# Artificial Neural Network Approach to Prediction of Protein-RNA Residue-base Contacts

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Keywords: Fully Connected Neural Network, Protein-RNA Interaction, Residue-base Contact.

Abstract: Protein-RNA complexes play essential roles in a cell, and are involved in the post-transcriptional regulation of gene expression. Therefore, it is important to analyze and elucidate structures of protein-RNA complexes and also contacts between residues and bases in their interactions. A method based on conditional random fields (CRFs) was developed for predicting residue-base contacts using evolutionary relationships between individual positions of a residue and a base. Further, the probabilistic model was modified to improve the prediction accuracy. Recently, many researchers focus on deep neural networks due to its classification performance. In this paper, we develop a neural network with five layers for predicting residue-base contacts. From computational experiments, in terms of the area under the receiver operating characteristic curve (AUC), the predictive performance of our proposed method was comparable or better than those of the CRF-based methods.

## **1 INTRODUCTION**

Interactions between proteins and RNAs are involved in the post-transcriptional regulation of gene expression including alternative splicing, polyadenylation, localization and translation (Glisovic et al., 2008). For instance, a ribosome is formed with multiple proteins and RNAs, and synthesizes proteins from messenger RNAs. Disruption of protein-RNA interactions may cause various diseases including cancers. Therefore, it is needed to obtain precise knowledge of contact positions between proteins and RNAs to understand their molecular function.

It is known that there are several RNA-binding domains such as RNA recognition motif (RRM), heterogeneous nuclear ribonucleoproteins (hnRNPs) (Beyer et al., 1977), the K-homology domains (Siomi et al., 1993), double-stranded RNA-binding domains (dsRBD) (Feng et al., 1992), TIA-1 (Kedersha et al., 1999) and zinc fingers (Hall, 2005). The sequence and structural properties of RNA-protein interaction sites in 211 RNA-protein chain pairs were investigated, and it was reported that 78% of hydrogen bonds involve amino acid side chains, and the remaining involve the protein backbone (Gupta and Gribskov, 2011). Several computational methods have been developed for predicting RNA-binding amino acid residues in proteins. Sun et al. proposed RNAProSite, which utilizes the random forest (Breiman, 2001) with electrostatic feature, triplet interface propensity, position-specific scoring matrices (PSSM) profile, geometrical characteristic and physicochemical property (Sun et al., 2016). Sharan et al. developed an integrated pipeline, called APRICOT, that identifies functional motifs in protein sequences using PSSMs, hidden Markov models of RNA-binding domains, and sequence-based features (Sharan et al., 2017). It was reported that APRICOT achieved sensitivities higher than or as good as RNAProSite and other high performing predictors. Tang et al. proposed PredRBR that utilizes gradient tree boosting and many kinds of sequence and structural site features (Tang et al., 2017).

On the other hand, concerning binding sites of RNAs, 24.6% of hydrogen bonds involve nucleobase-specific interactions, and the remaining involve the RNA backbone (Gupta and Gribskov, 2011). Alipanahi et al. proposed DeepBind that uses many RNA sequences with binding scores determined from protein binding microarray experiments, and extracts motif features by a deep learning technique, which outperformed 26 other methods such as FeatureRE-

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DOI: 10.5220/0007348101630167

In Proceedings of the 12th International Joint Conference on Biomedical Engineering Systems and Technologies (BIOSTEC 2019), pages 163-167 ISBN: 978-989-758-353-7

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DUCE (Weirauch et al., 2013) and BEEML-PBM (Zhao et al., 2011) when the correlation between the predicted and actual probe intensities was evaluated (Alipanahi et al., 2015). Zeng et al. systematically examined various models of convolutional neural networks to further improve DeepBind, and observed that deploying more convolutional kernels was always beneficial, but the local-pooling and additional convolutional layers were useful only in the motif occupancy task when higher-order features existed, and they did not achieve significant improvement (Zeng et al., 2016). These methods were developed for identifying RNA and DNA motifs bounded by transcription factors. However, both positions in binding RNA and protein were not identified. Methods for predicting residue-base contacts in protein-RNA interactions were proposed using conditional random fields (CRFs), which used evolutionary measurements obtained from multiple sequence alignments (Hayashida et al., 2013; Hayashida et al., 2018). For analyzing mechanisms of protein-RNA interactions in detail, we also deal with the problem of predicting residue-base contacts.

Recently, artificial neural network techniques (Le-Cun et al., 2015; Glorot et al., 2011) have been applied in many research fields due to its high classification performance. We explore neural network architectures to overcome the prediction accuracy by the CRF-based method. For evaluating the proposed neural network, we perform computational experiments as done in the previous study. The results show that in terms of the area under the receiver operating characteristic curve (AUC), the predictive performance of our proposed method was comparable or better than those of the CRF-based methods.

### 2 METHODS

We address the following problem. Given two sequences  $\mathbf{p} = p_1 \cdots p_{|\mathbf{p}|}$  and  $\mathbf{r} = r_1 \cdots r_{|\mathbf{r}|}$  of a protein and RNA, find whether or not  $p_i$  and  $r_j$  interacts for all *i* and *j*. We briefly review the CRF-based method and an evolutionary measurement MI<sub>p</sub> (mutual information improved) proposed by (Dunn et al., 2008) between positions of amino acids and bases, and the latter is also used by our method. After that, we explain our neural network architecture.

#### 2.1 Evolutionary Measurement

One method of measuring coevolutionary relationship between positions of a residue and a base in protein and RNA sequences is to calculate mutual information from multiple sequence alignments. MI<sub>p</sub> was developed to improve protein residue-residue contact prediction by subtracting a bias from mutual information. Suppose that we have two multiple alignments for protein and RNA sequences,  $\boldsymbol{p} = p_1 \cdots p_{|\boldsymbol{p}|}$  and  $\boldsymbol{r} = r_1 \cdots r_{|\boldsymbol{r}|}$ , respectively, where  $|\boldsymbol{p}|$  means the length of  $\boldsymbol{p}$ . If *i*-th residue  $p_i$  and *j*-th base  $r_j$  interact with each other to maintain a biological system in an individual organism, there must be some relationship between them. Then, mutual information between positions *i* and *j* is defined by  $m_{ij} = \sum_{a \in A} \sum_{b \in B} Pr(p_i = a, r_j = b) \log \frac{Pr(p_i = a, r_j = b)}{Pr(p_i = a)Pr(r_j = b)}$ , where *A* and *B* denote sets of amino acids and bases, respectively. MI<sub>p</sub> was modified as  $m_{ij} - \frac{\sum_{i=1}^{|\boldsymbol{p}|} m_{ij} \sum_{j=1}^{|\boldsymbol{p}|} m_{ij}}{\sum_{i=1}^{|\boldsymbol{p}|} \sum_{i=1}^{|\boldsymbol{p}|} m_{ij}}$  for our purpose.

## 2.2 Conditional Random Field (CRF)-based Method

Conditional random fields (CRFs) were proposed by extending Markov random fields (Lafferty et al., 2001). The CRF with a strictly positive density in the previous study was defined by  $Pr(x_{ij}|\mathbf{x}_{\mathcal{N}_{ij}}, \mathbf{m}, \mathbf{p}, \mathbf{r}) = \frac{1}{Z_{ij}} \exp\left\{\mathbf{w}_{j}^{T} \mathbf{f}_{ij}(\mathbf{x}, \mathbf{m}, \mathbf{p}, \mathbf{r}) + \mathbf{w}_{g}^{T} \sum_{(k,l) \in \mathcal{N}_{ij}} \mathbf{g}_{ijkl}(\mathbf{x}, \mathbf{m}, \mathbf{p}, \mathbf{r})\right\}$ , where  $x_{ij} = 1$ means that *i*-th residue and *j*-th base interact with each other,  $x_{ij} = -1$  otherwise,  $\mathbf{f}_{ij}(\mathbf{x}, \mathbf{m}, \mathbf{p}, \mathbf{r}) = x_{ij} \left( \begin{pmatrix} 1 \\ m_{ij} \\ \max_{(k,l) \in \mathcal{N}_{ij}} m_{kl} \\ \min_{(k,l) \in \mathcal{N}_{ij}} m_{kl} \end{pmatrix} \oplus \delta_{(p_i, r_j)} \right)$ ,  $\mathbf{g}_{ijkl}(\mathbf{x}, \mathbf{m}, \mathbf{p}, \mathbf{r}) = x_{ij} x_{kl} \begin{pmatrix} |m_{ij} - m_{kl}| \\ m_{ij} m_{kl} \end{pmatrix}$ ,  $\delta_{(p_i, r_j)}$  de-

notes a  $|A| \times |B|$  dimensional vector which only the element corresponding to the amino acid  $p_i$  and base  $r_j$  is one,  $\mathcal{N}_{ij}$  for  $i = 1, \dots, |\mathbf{p}|$  and  $j = 1, \dots, |\mathbf{r}|$  denotes a set of adjacent pairs of (i, j), and was defined by  $(i \pm 1, j), (i, j \pm 1)$  (see Figure 1). In this method,  $m_{i'j'}$  at the gray square in the figure was given as one of input data for a residue-base pair (i, j), that is,  $(i', j') \in \{(i, j)\} \cup \mathcal{N}_{ij} \cup \bigcup_{(k,l) \in \mathcal{N}_{ij}} \mathcal{N}_{kl}$ . The probability model contains dependency relationships between positions (i, j) and  $(i', j') \in \mathcal{N}_{ij}$ .

Parameters  $\boldsymbol{w}_f$  and  $\boldsymbol{w}_g$  in the CRF model are determined by maximizing the pseudo-likelihood function,  $L(\boldsymbol{\theta}) = \prod_n \prod_{i=1}^{|\boldsymbol{p}|} \prod_{j=1}^{|\boldsymbol{r}|} Pr(x_{ij}^{(n)} | \boldsymbol{x}_{\mathcal{N}_{ij}}^{(n)}, \boldsymbol{m}^{(n)}, \boldsymbol{p}^{(n)}, \boldsymbol{r}^{(n)}, \boldsymbol{\theta})$ given  $\boldsymbol{x}^{(n)}, \boldsymbol{m}^{(n)}$  for each sequence pair  $\boldsymbol{p}^{(n)}, \boldsymbol{r}^{(n)}$ .



Figure 1: Illustration of adjacent pairs of (i, j). The positions (i', j') at the gray squares are included in  $\mathcal{N}_{ij}$ .

#### 2.3 Neural Network Architecture

We propose a neural network with five layers as shown in Figure 2. The input layer has  $(2k_m + 1)^2 +$  $(|A|+|B|)(2k_s+1)$  neurons having evolutionary measurement values of pairs (i', j') for all  $i - k_m \le i' \le i'$  $i+k_m, j-k_m \le j' \le j+k_m$ , and one-hot vectors corresponding to subsequences from  $p_{i-k_s}$  to  $p_{i+k_s}$  of protein **p** and from  $r_{j-k_s}$  to  $r_{j+k_s}$  of RNA **r**, where  $k_m$ and  $k_s$  are constant integers, and a one-hot vector for a constant number c is defined as a vector that only c-th element is one and the others are zero. For example, when  $k_m = 2$ ,  $m_{i' j'}$  at the gray and white square in Figure 1 is given with respect to (i, j) to the input layer. In addition, amino acids can be classified, and |A| can be equal or less than 20. The neural network has three hidden layers with  $n_1, n_2$ , and  $n_3$  neurons, respectively. The output layer has two neurons corresponding to the two classification results. All successive layers are fully connected and the rectified linear unit (ReLU) (Glorot et al., 2011) defined by  $f(x) = \max\{0, x\}$  is applied to the output of each neuron except the final layer. The softmax function is applied in the final layer. In addition, bias variables are added to each neuron except the input layer. Then, the total number of parameters is  $((2k_m+1)^2 + (|A| +$  $|B|(2k_s+1)n_1+n_1+\sum_{i=1}^3 \{n_in_{i+1}+n_{i+1}\}+2n_3+2.$ 



Figure 2: Illustration of the neural network with five layers.

### **3 RESULTS**

For evaluation of the proposed method, we used the same dataset as that in the previous study, which consists of residue-base pairs included in thirteen protein-RNA pairs in four complexes identified by '1yl4', '2hgu','3kc4', and '3kcr' in PDB (Rose et al., 2017) as shown in Table 1.

Each line in the table shows a protein-RNA pair, the PDB identifier, the chain identifier, the protein and RNA sequences p, r in UniProt and GenBank databases (The UniProt Consortium, 2017; Benson et al., 2011), the length, and the number of contacts between residues and bases in the protein and the RNA. It was assumed that *i*-th residue and *j*-th base interact with each other if the Euclidean distance between atoms of the residue and base is less than or equal to 3 Å because the distances of hydrogen bonds are about 2.7 to 2.9 Å.

We used multiple sequence alignments of Pfam and Rfam databases (Finn et al., 2016; Kalvari et al., 2018) for the protein p and RNA r to calculate MI<sub>p</sub>. We examined classifications of amino acids with 8, 10, and 15 groups according to the study (Murphy et al., 2000), that is, |A| took 8, 10, 15, and 20, and MI<sub>p</sub> was calculated based on each case of A (see Table 2).

We performed cross-validation procedures, and took the average of AUC scores as well as the previous study, where among thirteen protein-RNA pairs in Table 1, all residue-base pairs included in one protein-RNA pair were used for test, and the others were used for training. We examined the window size by varying the values of  $k_m$  and  $k_s$ , and set  $n_1 = 750$ ,  $n_2 = 680$ , and  $n_3 = 250$ . We used the tensorflow-gpu library (version 1.4.1) to minimize the cross entropy of the output and to calculate the AUC score (Abadi et al., 2015).

Table 3 shows the results on average AUC scores by the CRF-based method and the proposed fully-connected neural network method in the cases  $(k_m, k_s) = (1, 2), (2, 1), (2, 2)$ . In the three cases, the AUC scores in the case of (2, 1) were better than those in other cases in the same classification of amino acids. It implies that amino acids and bases at positions  $(i \pm 2, j \pm 2)$  far from the position of interest (i, j) were not effective to enhance the prediction accuracy. On the other hand, the evolutionary measurement  $MI_p$  between positions  $(i \pm 2, j')$  and  $(i', j \pm 2)$  for  $i - 2 \le i' \le i + 2, j - 2 \le j' \le j + 2$  were useful. It is expected that the neural network with  $(k_m, k_s) = (2, 2)$  would be equivalent to the neural network with (2,1) if appropriate parameters are estimated as zero, and the AUC score with (2,2) would

PDB	Protein sequence			RNA sequence			# contacts
	chain	UniProt	length	chain	GenBank	length	
1yl4	K	RS8_THET8	135	Α	M26923	1889	29
1yl4	Μ	RS10_THET8	97	Α	M26923	1711	20
1yl4	0	RS12_THET8	122	A	M26923	1972	45
1yl4	Т	RS17_THET8	69	Α	M26923	1690	29
2hgu	R	RL18_THETH	110	В	X01554	1543	28
2hgu	Ζ	RL27_THET8	81	Α	X12612	1356	20
2hgu	5	RL33_THET8	48	A	X12612	1445	18
3kc4	Е	RS5_ECOLI	67	A	J01695	1701	13
3kc4	G	RS7_ECOLI	147	Α	J01695	1941	25
3kc4	0	RS15_ECO57	83	Α	J01695	1821	21
3kc4	Q	RS17_ECOLI	69	Α	J01695	1690	18
3kcr	W	RL27_ECOLI	77	8	J01695	1356	18
3kcr	3	RL35_ECOLI	61	8	J01695	1337	12

Table 1: Dataset of the residue-base pairs in protein-RNA complexes.

Table 2: Grouping of amino acids (Murphy et al., 2000).

#groups	groups of amino acids
8	(MLVIC) (GA) (TS) (P) (FYW)
	(DENQ) (RK) (H)
10	(MLVI)(C)(G)(A)(TS)(P)
	(FYW) (DENQ) (RK) (H)
15	(MLVI)(C)(G)(A)(T)(S)(P)
	(FY) (W) (D) (E) (N) (Q) (RK) (H)

Table 3: Results on average AUC scores by the CRFbased method and the proposed neural network method with  $(k_m, k_s) = (1, 2), (2, 1), (2, 2).$ 

#groups	CRF	Proposed			
		(1,2)	(2,1)	(2,2)	
8	0.692	0.671	0.674	0.668	
10	0.699	0.673	0.684	0.681	
15	0.699	0.670	0.711	0.682	
20	0.693	0.665	0.690	0.678	

be larger than or equal to that with (2,1). However, the AUC score with (2,1) was larger than that with (2,2).

For classification of amino acids, as reported in the previous study, the AUC score with 15 groups was better than others in almost all cases. In addition, the AUC score by our method with  $(k_m, k_s) = (2, 1)$ and 15 groups was better than that by the CRF-based method.

## 4 CONCLUSIONS

We proposed a neural network approach to prediction of protein-RNA residue-base contacts. In the neural network, neurons between successive layers were fully connected, and the ReLU activation function was applied. From the cross-validation computational experiments to evaluate the proposed method, the results show that in terms of the area under the receiver operating characteristic curve (AUC), the predictive performance of our proposed method was comparable or better than those of the CRF-based method. As future work, other types of advanced neural networks should be examined for further improvement of prediction accuracy, and for understanding interactions between residues and bases in detail. In our method, subsequences as long as motifs cannot be dealt. Therefore, we would like to improve our method to deal with longer subsequences.

## ACKNOWLEDGEMENTS

This work was partially supported by Grants-in-Aid #16K00392 and #16KT0020 from JSPS, Japan.

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