An Accurate Tax Fraud Classifier with Feature Selection based on Complex Network Node Centrality Measure

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Abstract: Fiscal evasion represents a very serious issue in many developing countries. In this context, tax fraud detection constitutes a challenging problem, since fraudsters change frequently their behaviors to circumvent existing laws and devise new kinds of frauds. Detecting such changes proves to be challenging, since traditional classifiers fail to select features that exhibit frequent variations. In this paper we provide two contributions that try to tackle effectively the tax fraud detection problem: first, we introduce a novel feature selection algorithm, based on complex network techniques, that is able to capture key fraud indicators – over time, this kind of indicators turn out to be more stable than new fraud indicators. Secondly, we propose a classifier that leverages the aforementioned algorithm to accurately detect tax frauds. In order to prove the validity of our contributions we provide an experimental evaluation, where we use real-world datasets, obtained from the State Treasury Office of Ceará (SEFAZ-CE), Brazil, to show how our method is able to outperform, in terms of F_1 scores achieved, the state-of-the-art available in the literature.

1 INTRODUCTION

Fiscal evasion represents a very serious issue for the economy of developing countries. Although institutions often undertake initiatives to collect meaningful taxpayer information, thus trying to reduce fiscal evasion, the level of tax frauds remains high – for instance, the level of tax evasion in Brazil is of about US\$ 143 billions (Sonegometro, 2016). On the positive side, the continuous collection of more and more taxpayer data opens up to new kinds of opportunities, since it allows the creation of increasingly effective approaches that are able to mitigate tax evasion.

In this work, we consider a real-world scenario involving the State Treasury Office of Ceará (SEFAZ-CE, Brazil), the agency in charge of supervising over 200,000 active contributors in the state of Ceará, Brazil. Although SEFAZ-CE maintains a large dataset containing a plethora of information, its enforcement team struggles to perform thorough inspections on taxpayers accounts. Indeed, the inspection process involves countless fraud indicators, thus requiring burdensome amounts of time and being potentially subject to human errors. In this paper, we aim to ease this kind of tasks by introducing novel algorithmic tools.

We start by posing ourselves four key questions:

what are the *behavioral patterns* behind fraud indicators? Are there some kind of *correlations* among fraud indicators? Which are the *most relevant* fraud indicators? How can we assess the *risk* that some taxpayer commits a fraud?

In this paper we try to answer these questions by introducing a new method for predicting potential tax frauds. The method is structured in four phases, and relies on data mining, statistical analysis, and dimensionality reduction techniques. During the first phase, our approach analyzes the frequency of individual attributes, as well as the frequency associated with combinations of attributes, trying also to understand whether attributes exhibit some kind of statistical distribution over time. By virtue of these information, in the second phase our method infers the dimensions that are the most relevant for taxpayer classification. Subsequently, in the third phase our approach validates the hypothesis of using the centrality measure to select key indicators, while in the final phase it outputs a list that reports the fraud risk associated with each taxpayer. Overall, our proposal significantly improves the approach presented in (Matos et al., 2015), in that it uses complex network techniques to pick up key indicators that can help to accurately identify frauds.

In the experimental evaluation we show how our

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algorithm is able to achieve equivalent, or better, F_1 scores with respect to the algorithm proposed in (Matos et al., 2015) – the improvement is equal to about 54% when considering the dataset introduced in this work, while comparable F_1 scores are achieved when considering the dataset introduced in (Matos et al., 2015). In the same evaluation we also show how our method is able to achieve better F_1 scores – the improvement is up to 47% when considering the dataset introduced in SVM¹-based approach (Shavers et al., 2006).

The paper is structured as follows: Section 2 presents the related work. Section 3 presents the case study that we consider in this work. Section 4 presents our proposal. Section 5 presents the experimental setting, while Section 6 presents the experimental evaluation. Finally, Section 7 draws the final conclusions.

2 RELATED WORK

(Glancy and Yadav, 2011) proposes a quantitative model to detect fraudulent financial reports. The goal of the model is to detect attempts to conceal information, or report incorrect information, in annual filings presented to the US Securities and Exchange Commission (SEC). In order to achieve this, the authors analyze all the information contained within a textual document by means of techniques based on the Singular Value Decomposition (SVD).

(Ngai et al., 2011) presents a review of the literature – along with a classification scheme – concerning the application of data mining techniques to detect financial frauds. The findings clearly show that data mining techniques have been applied extensively to detect insurance frauds, although corporate and credit card frauds have also attracted a great deal of attention in recent years. In general, the review shows that the main data mining techniques used in the literature are based on logistic models, neural networks, Bayesian belief networks, and decision trees.

(Bhattacharyya et al., 2011) evaluates two approaches, both relying on the usage of support vector machines, random forests techniques and logistic regression, as part of an attempt to better detect credit card frauds. In this study, the authors consider real-world data concerning international credit card transactions.

(Ravisankar et al., 2011) considers data mining techniques, such as Multilayer Feed Forward Neural Network (MLFF), Support Vector Machines (SVM), Genetic Programming (GP), Group Method of Data Handling (GMDH), Logistic Regression (LR), and Probabilistic Neural Network (PNN), to identify companies that commit financial statement frauds. Coupled with these techniques, the authors consider also the usage of feature selection techniques. The experimental evaluation, which considers a dataset involving 202 Chinese companies, shows how PNN is the clear winner when feature selection is not used, while GP and PNN emerge as winners in the opposite case.

(Kirkos et al., 2007) explores the effectiveness of data mining classification techniques to detect companies that issue fraudulent financial statements (FFS), and deals with the identification of factors associated with FFSs. More precisely, the study investigates the usefulness of decision trees, neural networks and Bayesian belief networks; in the end, the authors report that Bayesian Belief Networks emerge as winners.

(Sánchez et al., 2009) proposes the use of association rules to extract behavior patterns from unlawful transactions observed in transactional credit card databases. In turn, this knowledge is exploited to detect and prevent frauds.

(Li et al., 2012) employs Bayesian classification and association rules to identify signs of fraudulent accounts and patterns of fraudulent transactions; detection rules are created according to identified signs, and used to devise a system able to detect fraudulent accounts. By means of an empirical verification, the authors show their solution can successfully identify fraudulent accounts in early stages, as well as provide useful information to financial institutions.

(Phua et al., 2010) presents a survey that categorizes, compares, and summarizes the literature related to automated fraud detection. More precisely, the survey covers a set of works published between 2000 and 2010, and discusses the main methods and techniques used to detect frauds automatically, along with their shortcomings.

(Fanning and Cogger, 1998) uses a Neural Network to devise a fraud detection model. The input vector consists of financial ratios and qualitative variables. In the experimental evaluation, the authors compare the performance of their model with standard statistical methods, such as linear and quadratic discriminant analysis, and logistic regression. Overall, the authors claim that their model is more effective at detecting frauds than its competitors.

(Abbott et al., 2000) uses statistical regression analysis to examine if the use of independent audit committees (such as independent managers that meet at least twice per year) within companies can mitigate the likelihood of frauds. Indeed, the paper concludes that when this happens, firms are less likely to

¹The acronym stands for *support vector machine*.

be sanctioned for fraudulent or misleading reporting.

3 CASE STUDY

In this section we present a case study that concerns the data collected by the Treasury State of Ceará (SEFAZ-CE), Brazil, which is responsible for collecting taxes within the state of Ceará. This case study will serve us as a basis to represent the problem we want to tackle, thanks to the volume and nature of the data provided by the agency.

One of the goals of this study is to analyze taxpayer fraud indicators to identify relevant key indicators (main features) that may characterize potential tax frauds. Indeed, the data to be analyzed may be possibly huge, and may contain many different kinds of information – just to name a few examples, accounting data, goods inventory, sales data, legal data, etc. A proper interpretation of fraud indicators is of paramount importance to guide tax auditors during the process of identifying irregular behaviors. Indeed, without the aid of algorithmic tools, auditors must usually resort to thorough and complex analyses which, in turn, make the task of detecting frauds time consuming and error prone.

3.1 Tax Fraud Indicator Dataset

Data provided by SEFAZ-CE were extracted from 8 applications, summing up to 72 million of records. We selected taxpayers data collected during a period ranging from 2009 to 2011, which corresponds to the current audit period. We used fourteen fraud indicators, all identified by expert tax auditors. From a financial point of view, these indicators are of key importance, since they correspond to the largest amount of money that can be recovered from fraudulent transactions. Each fraud indicator is determined by a tax auditor after analyzing information issued by taxpayers, such as tax documents, records of the movement of goods at the border of the state of Ceará, and taxpayer sales data. Due to confidentiality reasons, we anonymized the indicators by means of letters and numbers; more specifically, to anonymize taxpayers data a sequential ID is assigned to each taxpayer, while each fraud indicator - fourteen in total - is renamed by means of the symbols A, B, C, D, E, F, G, H, I, J, K, L, M, and N. Data from 2009 and 2010 have the same indicators (A, B, C, D, E, F, G, H, I, J, K, L, M and N), while data from 2011, despite having the same number of indicators, is characterized by different kinds of indicators, namely X1, X2, X3, X4, X5, X6, X7, X8, X9, X10, X11, X12, X13, X14; this is





Figure 1: Frequency of tax fraud indicators for the years 2009, 2010 and 2011.

due to the fact that indicators frequently change from year from year, since fraudster tend to search alternative ways to avoid paying taxes.

As shown in the section detailing our tax fraud detection method (Section 4), frequent variations affect fraud indicators (features) year by year: this calls for an algorithm that is able to automatically identify key indicators. This, in turn, helps to better characterize tax fraudsters, thus improving the quality of the results returned by a predictive model. Indeed, we highlight that this is one of the main contributions characterizing this paper, thus differentiating our work with respect to (Matos et al., 2015).

3.2 Tax Fraud Matrices

Three matrices were constructed for the years 2009, 2010, and 2011. Each matrix relates to taxpayers (rows) and their corresponding fraud indicators (columns). Each indicator uses a binary representation, where 1 (one) indicates the presence of fraud, while 0 (zero) the absence. The matrix for data related to 2009 has 11,386 rows and 14 columns, the one for 2010 possesses 12,424 rows and 14 columns, while the one from 2011 contains 10,627 rows and 14 columns. Taxpayers who did not present any evidence of fraud were excluded, since they were considered outliers.

3.3 Data Overview

Figure 1 presents three histograms, detailing the frequency of fraud indicator frequencies collected for the years 2009, 2010 and 2011 respectively. In 2009, 10,789 (95%) out of 11,386 taxpayers have at least one type of fraud evidence, while 597 (5%) of taxpayers do not present any evidence. In 2010, 11,989 (96%) out of 12,424 taxpayers exhibit at least one type of fraud evidence, while 435 (4%) do not present any kind of anomaly. Overall, we report that the frequency of the vast majority of fraud indicators increased from 2009 to 2010, thus indicating that tax evasion represents a very relevant problem that needs to be addressed.

4 TAX FRAUD DETECTION METHOD

In this section we present a detailed description of TAXFRAUDDETECTOR, our tax fraud detection method. The main goal of TAXFRAUDDETECTOR is to compute the risk that a taxpayer has to commit a fraud. TAXFRAUDDETECTOR takes in input four parameters, i.e., a tax fraud matrix, S, and three thresholds, *supp*, *conf*, and *lift* representing, respectively, the *support*, *condifence*, and *lift* thresholds used by the Apriori algorithm (Agrawal et al., 1994) leveraged within our approach; in this context, we remind that the value given to *lift* determines the final set of association rules deemed relevant by TAXFRAUDDETEC-TOR, hence highlighting its important role. Algorithm 1 presents the pseudocode.

TAXFRAUDDETECTOR starts by processing the tax fraud matrix *S* by means of Apriori (line 2, function *KeyRules*): this has the purpose of identifying relevant association rules that, in turn, allow to focus on the most relevant fraud indicators (function *KeyRules*,

Algorithm 1: TAXFRAUDDETECTOR.

- S, the data matrix.
- *supp*, the support threshold to be used with Apriori.
- *conf*, the confidence threshold to be used with Apriori.
- *lift*, the lift threshold to be used with Apriori.
- 1 begin

Input :

- 2 $kRules \leftarrow KeyRules(S, supp, conf, lift)$
- 3 $KeyIndicators \leftarrow KFind(kRules)$
- 4 $S' \leftarrow Subset(S, KeyIndicators)$
- 5 return DimRedSVD(S')

Algorithm 2: KevRule	es(S. supp. cont	: li	ft
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1	begin
2	$RuleSet \leftarrow \emptyset$
3	$AP \leftarrow Apriori(S, supp, conf)$
4	foreach $ap \in AP$ do
5	if $(Lift(ap) \ge lift)$ then
6	$\left\lfloor RuleSet \leftarrow RuleSet \cup \{ap\}\right\}$
7	return RuleSet

Algorithm 2, line 5). We note that this is the main difference our method exhibits with respect to (Matos et al., 2015), since the latter performs the selection of key determinants by means of inference rules. Subsequently, association rules are used to generate a graph (we call it *fraud graph*) and discover the key fraud indicators (line 3, function *KFind*). Key indicators are finally used to filter out from *S* irrelevant indicators, thus obtaining a modified data matrix *S'* (line 4, function *Subset*). The algorithm concludes by reducing the dimensionality of key indicators, by means of an SVD-based algorithm (Golub and Reinsch, 1970), to a single dimension (line 5, function *DimRedSVD*): this generates a list of scalars, each one representing the degree of fraud risk associated with a taxpayer.

Algorithm 3: *KFind*(*kRules*).

1	be	egin
2		$KeyIndicator \leftarrow 0$
3		$G \leftarrow$ graph where each <i>sequence</i> of indicators appearing in
		<i>kRules</i> is a vertex $v \in V$, while each <i>association rule</i> $ar \in kRules$
		represents an edge $e \in E$
4		foreach $v \in G$ do
5		$v_{Degree} \leftarrow v_{InDegree} + v_{OutDegree}$
6		foreach $v \in G$ do
7		if $v_{Degree} > (AVGDegree(G) + 3 \cdot STDevDegree(G))$ then
8		$\left\lfloor KeyIndicator \leftarrow KeyIndicator \cup \{v\}\right\}$
9		_ return KeyIndicator

Before concluding this section we spend two words on *KFind* (Algorithm 3). *KFind* takes in input a set of association rules, i.e., *kRules*: first, from *kRules* it generates a graph, G = (V, E), that represents relationships among fraud indicators (line 3). The graph is built as follows: each vertex represents a sequence of fraud indicators, while each edge represents an association rule – for example, the existence of an association rule $(ABC \rightarrow D) \in kRules$ implies that $\{ABC, D\} \in V$ and $(ABC, D) \in E$. Finally, *KFind* selects the nodes having degree (i.e., in-degree plus out-degree) greater than three times the standard deviation characterizing *G*'s degree distribution – in other words, we exploit the 3-sigma confidence interval (Montgomery, 2007; Bland and Altman, 1996).

5 EXPERIMENTAL SETTING

In the following we present the experimental setting used to conduct the experiments reported in Section 6.

5.1 Methodology

In order to conduct the experimental evaluation we applied the following methodology: first, from the dataset provided by SEFAZ-CE (introduced in Section 3) we picked up 120 contributors having the highest values in the ranking list computed by TAXFRAUDDETECTOR – as such, this list represents the group of people that, according to our method, have the highest chance to be fraudsters. Next, from the same dataset we picked up 50 contributors having the lowest values, thus representing the group of people that, according to our method, have the lowest chance to be fraudsters.

Subsequently, we provided the two lists to two experienced tax auditors, who conducted a thorough analysis to check the correctness of TAXFRAUDDE-TECTOR's results and create a ground truth. From the analysis, they concluded that out of 120 people making up the first group, 85 were indeed fraudsters, while out of 50 people making up the second group, 23 were honest taxpayers.

To estimate the accuracy of the classification methods when employing selected features, we use the k-fold cross-validation technique; more specifically, we rely on the 10-fold cross-validation as it tends to provide less biased estimations (Kohavi et al., 1995).

5.2 Measures

In order to assess the quality of the results returned by TAXFRAUDDETECTOR and its competitors, we resort to well-established metrics commonly used in data mining to evaluate the quality of a classifier (Tan Table 1: Confusion matrix, with positive and negative classification.

Classification	Correct	Not Correct
Fraudsters	85 (TP)	35 (FP)
Not fraudsters	7 (FN)	23 (TN)

Table 2: Statistical measures used to assess the quality of the results returned by classifiers.

Measure	Definition		
Accuracy	$A = \frac{TP + TN}{N}$		
Precision	$P = \frac{TP}{TP + FP}$		
Recall	$R = \frac{TP}{TP + FN}$		
F_1 Score	$F = \frac{2 \cdot R \cdot P}{R+P}$		

et al., 2005). In the following we briefly introduce them.

Given a set of N taxpayers, we can evaluate the results of a classifier by constructing an integer confusion matrix; in order to do this, we first have to define the following types of outcomes when considering any result:

- A *True Positive* (TP) result occurs when a fraudster is correctly classified as such.
- A *False Positive* (FP) result occurs when an honest contributor is classified as a fraudster.
- A *False Negative* (FN) result occurs when a fraudster is not classified as such.
- A *True Negative* (TN) result occurs when a honest contributor is classified as honest.

Accordingly, we arranged the figures returned by the auditors' evaluation into a *confusion matrix* (Table 1), which in turn allows to easily derive statistical measures that are commonly used to assess the quality of a classifier (Table 2).

5.3 Competitors

In the experimental evaluation we compare the following methods:

- TAXFRAUDDETECTOR.
- The method proposed in (Matos et al., 2015), which is also the current state-of-the-art in the literature.
- An SVM-based approach that uses indicators (as features) previously selected by TAXFRAUDDE-TECTOR.
- An SVM-based approach that uses indicators previously selected in (Matos et al., 2015).
- An SVM-based approach that does not recur to any kind of feature selection.

We included an SVM-based classifier mainly for two reasons: first, to analyze how it performs with respect to our method; secondly, to understand whether TAXFRAUDDETECTOR can be used as a tool to improve the performance of approaches based on machine learning techniques. Finally, we report that the SVM classifier used in this work is based on the radial basis function kernel.

5.4 **Run-time Parameters**

When executing TAXFRAUDDETECTOR we provide the following parameters: supp = 0.6, conf = 0.6and lift = 1.05. We report that these values were chosen according to the opinions provided by SEFAZ-CE business experts.

When executing the algorithm from (Matos et al., 2015), we provided the same set of parameters that were used in their paper.

Finally, the SVM-based approach relies on the SVM package available in R (David Meyer, 2017; R Core Team, 2016); the following parameters are provided at execution time: *kernel* = "radial", *gamma* = 0.01, *cost* = 10. We report that the values given to *gamma* and *cost* were picked up after trying out different values, with *gamma* varied in the $[10^{-6}, 10^{-1}]$ range and *cost* varied in the $[10^1, 10^2]$ range.

6 EXPERIMENTAL EVALUATION

In this section we assess the quality of the results achieved by TAXFRAUDDETECTOR and its competitors by means of the measures defined in Table 2, and according to the data reported in the confusion matrix (Table 1).

The experiments relates to the results achieved when considering the dataset covering the year 2011. Table 3 shows the results. From the results, we notice that TAXFRAUDDETECTOR is able to achieve the best classification quality, with an F_1 score equal to 77%, thus indicating that our approach is able to detect potential fraudsters more effectively than our competitors. Another observation is that TAXFRAUDDETECTOR shows better results than the SVM-based classifier, and that the latter is able to improve its classification quality considerably once it is combined with our approach (or, to a lesser degree, with (Matos et al., 2015)). Finally, we report that results related to data covering the years 2009 and 2010 exhibit similar results (we omit them for brevity).

In general, we deem that the results show how feature selection, coupled with centrality measure (Boccaletti et al., 2006), is able to considerably improve



Figure 2: Degree distribution for the years 2010 and 2011. The X-axis is associated with the degree, while the Y-axis is associated with the occurrences of vertices having a given degree.

the classification of fraudsters, either for TAXFRAUD-DETECTOR, (Matos et al., 2015), or SVM. As such, we believe that centrality measure is an adequate feature for classification, since graphs generated during the classification process have a degree distribution that behaves according to the power law (Figure 2).

7 CONCLUSIONS

In this paper we proposed a new method to determine the risk that taxpayers have to commit tax frauds. The method extends and improves (Matos et al., 2015) in that it uses a new technique to discover key indicators of frauds by resorting to the centrality measure over a graph of indicators: this implicitly captures relationships between key fraud indicators.

On the one hand, we claim that previous methods fail to perform accurate predictions since they cannot cope effectively with changes that affect indicators over time. On the other hand, our technique relies on the observation that, once we are able to capture relationships between indicators, this allows to find out the most relevant ones. Moreover, the degree distribution of a graph of indicators behaves according to a power law, which in turn suggests that key indicators retain their importance regardless of the scale used to

Weighted degree distribution 2010

Table 3: Assessment of the quality of the results returned by	TAXFRAUDDETECTOR	and its competitors wh	ien analyzing the
SEFAZ-CE 2011 dataset.			

Method	Accuracy	Precision	Recall	F ₁ Score
TAXFRAUDDETECTOR	81.33%	78.14%	76.08%	77.0962%
(Matos et al., 2015)	51.27%	48.94%	51.11%	50.0014%
SVM using TAXFRAUDDETECTOR	56.26%	53.12%	47.23%	50.0021%
SVM using (Matos et al., 2015)	33.42%	30.07%	39.13%	34.0069%
SVM	87.49%	45.09%	8.22%	13.9112%

analyze them. As such, this scenario represents a typical complex network, hence a proper analysis of the underlying topology can offer useful insights into the network properties.

In the experimental evaluation we show that our approach achieves F_1 scores of about 54% greater than (Matos et al., 2015) when considering the dataset introduced by this work, while it maintains equivalent F_1 scores when considering the dataset introduced in (Matos et al., 2015). Furthermore, we show that our method is able to improve F_1 scores of about 47% with respect to an SVM-based approach, when considering the dataset introduced in this work.

As a future line of research, we are considering the application of other metrics over graph determinants to further improve the feature selection process; finally, we plan to explore more issues related to graph topology, which in turn have the potential to improve the accuracy of fraud detection.

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