Hierarchical Self-organizing Maps System for Action Classification

Zahra Gharaee¹, Peter Gärdenfors¹ and Magnus Johnsson^{1,2}

¹Cognitive Science, Lund University, Helgonavägen 3, Lund, Sweden ²Department of Intelligent Cybernetic Systems, NRNU MEPhI, Moscow, Russia

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Abstract: We present a novel action recognition system that is able to learn how to recognize and classify actions. Our system employs a three-layered neural network hierarchy consisting of two self-organizing maps together with a supervised neural network for labelling the actions. The system is equipped with a module that preprocesses the 3D input data before the first layer, and a module that transforms the activity elicited over time in the first layer SOM into an ordered vector representation before the second layer, thus achieving a time invariant representation. We have evaluated our system in an experiment consisting of ten different actions selected from a publicly available data set with encouraging result.

1 INTRODUCTION

Humans increasingly interact with robotic systems. Service robots that communicate and collaborate with people can undertake tasks that stand-alone robots cannot. In order to realize their full value, robots will need to interact and work with people fluently. The design of intelligent collaborative robots in open, complex and changing environments where they are expected to communicate, interact and work with people presents great scientific challenges.

The success of the human-robot interaction depends on the development of robust methods that enable robots to recognize and predict goals and intentions of other agents. Humans do this, to a large extent, by interpreting and categorizing the actions they perceive. Hence, it is central to develop methods for action categorization that can be employed in robotic systems. This involves an analysis of on-going events from visual data captured by cameras to track movements of humans and to use this analysis to identify actions. Modelling these tasks is also crucial in a variety of other domains such as computer games, surveillance, assisted living, ambient intelligence, and decision support.

In this article, we present an action categorization method that, at large, works like the human system. Results from the cognitive sciences indicate that the human brain performs a substantial information reduction when categorizing actions. In particular, (Johansson, 1973) patch-light technique for analyzing biological motion is a source of inspiration for us. He attached light bulbs to the joints of actors who were dressed in black and moved in a dark room. The actors were filmed performing actions such as walking, running, and dancing. Watching the films - in which only the dots of light could be seen - subjects recognized the actions within tenths of a second. Further experiments by (Runesson and Frykholm, 1983), see also (Runesson, 1994), have shown that subjects extract subtle details of the actions performed, such as the gender of the person walking or the weight of objects lifted (where the objects themselves cannot be seen). An important lesson to learn from the experiments by Johansson and his followers is that the kinematics of a movement contains sufficient information to identify the underlying dynamic patterns.

From a computational point of view, there are many challenges that make the action recognition task difficult to imitate artificially. For example, the acting individuals differ in height, weight and bodily proportions. Other important issues to be addressed are the impact of the camera's viewing angle and its distance from the actor and the performance speed of the actions. In brief, categorizations of actions ought to be invariant under distance, viewing angle, size of actor, lighting conditions and temporal variations.

One idea for a model of actions comes from (Marr and Vaina, 1982) and (Vaina, 1983), who extend (Marr and Nishihara, 1978) cylinder models of objects to an analysis of actions. In Marr and Vaina's model, an action is described via differential equati-

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ons for movements of the body parts of, for example, a walking human. What we find useful in this model is that a cylinder figure can be described as a vector with a limited number of dimensions. Each cylinder can be described by two dimensions: length and radius. Each joining point in the figure can be described by a small number of coordinates for point of contact and angle of joining cylinders. This means that, at a particular moment, the entire figure can be written as a (hierarchical) vector of a fairly small number of dimensions. An action then consists of a sequence of such vectors. In this way, the model involves a considerable reduction of dimensionality in comparison to the original visual data.

This representation fits well into the general format of conceptual spaces presented by (Gärdenfors, 2000) and (Gärdenfors, 2007). From that theory we borrow the idea that a concept, in this case a sequence of bodily positions, form a convex region in action space, see (Gärdenfors, 2007), (Gärdenfors, 2000) and (Gärdenfors and Warglien, 2012).

One may interpret here convexity as the assumption that, given two actions in the region of an action concept, any linear morph between those actions will fall under the same concept. One way to support the analogy between the thesis about properties and the thesis about actions is to establish that action concepts share a similar structure with object categories (Hemeren, 2008, p. 25). Indeed, there are strong reasons to believe that actions exhibit many of the prototype effects that (Rosch, 1975) presented for object categories. In a series of experiments, (Hemeren, 2008) showed that action categories show a similar hierarchical structure and have similar typicality effects to object concepts. He demonstrated a strong inverse correlation between judgments of most typical actions and reaction time in a word/action verification task.

We take inspiration from these models in the sense that we represent actions as sequences of vectors and aim to categorize an action on the basis of its similarities to other actions. In our model, similarity is modelled as closeness in Self-Organizing Maps, SOMs, (Kohonen, 1988).

In the current study we have used an approach similar to the one presented in (Buonamente et al., 2016) in which we have done experiments employing hierarchical SOMs for action recognition using 2D movies as input. In this study instead our system uses sequences of sets of 3D joint positions extracted from the depth images captured by a 3D camera similar to a kinect sensor. By using 3D input data the system will receive more information from the actor's spacial trajectories and thus be able to exploit this information for classifying actions with a significantly higher performance as shown in the results. Moreover, in this study we applied a pre-processing mechanism on the 3D input data to make it independent of the actor's orientation and distance to the camera while extracting the local interest points from the body of the actor by applying an attentional mechanism. In this way the system's performance is improved.

One of our motivations for a SOM based approach to action recognition is to achieve an ability to internally simulate (Hesslow, 2002) the likely continuation of partly seen actions. This can be done by employing Associative Self-Organizing Maps, A-SOMs, (Johnsson et al., 2009), and have been investigated by using 2D movies as input in a number of studies (Johnsson and Buonamente, 2012; Buonamente et al., 2013a; Buonamente et al., 2013b; Buonamente et al., 2014; Buonamente et al., 2015).

In the literature one finds several systems that can categorize different sets of actions. Among them is the one presented by (Li et al., 2010), which was evaluated by the MSR Action 3D dataset ¹. The same dataset has also been employed by many other researchers ((Xia et al., 2012);(Masood et al., 2013); (Oreifej et al., 2013); (Yang et al., 2012); (Wang et al., 2012a); (Wang et al., 2012b); (Lo Presti et al., 2014)). In this study, we have evaluated our action recognition system by actions from the the MSR Action 3D dataset that are performed by the upper parts of the body resulting in a more difficult classification task for the system since the similarity between the actions (e.g, hand catch and high throw) increases. The implementation of most of the code for the experiments presented in this paper was done in C++ using the neural modelling framework "Ikaros" (Balkenius et al., 2010) and some in MatLab.

The rest of the paper is organized as follows: The proposed architecture is presented in section 2. In section 3, an experiment evaluating our action recognition system is presented. Finally, section 4 concludes the paper.

2 ARCHITECTURE

In this paper, we focus on the recognition of bodily actions of one person. The architecture, Fig. 1, is composed of three neural network layers. The first layer consists of a SOM that develops a compressed and ordered representation of the preprocessed input (i.e. parts of the scaled postures in an egocentric framework). The second layer consists of a second

¹The repository is available at

http://research.microsoft.com/en-us/um/people/zliu/ ActionRecoRsrc/

SOM. It receives ordered vectors that are spatialized representations of the activity patterns elicited in the first-layer SOM during actions. The ordered vector representation of the sequence of unique activations in the first layer provides a mechanism that makes the system time invariant. This is possible because similar movements carried out at different performance speed will elicit similar sequences of unique activations in the first layer SOM. Thus the second layer that receives these ordered vector representations will learn to cluster complete actions. The third layer consists of a custom made supervised neural network that labels the activity in the second layer SOM with the corresponding actions. The third layer could provide some independence of the camera's viewing angle, but this is done more efficiently as a part of the preprocessing, i.e. by scaling and transforming the sets of joint positions into an egocentric framework before they are received by the first layer SOM.

To evaluate the architecture, we used input data composed of sequences of sets of 3D joint positions obtained by a depth camera similar to the Kinect sensor.

In the following subsections, the different layers of the architecture will be described.



Figure 1: The three layer action recognition architecture. The first layer consists of a SOM. Layer two consists of a SOM, and layer 3 of a custom made supervised neural network. The darker arrows in the SOM represent the activity trace during the performance of an action.



Figure 2: Different sizes of body skeletons due to different distances.



Figure 3: A sketch of a human body skeleton and the joints received from the Kinect.

2.1 Preprocessing

Before entering the first-layer SOM, the input data is preprocessed. The distance and the capturing angle between the depth camera and the subjects performing the actions may differ. This can partially be handled by the three neural network layers in the architecture, but by re-scaling and transforming the joint positions into an egocentric coordinate system the performance of the architecture can be improved. Thus, first the joint positions in each posture frame from the depth camera is re-scaled, Fig. 2, i.e. made into a standard size. Then the coordinates of the joint positions are transformed into a new and egocentric coordinate system located close to joint number 7 of the skeleton, Fig. 3.

To calculate the axes of the egocentric coordinate system, joints 5, 6 and 7 are used. As can be seen in Fig. 4, these joints constitutes the vertices in a triangle and the projection 0 of joint 7 on the side connecting joints 5 to 6 can be calculated. Then axes originating in the point 0 along the line between the point 0 and joint 7 and along the line between joints 5 and 6 can be selected together with an axis orthogonal to the triangle for the new coordinate system and

a transformation matrix (Craig, 1989) can be calculated, which enables all the joints to be expressed in egocentric coordinates.



Figure 4: The joints used to calculate the egocentric coordinate system.

Due to limitations in visual field, time, and processing capacity, the entire input information cannot always be processed in real time (Shariatpanahi and Ahmadabadi, 2007). By using attention mechanisms, performance can also be improved, e.g. in a driving task (Gharaee et al., 2014) or in the case of action perception in the current study. We applied an attentional mechanism to the part of the skeleton that exhibits the largest movements, the influence of less relevant parts of the input data can be decreased whereas the influence of more relevant parts of input data in performing an action are increased.

In our experiment, this was achieved by dividing the skeletons into five basic parts, Fig. 5. The division is based on how actions are performed in a human body. The focus of attention is set to the moving part which, in this dataset, is the left arm of the subjects. This can be seen for one subject in Fig. 6.



Figure 5: The division of the skeleton into five basic parts.

2.2 The First and Second Layer SOMs

The first two layers of the architecture consist of SOMs. The SOMs are trained using unsupervised



Figure 6: A visualization of the series of posture frames for six of the ten actions performed by the first subject in the first event in the dataset we used. The attention is focused on the left arm of the actor.

learning to produce dimensionality reduced and discretized representations of their input spaces. These representations preserve the topology of their corresponding input spaces, which means that nearby parts of the network will respond to similar input patterns, reminiscent of the cortical maps found in mammalian brains. The SOMs will therefore generate a measure of similarity which is the founding property of a conceptual space (Gärdenfors, 2000). In other words, the map generated by a SOM can be seen as a conceptual space that is generated from the training data.

The topology-preserving property of SOMs is a consequence of the use of a neighbourhood function in the adaptation of the neuron responses, i.e. the adaptation strength is a decreasing function of the distance of the most activated neuron in the network. This also provides the SOM, and in the extension our action recognition system, with the ability to generalize learning to novel inputs. This is because similar inputs elicit similar activities in the SOM. Thus similar sequences of postures will elicit similar sequences of activity in the first layer SOM, and these will in turn elicit similar activations in the second layer SOM.

The SOM consists of an $I \times J$ grid of neurons with a fixed number of neurons and a fixed topology. Each neuron n_{ij} is associated with a weight vector $w_{ij} \in R^n$ with the same dimensionality as the input vectors. All the elements of the weight vectors are initialized by real numbers randomly selected from a uniform distribution between 0 and 1.

At time t each neuron n_{ij} receives the input vector

 $x(t) \in \mathbb{R}^n$. The net input $s_{ij}(t)$ at time t is calculated using the Euclidean metric:

$$s_{ij}(t) = ||x(t) - w_{ij}(t)||$$
(1)

The activity $y_{ij}(t)$ at time *t* is calculated by using the exponential function:

$$y_{ij}(t) = e^{\frac{-s_{ij}(t)}{\sigma}}$$
(2)

where σ is the exponential factor set to 10^6 and $0 \le i < I, 0 \le j < J, i, j \in N$. The role of the exponential function is to normalize and increase the contrast between highly activated and less activated areas.

The neuron n_c with the strongest activation is selected:

$$c = \operatorname{argmax}_{ij} y_{ij}(t) \tag{3}$$

The weights w_{ijk} are adapted by

$$w_{ijk}(t+1) = w_{ijk}(t) + \alpha(t)G_{ijc}(t)[x_k(t) - w_{ijk}(t)]$$
(4)

where $0 \le \alpha(t) \le 1$ is the adaptation strength, $\alpha(t) \to 0$ when $t \to \infty$. The neighbourhood function $G_{ijc}(t) = e^{-\frac{||r_c - r_{ij}||}{2\sigma^2(i)}}$ is a Gaussian function with a radius that decreases with time, and $r_c \in R^2$ and $r_{ij} \in R^2$ are location vectors of neurons n_c and n_{ij} respectively.

2.3 Ordered Vector Representation

The activity elicited in the first-layer SOM during the sequence of preprocessed input corresponding to an action is re-arranged into a spatial representation by a process we call ordered vector representation before entering the second-layer SOM. The ordered vector representation process consists of building a vector representation of the activity trajectory elicited in the first layer SOM during an action. Since sufficiently similar postures are represented by the same neuron, a particular movement carried out at various speeds will elicit an activity trajectory along the same path in the first layer SOM. Since this path, which will be similar for the same movement carried out at various speeds by the performing agent (see Fig. 7), is what is used to build the input vector for the second layer SOM, time invariance is achieved.

The ordered vector representation in this experiment works as follows. The length of the activity trace of an action Δ_i is calculated by

$$\Delta_j = \sum_{i=1}^{N-1} ||P_{i+1} - P_i||_2 \tag{5}$$



Figure 7: The activity trajectory in the first layer SOM during an action carried out at two different speeds.

where N is the total number of centres of activity for action sequence j and P_i is the *i*th centre of activity in the same action sequence.

Suitable lengths of segments to divide the activity trace for action sequence j in the first layer SOM are calculated by

$$d_j = \Delta_j / N_{Max} \tag{6}$$

where N_{Max} is the longest path in the first layer SOM elicited by the *M* actions in the training data.

Each activity trace in the first layer SOM, elicited by an action, is divided into d_j segments, and the coordinates of the borders of these segments in the order they appear from the start to the end on the activity trace are composed into a vector used as input to the second-layer SOM.

2.4 Output Layer

The output layer receives the activity of the second layer SOM as input and consists of an $I \times J$ grid of a fixed number of neurons with a fixed topology. Each neuron n_{ij} is associated with a weight vector $w_{ij} \in \mathbb{R}^n$. All the elements of the weight vector are initialized by real numbers randomly selected from a uniform distribution between 0 and 1.

At time t each neuron n_{ij} receives an input vector $x(t) \in \mathbb{R}^n$.

The activity $y_{ij}(t)$ at time t in the neuron n_{ij} is calculated using the standard cosine metric:

$$y_{ij}(t) = \frac{x(t) \cdot w_{ij}(t)}{||x(t)||||w_{ij}(t)||}$$
(7)

During the learning phase the weights w_{ijl} are adapted by

$$w_{ijl}(t+1) = w_{ijl}(t) + \beta x_l(t) [y_{ij}(t) - d_{ij}(t)]$$
(8)

where β is the adaptation strength and $d_{ij}(t)$ is the desired activity for the neuron n_{ij} . The desired activity is the activity pattern in the output layer that corresponds to the unambiguous recognition of the ongoing action.

3 EXPERIMENT

We have evaluated our action recognition architecture, Fig. 1, in an experiment in which we used joint positions obtained by a depth camera, similar to a Kinect sensor (Wan, 2015). In this experiment we tested the ability of the architecture to categorize actions based on sequences of sets of joint positions. The employed dataset contains 276 samples with 10 different actions performed by 10 different subjects in 2 to 3 different events. Each action sample is composed of a sequence of frames where each frame contains 20 joint positions, Fig. 3, expressed in 3D cartesian coordinates. The actions are: 1. High Arm Wave, 2. Horizontal Arm Wave, 3. Hammer, 4. Hand Catch, 5. Forward Punch, 6. High Throw, 7. Draw X, 8. Draw Tick, 9. Draw Circle, 10. Tennis Swing.

Forward Punch



Figure 8: Examples of some of the activity traces in the first layer SOM elicited by the training data for the action forward punch. As can be seen, the activity traces elicited by a particular action in the first layer SOM can be grouped into subclasses of typical patterns. In the figure these subclasses are indicated by numbers. The reason to why there are several typical patterns is that an action can be carried out in multiple ways. For example, different subjects might have different typical ways of carrying out the same action.



Figure 9: Examples of activity traces in the first layer SOM elicited by the test data for the action forward punch. The numbers indicate what subclass the patterns belong to.

For the experiment, the dataset was split into a training set containing 80% of the action instances

randomly selected from the original dataset and a test set containing the remaining 20% of the instances. Then the architecture was trained with randomly selected instances from the training set in two phases, the first to train the first-layer 30×30 neurons SOM, and the second to train the second layer 35×35 neurons SOM and the output layer containing 10 neurons. Fig. 8 shows examples of activity traces in the first layer SOM elicited by the training data for the action forward punch, and Fig. 9 shows examples of activity traces in the first layer SOM elicited by the test data for the action forward punch.

The activity traces in the first layer SOM are clustered in the second layer SOM. Each action appears to be mapped into two or three clusters. The result of the supervised third layer neural network, which labels the clusters in the second layer SOM, is shown in Fig. 10. As can be seen, 83% of the test actions are correctly categorized. Fig. 11 shows the categorization result for each of the ten actions. As shown in Fig. 11 four actions among the ten are classified completely correct with 100% accuracy. The performance of the system decreases when the similarity between different actions increases, and it occurs when these actions are performed in a more similar way in most of the sequences. This case can be seen in the actions hand catch and high throw or the actions hammer and forward punch which as a consequence receive lower performance of classification.

As shown in Fig. 10, we improved the action recognition performance of hierarchical SOM system from around 50% in the (Buonamente et al., 2016), to 83% in this study. The result also shows a significant improvement to the state-of-the-art method in (Li et al., 2010) from 74.7% recognition accuracy to 83% . Our system outperforms several other studies including ((Xia et al., 2012);(Masood et al., 2013); (Yang and Tian, 2012); (Lo Presti et al., 2014)). In our approach, we use a learning mechanism based on self organizing neural networks both as a descriptor for action recognition or unique feature extraction in the first layer and as a classifier in the second layer. It represents the flexibility and robustness of SOM architecture which can be utilized to satisfy different goals. Moreover, by applying SOM in the first layer we could easily build a compact representation of postures into a set of action patterns which help us to face the problem of high dimensionality of the input data. By applying ordered vector representation on the patterns we invented a time invariant representation of actions to deal with another condition in a real situation in which different actions are composed of different number of posture frames and could elicit different number of activated neurons in SOM.



Figure 10: The result of the supervised third layer neural network in the experiment using sequences of joint positions as input.



Figure 11: The categorization result for each of the ten actions in the experiment using sequences of joint positions as input. The actions are: 1. High Arm Wave, 2. Horizontal Arm Wave, 3. Hammer, 4. Hand Catch, 5. Forward Punch, 6. High Throw, 7. Draw X, 8. Draw Tick, 9. Draw Circle, 10. Tennis Swing.

4 CONCLUSIONS

In this article we have presented a three layered hierarchical SOM based architecture for action recognition. The architecture is inspired by findings concerning human action perception, in particular those of (Johansson, 1973). The first layer in the architecture consists of a SOM. The second layer is also a SOM, and the third layer is a custom made supervised neural network.

The experiment tested the architecture's ability to categorize actions based on input sequences of 3D joint positions. The primary goal of the architecture is to categorize human actions. As in prototype theory, the categorization in our system is based on similarities of actions, and similarity is modelled in terms of distances in SOMs. In this sense, our categorization model can be seen as an implementation of the conceptual space model of actions presented in (Gärdenfors, 2007) and (Gärdenfors and Warglien, 2012). We believe that attention plays an important role in selecting what information is most relevant in the process of action recognition, and our experiment is a way of testing this hypothesis. The hypothesis should, however, be tested with further datasets in order to be better evaluated.

We have previously tested our action recognition architecture when trained to recognize manner and result actions performed online in real time by a human performer in front of the system's Kinect sensor (Gharaee et al., 2016) (demo movies are available at the web site http://magnusjohnsson.se/ar.html).

A model of action categorization based on patterns of forces is presented in (Gärdenfors, 2007) and (Gärdenfors and Warglien, 2012). Extending the architecture to also taking into account forces by considering the second order dynamics (corresponding to sequences of joint accelerations) should improve the performance even more. We will explore this in the future. The data we have tested comes from human actions. The generality of the architecture allows it to be applied to other forms of motion involving animals and artefacts. This is another area for future work.

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