\sigma_i}$$
(1)

The dependence of the *N* vectors can be verified by calculating the determinant of the $N \times N$ matrix built by placing, one after the other, the n-tuples that express the vectors in a certain base. The vectors are independent when the determinant of the matrix is different from zero.

A vector space (or linear space) is a mathematical structure composed by a collection of vectors that may be added together and multiplied (or, more correctly, scaled) by numbers called scalars. In other words, a vector space V is a set that is closed under finite vector addition and scalar multiplication. A vector sub-space (or linear sub-space) is a vector space that represents a subset of some other vector space of higher dimension.

3 NOTATION AND PROBLEM DEFINITION

This section introduces the notation adopted and defines the problem faced by our approach.

3.1 Notation

Given a set of classified instances $T = \{t_1, t_2, ..., t_N\}$, and a set of fields $F = \{f_1, f_2, ..., f_X\}$ that compose each *t*, we denote as $T_+ \subseteq T$ the subset of non-default instances, and as $T_- \subseteq T$ the subset of default ones.

We also denote as $\hat{T} = {\hat{t}_1, \hat{t}_2, ..., \hat{t}_M}$ a set of unclassified instances, and as $E = {e_1, e_2, ..., e_M}$ these instances after the classification process, thus $|\hat{T}| = |E|$.

Each instance can belong to one class $c \in C$, where $C = \{accepted, rejected\}.$

3.2 **Problem Definition**

On the basis of the *linear dependence*, measured by calculating the determinant of the matrices composed by the vector representation of the non-default instances in T_+ and that of the unclassified instances in \hat{T} , we classify each instance $\hat{t} \in \hat{T}$ as *accepted* or *rejected*, by exploiting a *Band of Reliability* β , defined on the basis of the proposed *LDB* approach.

Given a function $eval(\hat{t},\beta)$ used to evaluate the classification performed by exploiting the β information, which returns a boolean value σ (0=wrong classification, 1=correct classification), our objective can be formalized as the maximization of the results sum, as shown in Equation 2.

$$\max_{0 \le \sigma \le |\hat{T}|} \sigma = \sum_{m=1}^{|\hat{T}|} eval(\hat{t}_m, \beta)$$
(2)

4 OUR APPROACH

The implementation of our strategy is carried out through the following steps:

- 1. **Data Normalization:** normalization of the F values in a range [0,1], to make homogeneous the range of involved values, regardless to the considered field or dataset, without losing information;
- 2. **ASD Definition:** definition of the *Average of Submatrices Determinants* (*ASD*) criterion, used to evaluate the linear dependence in a square and non-square matrix of vectors;
- Reliability Band Calculation: calculation of the *Reliability Band* β, on the basis of the ASD crite- rion, an information used to evaluate the level of reliability of the new instances;
- 4. **Instances Classification:** formalization of the *Linear Dependence Based (LDB)* process needed to classify (as *accepted* or *rejected*) a set of unevaluated instances, by exploiting the *ASD* criterion and the β information.



Figure 1: LDB - High-level Architecture.

In the following, we provide a detailed description of each of these steps, since we have introduced the high-level architecture of the proposed *LDB* approach. It is presented in Figure 1, where T_+ , \hat{T} , and *E*, denote, respectively, the set of non-default instances, the set of instances to evaluate, and the set of classified instances at the end of the process (i.e., those in \hat{T}).

4.1 Data Normalization

As first step, we normalize all values F in the datasets T and \hat{T} in a range [0, 1]. It allows us to make homogeneous the range of involved values, regardless to the considered field or dataset. Such operation could be also useful in order to avoid potential problems during the determinant calculation, e.g., overflow, in case of very large matrices, by using certain software tools (Moler, 2004).

The process of normalization of a generic value $f_x \in F$ related to an instance $t \in T$ is reported in Equation 3 (the same goes for the set \hat{T}).

$$f_x = \frac{1}{\sum\limits_{\forall f_x \in T} f_x} \cdot f_x \tag{3}$$

4.2 ASD Definition

Given that there is not a mathematical definition of determinant of a non-square matrix, here we introduce the *Average of Sub-matrices Determinants* criterion (*ASD*), which allows us to extract this information in all cases (square and non-square matrices).

It calculates the average of the determinants of all square sub-matrices obtained by dividing the nondefault instance history matrix of size $|T_+| \times |F|$ in α square sub-matrices, whose number depends on the rule shown in Equation 4.

The additional element added to the set T_+ will be used to evaluate an instance in the context of the vector space of the other instances that composed the matrix.

$$\alpha = \begin{cases} \left\lfloor \frac{|F|}{(|T_{+}|+1)} \right\rfloor, & \text{if } |F| \ge (|T_{+}|+1) \\ \left\lfloor \frac{|T_{+}|+1}{|F|} \right\rfloor, & \text{otherwise} \end{cases}$$
(4)

In more detail, we calculate the determinant of each sub-matrix defined by moving (without overlaps) on the matrix $|F| \times (|T_+| + 1)$ by using a step $|T_+| + 1$ (i.e., along the rows), or by moving on the matrix by using a step |F| (i.e., along the columns). The *ASD* value is given by the average of all sub-matrices determinant.

By way of example, if the values are $|T_+| = 1$ and |F| = 6, we have $\alpha = \left\lfloor \frac{6}{1+1} \right\rfloor = 3$ sub-matrices of size 2 × 2, and the *ASD* value is calculated as shown in the Equation 5.

$$ASD\begin{pmatrix} a & b & c & d & e & f \\ g & h & i & l & m & n \end{pmatrix} = \frac{det\begin{pmatrix} a & b \\ g & h \end{pmatrix} + det\begin{pmatrix} c & d \\ i & l \end{pmatrix} + det\begin{pmatrix} e & f \\ m & n \end{pmatrix}}{3}$$
(5)

From now on, we use the notation ASD(X, Y) to denote the *Average of Sub-matrices Determinants* calculated by using as the last row of the sub-matrices the vector (or vectors) in the set *Y*, and for the other rows the vectors in the set *X*.

Practically, the *ASD* value gives us information about the linear dependence between vector segments that characterize the same subset of features, as demonstrated in Theorem 4.2.

Theorem. Given the vector space of the features that characterize the vector representation of transactions in a domain, we can express it as sum of two or more sub-spaces that characterize subsets of features.

Proof. A vector space can be defined as a combination of sub-spaces by using a decomposition approach, e.g., given a space $\Re^3 = x$ -axis+y-axis+z-axis, we can write any $\vec{w} \in \Re^3$ as a linear combination $c_1\vec{v}_1+c_2\vec{v}_2+c_3\vec{v}_3$ (where \vec{v} is a member of the axis, and $c \in \Re$), as shown in Equation 6.

$$\begin{pmatrix} w_1 \\ w_2 \\ w_3 \end{pmatrix} = 1 \cdot \begin{pmatrix} w_1 \\ 0 \\ 0 \end{pmatrix} + 1 \cdot \begin{pmatrix} 0 \\ w_2 \\ 0 \end{pmatrix} + 1 \cdot \begin{pmatrix} 0 \\ 0 \\ w_3 \end{pmatrix}$$
(6)

On the basis of the consideration that $\Re^3 = x$ -axis+y-axis+z-axis, we can prove the consistency



of the proposed ASD approach, since it gives us the mean value of the determinants calculated on a series of square sub-matrices composed by segments of vectors that belong to the same vector sub-space of the items features space.

It simply means that, by the *ASD* information, we are able to evaluate subsets of features (in terms of linear dependence between their vector representations), and the calculation of the mean value of these results gives us a single value that reports the relations of similarity in the entire space of the features, as previously demonstrated.

It should also be observed that the previous considerations remain valid in both cases considered by the Equation 4, because *the determinant of the transpose of any square matrix is the same determinant of the original matrix.*

4.3 Reliability Band Calculation

Denoting as d(t) the ASD value obtained by using as rows of the sub-matrices (except the last row) the nondefault instances in T_+ , and as last row a vector $t \in T_+$, in Equation 7 we define the set Δ of ASD variations.

$$\Delta = \{ d(t_2) - d(t_1), d(t_3) - d(t_2), \dots, d(t_N) - d(t_{N-1}) \}$$
(7)

The *Reliability Band*, denoted as β , is defined by using the average (*avg*), the minimum (*min*) and the maximum (*max*) value of Δ , as shown in Equation 8.

$$\beta = [b_L, b_H] = \left[\frac{avg + min}{2}, \frac{avg + max}{2}\right] \tag{8}$$

It gives us information about the linear dependence variations, when the *ASD* process involves only non-default cases. We use it during the evaluation process, by classifying the cases that generate *ASD* variations outside the β band (the dotted area shown in Figure 2) as potential default cases, according to the process explained in the following Section 4.4.

4.4 Instances Classification

This section starts by formalizing the algorithm used to perform the *Linear Dependence Based (LDB)* process of classification of an evaluated set of instances and it ends with the analysis of its asymptotic time complexity.

4.4.1 Algorithm

The Algorithm 1 takes as input a set T_+ of non-default instances occurred in the past and a set \hat{T} of unevaluated instances, returning as output a set E containing all instances in \hat{T} , classified as *accepted* or *rejected* on the basis of the *ASD* process and the β band (i.e., by using the b_L and b_H values).

Algorithm 1: LDB Instances classification.



In step 2 we calculate the ASD value by using the non-default instances in T_+ as rows of the submatrices (except the last row), and all vectors of the same set as last row (one at a time), as described in Section 4.2.

The *Reliability Band* β (Section 4.3) is calculated in *step 3*.

The *steps* from 4 to 11, process the instances $\hat{t} \in \hat{T}$, by using them to fill the last row of each sub-matrix in the *ASD* process, calculating, in the *step 5*, the variation δ between two instances, following the criterion described in Equation 7.

On the basis of the variation δ and the β band, each instance is classified as *accepted* or *rejected* in the *steps* from 6 to 10, and the result is placed in the set *E*, which is returned at the end of the process (*step* 12).

Considering that the calculation of the linear dependence variations (*step 5*) needs at least two instances, when we evaluate the first instance of the set \hat{T} (or when there is only an instance in this set), we

add an additional instance composed by using the average of each $f \in F$ of the set T_+ , as first instance of the set \hat{T} .

For algorithm readability reasons, we omitted this step, as well as that of the preliminary normalization of the sets T and \hat{T} .

4.4.2 Asymptotic Time Complexity Analysis

In view of a possible implementation of the *LDB* approach in a *real-time scoring system* (Quah and Sriganesh, 2008), where the *response-time* factor could represent an important element, here we define the theoretical complexity analysis of the Algorithm 1.

We denote as $N = \alpha$ the dimension of the input, since it is related to the number of sub-matrices involved in the *ASD* process, as shown in Equation 4. Considering that:

- (i) the complexity (*Big O notation*) of the *step 2* is $O(N^2)$, since it performs the *ASD* process by using *N* instances for *N* times, i.e., $ASD(T_+, T_+)$;
- (ii) the complexity of the *step 3* is O(1), because it obtains all needed information at the end of the previous *step 2*;
- (iii) the complexity of the cycle in the *steps 4-11* is the same of the *step 2*, because it performs the same operation by using the items in the set \hat{T} instead of the ones of the set T_+ .

On the basis of the previous considerations, it is clear that the asymptotic time complexity of the algorithm is $O(N^2)$.

However, it should be noted that the computational time can be reduced by distributing the process over different machines, by employing large scale distributed computing models like *MapReduce* (Dean and Ghemawat, 2008).

5 EXPERIMENTS

This section describes the experimental environment, the used datasets and metrics, the adopted strategy, and the results of the performed experiments.

5.1 Experimental Setup

The proposed approach was developed in Java, while the implementation of the state-of-the-art approach, used to evaluate its performance, was made in R^2 , by using the *randomForest* and *ROCR* packages.

²https://www.r-project.org/

Table 1: Datasets.

Dataset Name	Total Cases	Non-default $ T_+ $	Default $ T $	Attributes $ F $	Classes $ C $
DC	30,000	23,364	6,636	23	2
GC	1,000	700	300	21	2

The experiments have been performed by using two real-world datasets characterized by a strong unbalanced distribution of data, i.e., *Default of Credit Card Clients dataset* and *German Credit* datasets, both available at the UCI Repository of Machine Learning Databases³.

5.2 Datasets

The two real-world datasets used during the experiments have been chosen for two reasons: first, they represent two benchmarks in this context; second, they present a strong unbalanced distribution of data.

The datasets are released with all the attributes modified to protect the confidentiality of the data, and we use a version suitable for algorithms that, as the one proposed, can not operate with categorical variables (i.e., a version with all numeric attributes).

It should be noted that, in case of other datasets that contain categorical variables, their conversion in numerical ones is usually a simple task.

5.2.1 Default of Credit Card Clients

The *Default of Credit Card Clients* dataset (*DC*) contains 30,000 instances: 23,364 of them are creditworthy customers (77.88%) and 6,636 are non-creditworthy (22.12%) customers. Each instance contains 23 attributes and a binary class variable (*accepted* or *rejected*).

5.2.2 German Credit

The German Credit (GC) dataset contains 1,000 instances: 700 of them are credit-worthy customers (70.00%) and 300 are non-credit-worthy (30.00%) customers. Each instance contains 21 attributes and a binary class variable (accepted or rejected).

5.3 Metrics

This section presents the metrics used in the experiments.

5.3.1 Accuracy

The Accuracy metric reports the number of instances correctly classified (i.e., *true positives* plus *true nega*-

tives), compared to the total number of them. It gives an overview about the classification performance.

Formally, given a set of instances \hat{T} to be classified, it is calculated as shown in Equation 9, where $|\hat{T}|$ stands for the total number of instances, and $\hat{T}^{(+)}$ stands for the number of those correctly classified.

$$Accuracy(\hat{T}) = \frac{T^{(+)}}{|\hat{T}|} \tag{9}$$

•

5.3.2 F-measure

The *F*-measure (Powers, 2011) is the weighted average of the *precision* and *recall* metrics. It is a largely used metric in the statistical analysis of binary classification and gives us a value in a range [0, 1], where 0 represents the worst value and 1 the best one.

Formally, given two sets X and Y, where X denotes the set of performed classifications of instances, and Y the set that contains the actual classifications of them, this metric is defined as shown in Equation 10.

$$F\text{-measure}(X,Y) = 2 \cdot \frac{(precision(X,Y) \cdot recall(X,Y))}{(precision(X,Y) + recall(X,Y))}$$
with
$$precision(X,Y) = \frac{|Y \cap X|}{|X|}, \ recall(X,Y) = \frac{|Y \cap X|}{|Y|}$$
5.3.3 AUC
(10)

The Area Under the Receiver Operating Characteristic curve (AUC) is a performance measure (Faraggi and Reiser, 2002; Powers, 2011) used to evaluate a predictive model of *credit scoring*. Its result is in a range [0, 1], where 1 indicates the best performance.

Given the subset T_+ of non-default instances in the set T and the subset T_- of default ones, all possible comparisons Θ of the scores of each instance t are reported in the Equation 11, and the AUC metric, by averaging over these comparisons, can be written as in Equation 12.

$$\Theta(t_+, t_-) = \begin{cases} 1, & \text{if } t_+ > t_- \\ 0.5, & \text{if } t_+ = t_- \\ 0, & \text{if } t_+ < t_- \end{cases}$$
(11)

$$AUC = \frac{1}{T_{+} \cdot T_{-}} \sum_{1}^{|T_{+}|} \sum_{1}^{|T_{-}|} \Theta(t_{+}, t_{-})$$
(12)

5.4 Strategy

In order to minimize the impact of data dependency and improve the reliability of the obtained results (Salzberg, 1997), the experiments have been performed by following the *k*-fold cross-validation criterion, with k=10: each dataset is randomly shuffled and then divided in *k* subsets; each subset *k* is used as

³ftp://ftp.ics.uci.edu/pub/machine-learning-databases/

test set, while the other k-1 subsets are used as training set; at the end of the process, we consider the average of results. The datasets' characteristics are summarized in Table 1.

For reasons of reproducibility of the *RF* experiments, we fix the seed of the random number generator by calling the *R* function *set.seed()*.

About the tuning of the *RF* parameters, they have been defined in experimental way, by researching those that maximize the classification performance.

5.5 Experimental Results

The results reported in this section represent the average of the results of all experiments, according to the adopted *k-fold cross-validation* criterion, exposed in the previous Section 5.4.

As we can observe in Figure 3 and Figure 4, the performance of our LDB approach is very close to those of RF in terms of *Accuracy*, as well as in terms of *F-measure*, where we also obtain better results (w.r.t. RF), by using the *DC* dataset.

The first and most important consideration when examining the results is related to the fact that we get these results by operating proactively, i.e., without using default instances during the training process, as it occurs in RF.

A subsequent consideration arises from the observation of the *F-measure* results in Figure 4, which show that the effectiveness of the *LDB* increases with the number of non-default instances used during the training process (as we can observe with the *DC* dataset), differently from *RF*, where this does not happen (although it exploits default and non-default instances during the training process).

It should also be observed that, as shown in Figure 5 and Figure 6, the performance of our approach remains quite stable with all subsets of data (i.e., the k subsets used during the k-fold cross-validation).

The performance of the proposed approach are very interesting also in terms of the AUC metric, as shown in Figure 7. It is a metric that evaluates the predictive power of a classification approach, and its results show that the LDB performance are similar to those of RF, considering that we did not train our model with both classes of instances.

In summary, all results show what we previously stated, i.e., our approach is able to operate in a proactive manner, by detecting default instances that have been never used to train it. It allows us to use it as a stand-alone approach, or as part of a non-proactive approach, to overcome the cold-start problem.

It should be added that the independent-samples *two-tailed Student's t-tests* highlighted that there is a



Figure 3: General Performance : Accuracy.



statistical difference between the results (p < 0.05).

6 CONCLUSIONS AND FUTURE WORK

The *credit scoring* techniques are used in most forms of consumer lending, e.g., credit cards, insurance policies, personal loans, and so on. Financial operators use the customers' credit scores to evaluate the potential risks of lending, attempting to reduce the losses due to default.

This paper proposes a novel approach of *credit* scoring that exploits a *Linear Dependence Based* (*LDB*) criterion to classify a new instance as accepted or rejected. Considering that it does not need to be trained with the default instances occurred in the past, it allows us to operate in a proactive manner, overcoming at the same time the cold-start and the data imbalance problems that affect the canonical machine learning approaches.

The experimental results presented in Section 5.5 show two important aspects related to our approach: on the one hand, it performs very similarly to one of the most performing approaches at the state of the art



Figure 5: Performance by k-folds: GC Dataset.



Figure 6: Performance by k-folds: DC Dataset.



Figure 7: AUC Performance.

(i.e., RF), by operating proactively; on the other hand, it is able to outperform RF, when in the training process a large number of non-default instances are involved, differently from RF, where the performance does not improve further.

A possible follow up of this paper could be a new series of experiments aimed at improving the nonproactive state-of-the-art approaches, by introducing, in the evaluation process, the information related to the default cases, as well as the development and evaluation of the proposed approach in heterogeneous scenarios, which involve different type of financial data, e.g., those generated in an E-commerce environment.

Finally, as part of a future research, we would also like to compare our approach to those in literature, issued after the writing of this paper.

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