

Analysis and Comparison of Traffic Accident Regression Prediction Model

Weihong Ma¹ and Zhenzhou Yuan²

MOE Key Laboratory for Urban Transportation Complex Systems Theory and Technology, Beijing Jiaotong University, Beijing 100044, China.

¹16120864@bjtu.edu.cn, ²zzyuan@bjtu.edu.cn

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Abstract: The purpose of this paper is to analyse the relationship between the number of road traffic accidents and road length, traffic conditions and other factors. Taking the number of road traffic accidents subject to Poisson regression, negative binomial (NB) regression and Zero Inflated Negative Binomial (NINB) regression as response variables, we construct a generalized linear model by introducing a joint function. We construct the Traffic Accident Prediction Model Based on Random Forest (RF) Regression. The defect models are compared, and based on the predictive model, selecting the significant factors and determining the degree of influence factors of road traffic accidents, reducing the number of traffic accidents and improve the overall security of the road.

1 INTRODUCTION

This paper studies the regression model of the number of traffic accidents. This paper studies the relationship between the number of traffic accidents and various influencing factors. Regression analysis was carried out on traffic accident number and influencing factors respectively, and strong correlation factors were selected. Based on the selected influencing factors, Poisson regression, NB regression, NINB regression and RF regression were used to compare the goodness of fit parameters of the model, select the model with the best fitting degree.

Analyzing the influencing factors of traffic accidents is the first condition to establish the traffic accident forecasting model. At the same time, it provides an important theoretical basis for the formulation of road traffic construction and traffic management measures so as to timely and pertinently take appropriate preventive measures and improvement measures. According to the existing relevant research results both at home and abroad, scholars at home and abroad have conducted extensive and in-depth research on the people, vehicles, road alignment and environment which are closely related to traffic accidents.

2 DOMESTIC AND FOREIGN RESEARCH INTRODUCTION

2.1 Influencing factors of traffic accidents

Chang et al. conducted a study on freeway traffic accident data from 1997 to 1998 in Taiwan. Studies have shown that: The number of lanes, the proportion of trucks, the length of road sections and the traffic volume are significantly and positively correlated with the number of traffic accidents (Chang L Y,2005).

Liande Zhong has studied the relationship between the number of highway traffic accidents and the road attributes, traffic attributes and environmental attributes and other factors, the research shows: whether the existence of the interchange zone, the average curve of the average curve, the cart ratio, the standard speed of the vehicle speed has a significant impact on the occurrence of traffic accidents(Liande Zhong,2008).

2.2 Traffic Accident Prediction Model

Traditional counting models, such as Poisson regression model and NB regression model, have been widely used in traffic accident prediction. Miaou and others used linear regression model and Poisson regression model to analyze the relationship between the number of truck accidents and the road alignment. The research shows that Poisson regression model is better than linear regression model(Miaou S P,1993).

Milton et al. Used a NB regression model to analyze the relationship between the number of traffic accidents in the main road in Washington state and the road conditions and traffic conditions, The research shows that the NB regression model has a good prediction effect(Milton J,1998).

Chen Yi used zero inflated Poisson model to fit the highway data. The research results show that when the vehicle flow reaches 18000 vehicles / day, the frequency of traffic accidents will increase significantly(Yi Chen,2013). At present, there are no scholars to study the RF regression model to predict traffic accidents.

3 ANALYSIS OF THE INFLUENCING FACTORS OF ROAD TRAFFIC ACCIDENTS

It is very important to analyze the law and influence mechanism of traffic accident by studying the effect of each influencing factor on traffic accidents and establishing a forecasting model of road traffic accidents so as to put forward corresponding improvement measures and preventive measures.

Firstly, we analyze the correlation between the number of traffic accidents and various influencing factors. By comparing the correlation coefficients, we select the factors that have a significant impact on the number of road traffic accidents. There are 200 available data (Specific data information in Table 1).

Table 1: Variable name and description.

Labels	Definition
Response variables	
Count	Number of total accidents
Continuous explanatory variables	
SLENGTH	Segment length
AADT	Annual average daily traffic (AADT) $\times 10^{-4}$
PSR	Pavement condition rating

AVGTRUCK	Average truck volume percentage
Labels	Definition
Categorical explanatory variables	
NOLANE0	Number of through lanes less than or equal to two
NOLANE1	Number of through lanes greater than two
RURAL0	Rural road
RURAL1	Urban road

Through the cross-linked list of factors, the correlation between the number of traffic accidents and various influencing factors is: AADT>NOLANE0>SLENGTH>AVGTRUCK>RURAL0>PSR.

The scattergrams of seven variables, Count, SLENGTH, AADT, NOLANE0, RURAL0, PSR and AVGTRUCK, are respectively obtained. The results are as follows:

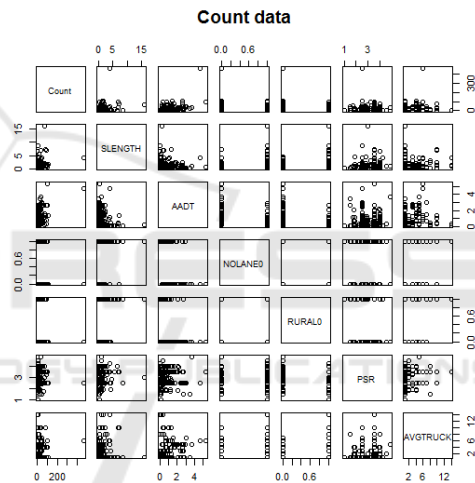


Figure 1: Scatter plot between the Count and the various factors

As can be seen from Figure 1, there is no obvious linear relationship between Count and each factor. There is a relatively weak linear relationship between SLENGTH and AADT and the number of traffic accidents. With the increase of AADT, the increase of Count is more obvious than that of SLENGTH. The number of traffic accidents with NOLANE0 of 1 was significantly greater than that of NOLANE0 with 0 .

4 ESTABLISH ROAD TRAFFIC ACCIDENT REGRESSION MODEL

This section will briefly introduce the theoretical system of Poisson regression model, NB regression model, NINB regression model and RF model. Based on these four model theories, we respectively construct road traffic accident prediction models.

Because the number of traffic accidents is a random variable. Firstly, we need to study the distribution of random variables. Then through the generalized linear regression model to study the relationship between the expected number of traffic accidents and various influencing factors. Finally, the connection function is used to achieve the fitting of the nonlinear relationship between the number of traffic accidents and various influencing factors. Generalized linear model is proposed by Nelder, which is very suitable for discrete traffic accident data. It has the following three aspects of the promotion of the traditional linear model(Zhuoheng Chen,2011).

(1) The distribution of the response variable Y can be taken from any distribution in the exponential distribution family;

(2) The linear combination of independent variables is $\eta = \beta_0 + \beta_1 \times x_1 + \dots + \beta_k \times x_k = X'\beta$. This is no different from the multiple linear regression model, Y, X desirable continuous or discrete values.

(3) The mean of response variables $E(Y) = \mu = h(X'\beta)$, h is monotonous and can guide..

Through training samples, we get a prediction model of traffic accident based on RF regression. We choose AIC criterion, BIC criterion to evaluate the goodness of fit of the generalized linear regression model, choose SSR to compare the goodness of fit of the RF regression model and the generalized linear regression model.

4.1 Poisson Regression Model

In fact, whether each vehicle has a traffic accident in each section can be regarded as a Bernoulli test. The probability of the incident is usually very small. If the number of vehicles entering the section within a certain statistical period is large enough, and the product of the number of vehicles and the event probability is moderate, the distribution of traffic accidents on each road segment can be described by Poisson distribution. Therefore, Poisson regression model is introduced for the prediction of traffic

accident number. The probability distribution of the Poisson regression model is as follows:

$$P(Y=y_i) = e^{-\lambda_i} \frac{\lambda_i^{y_i}}{y_i!} \quad (1)$$

y_i is the number of traffic accidents per unit time on the i-th road section; λ_i is the expected number of traffic accidents per unit time on the i-th road section (Yulong Pei,2003).

Below we establish the Poisson regression of road traffic accidents. Here logarithmic connection function is used to realize the Poisson regression fit between the number of traffic accidents and various influencing factors. After repeated model screening through the back method, the model with the highest goodness of fit includes four influencing variables: AVGTRUCK, NOLANE0, AADT and SLENGTH. Here by offset function to handle AADT and SLENGTH two exposure variables. It can be seen from the model that NOLANE0 has the greatest impact on the number of traffic accidents. The regression equation is as follows:

$$y = (SLENGTH * AADT)e^{3.9916 - 0.3683RURAL0 - 0.1901AVGTRUCK} \quad (2)$$

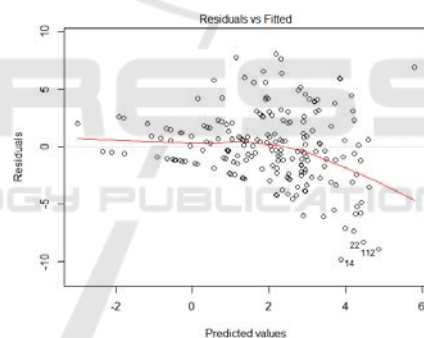


Figure 2: Poisson regression model Residual - Fitting Value graph

The result of model shows that:AIC=2698.7,BIC=2708.63,and SSR=1957.2, It can be seen from Fig. 2 that Residual values fluctuate in the [-10,10] range. The abnormal values increase with the increase of fitting values in the Poisson regression model, and the residuals tend to increase. The goodness of fit of the model is not ideal. The limitation of Poisson regression model lies in that the mean and variance are equal. Actually, most of the traffic accident data are characterized by excessive dispersion, ie, the variance is larger than the mean.

4.2 NB Regression Model

If the number of traffic accidents y_i of the unit time on the i section obeys the Poisson distribution, The

expected value of the number of accidents λ_i is subject to the gamma distribution, The number of traffic accidents y_i on the section i is subject to NB distribution(Min Chen,2012). The probability distribution of the NB regression models is as follows:

$$P(Y=y_i) = \frac{\Gamma(y_i + (1 + 1/K))}{\Gamma(1/K) \cdot y_i!} \cdot \left(\frac{1}{1 + K\lambda_i}\right)^{1/K} \cdot \left(\frac{K\lambda_i}{1 + K\lambda_i}\right)^{y_i} \quad (3)$$

In the formula, K is a discrete coefficient, Γ is a gamma distribution.

Below we establish the NB regression model of road traffic accidents. Here logarithmic connection function is used to realize the NB regression fit between the number of traffic accidents and various influencing factors. After repeated model screening through the back method, the model with the highest goodness of fit includes four influencing variables: AVGTRUCK、RURAL0、AADT、SLENGTH. Here by offset function to handle AADT and SLENGTH two exposure variables. From the model, it can be seen whether the country road has the greatest impact on the number of traffic accidents, and the following regression equation is obtained:

$$y = (SLENGTH * AADT)e^{3.9992 - 0.7012RURAL0 - 0.1266AVGTRUCK} \quad (4)$$

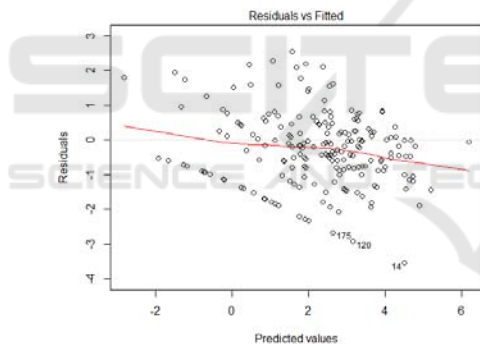


Figure 3: NB regression model residual fitting value

It can be seen from Fig. 3 that Residual values fluctuate in the $[-4,4]$ range, and the wave amplitude is smaller than that of Poisson regression. The result of model shows that: AIC=1363.3, BIC= 1376.513, SSR= 230.7843, which is much smaller than that of Poisson regression model. NB model is higher than the Poisson model and are more appropriate to the actual data. The fitting degree of the NB regression models is better.

4.3 ZINB Regression Model

ZIP regression model is the first choice to deal with ZI data. Its expression is clear, and it is more convenient to deal with. In the field of practical applications, zero expansion data will also appear as

follows: 1) there is a large discretization in the non zero part relative to the ordinary Poisson distribution; 2) the absence of observations. The ZINB regression model can solve the problem of large variance and zero expansion(Honglu Zhang,2015).

If there is a group of discrete random variables Y_{ij} ($i=1,2,\dots,m;j=1,2,\dots,n;N=\sum_{i=1}^m n_i$) have the following distribution:

$$P(Y_{ij}=y_{ij}) = \begin{cases} \varphi_{ij} + (1 - \varphi_{ij})(1 + \alpha_{ij})^{y_{ij}}, & y_{ij} = 0 \\ (1 - \varphi_{ij}) \frac{\Gamma(y_{ij} + 1/\alpha)}{\Gamma(1/\alpha) y_{ij}!} (1 + \alpha_{ij})^{y_{ij}} (1 + \alpha_{ij})^{-1/\alpha}, & y_{ij} > 0 \end{cases} \quad (5)$$

It is called Y_{ij} obeys the ZINB distribution.

Below we establish the NINB regression model of road traffic accidents. Here logarithmic connection function is used to realize the NINB regression fit between the number of traffic accidents and various influencing factors. After repeated model screening through the back method, the model with the highest goodness of fit includes four influencing variables: NOLANE0, AVGTRUCK, PSR, RURAL0, AADT, SLENGTH. Here by offset function to handle AADT and SLENGTH two exposure variables. From the model, it can be seen whether the country road has the greatest impact on the number of traffic accidents, and the following regression equation is obtained:

$$\begin{cases} \ln \lambda = \log(SLENGTH * AADT) - 4.4836 - 0.068NOLANE0 - 0.1512PSR - 0.1253AVGTRUCK - 0.6341RURAL0 \\ \log i(i-1) = \log(SLENGTH * AADT) - 4.504 - 11.943NOLANE0 - 6.508PSR + 1.613AVGTRUCK - 14.236RURAL0 \end{cases} \quad (6)$$

It is known from the model results that AIC=1362.182. Compared with the NB regression model, the AIC=1363.3 is smaller. The goodness of fit is higher than that of the NB model, and it is more appropriate to the actual data, so the fitting degree of the NB regression model with zero expansion is better.

4.4 RF Regression Model

As with other models, RF regression model can explain the effect of several independent variables (X_1, X_2, \dots, X_k) on the dependent variable Y . If the dependent variable Y has n observations, k independent variables are related to it. When constructing the decision tree, the random forest randomly selects n observations from the original data, some of them are selected multiple times, Some are not selected, this is Bootstrap resampling method. At the same time, random forest randomly selects some variables from k independent variables to determine the decision tree node. In this way, the

decision tree that builds each time may not be the same. In general, a random forest randomly generates hundreds to thousands of decision trees, and then selects the tree with the highest degree of repetition as the final result(Lihui Li,2017).

In the traffic accident forecasting, the eigenvector is established as the input characteristic by the influencing factors of the number of traffic accidents, and the traffic accident number corresponding to the eigenvector is taken as the forecasting result. The forecasting model is obtained by fitting the training samples.

Below we set up a RF regression model of road traffic accidents. After repeated model screening, the model with the highest goodness-of-fit includes the six influencing variables: RURAL0, NOLANE0, AVGTRUCK, PSR, AADT and SLENGEH. The IncNodePurity values of PSR, RURAL0 and AVGTRUCK are small among the influencing variables. The influence of this variable on the number of traffic accidents is larger. The figure below shows: Residuals in the RF regression model tend to stabilize as the number of decision trees increases.

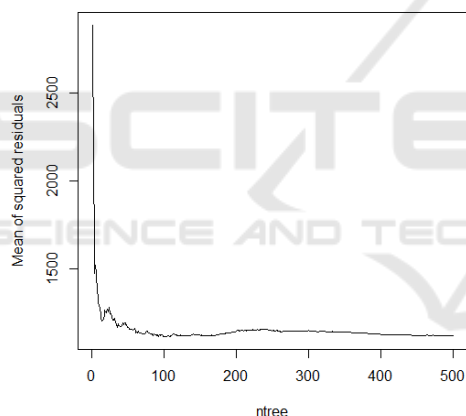


Figure 4: Simulation results

The model results show that the :SSR=1113.6. Compared with Poisson regression model, the SSR is smaller, which is larger than the SSR of NB regression model. Therefore, the goodness of fit of the RF regression model is higher than that of Poisson regression model, which is worse than the NB regression model. The machine learning prediction model has a low prediction accuracy on the number of traffic accidents.

5 CONCLUSION AND OUTLOOK

This paper tries to find a model that is closer to the actual traffic condition by carrying out Poisson regression,NB regression, ZINB regression and RF

regression on road traffic accidents. Assuming that the number of traffic accidents subject to different distributions, by selecting the strong influencing factors among the different factors in the regression model to build a model closer to the actual situation.

The simulation results show that under the existing traffic data, Poisson regression model has a poor fitting degree, followed by a RF regression model, and AIC difference between the NB regression and ZINB regression model is not very much. ZINB regression model has the best goodness of fit. All models eventually include the two variables:RURAL0 and AVGTRUCK, and the impact of RURAL0 on the number of road accidents in all three models is greater than the other factors. Urban roads are more prone to traffic accidents than rural roads; there are more traffic accidents on roads with large truck proportions. Therefore, we come to the conclusion that we should strengthen the management of urban road traffic conditions, the specific measures should be based on traffic characteristics of specific sections of the traffic investigation. Traffic management should be strengthened for areas with frequent and high traffic accidents. Controlling the number of trucks within a reasonable range can help reduce traffic accidents.

The factors considered in this paper may not be comprehensive. Due to the lack of data collection, the data related to traffic accidents will also affect the accuracy of the results of regression analysis. In the future, I hope to further study in this area and analyze the relationship between traffic accidents in a more comprehensive way from various perspectives. I hope that the best model of traffic accident can be fitted to achieve a more accurate prediction of traffic accidents.

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