

Kohonen Map Modification for Classification Tasks

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Abstract: This paper aims to present a classification model based on Kohonen maps with a modified learning mechanism and structure as well. Modification of the model structure consists of its modification for hierarchical training and recall. The change of the learning process is the transition from unsupervised to supervised learning. Experiments were performed with the modified model to verify changes in the model and compare the results with other research.

1 INTRODUCTION

A variety of methods are available for advanced data processing, often in the field of artificial intelligence. Their use then depends on what data we have and what tasks we want to solve. One group of possible tools for the implementation of machine learning or data analysis has quite a long been a neural network.

For the learning of neural networks are used two types of learning methods. In unsupervised learning, we only have unrated input data that we intend to analyze in some way. This procedure is typically used in the early stages of data analysis when we examine the structure of the data, its internal relationships, and its character.

In supervised learning, we train the model not only with the input patterns but also with the required output. These examples of the $R^n > R^m$ transformation are used to form internal rules or model parameter settings. This approach is suitable for tasks with the desired transformation function, e.g., classification.

If we use a neural network, our goal is to learn the network to be able to respond appropriately to inputs that have not been trained with (the principle of generalization). Therefore, two disjoint data sets - training and testing - are typically used. The process of using the model can thus be divided into two main phases - the setting phase (learning) and the production phase (recall). The production phase is the very reason for the existence of the model, in it, the learned settings are used for processing of previously unseen (test) input data.

A useful but nowadays not very frequently used model is the so-called Kohonen map, which is designed for unsupervised learning and therefore cluster data analysis. The big advantage of the model is a visual representation of network activity.

The author worked with Kohonen maps previously, and this work showed the weaknesses of learning algorithms (esp. 2D area fragmentation) and the limitations of unsupervised learning. On the other hand, the solved tasks revealed that Kohonen maps are very comfortable for use in systems with a required visual representation of learning dynamics. That was the primary motivation for modifying of Kohonen network model and extending its capabilities presented in this paper.

Therefore, a modified learning algorithm and a multi-level model structure based on Kohonen maps were designed. The model was experimentally used (as the proof of concept) for the task of economic data processing (Vochozka et al., 2017) and preliminarily tested (Jelínek, 2018). This paper aims to present the actual state of the model and new experiments with it to demonstrate its usefulness.

The following chapters are organized as follows. In Chapter 2 is briefly discussed the related work. Chapter 3 focuses on a description of the standard Kohonen map model and shows the parameters of it. Chapter 4 then concentrates on the description of the modifications that were made, and Chapter 5 focuses on experiments with the model conducted primarily to verify the benefits of the proposed modifications.

2 RELATED WORK

When we talk about neural networks for the implementation of machine learning or data analysis, we usually mean a neural network based on an artificial neuron model (McCulloch and Pitts, 1943). Probably the greatest attention was given to models of multi-layered perceptron (Rosenblatt, 1957) and models based on this principle and using back propagation method of learning (Rumelhart et al., 1986).

The multilayer artificial neural network models have their renaissance nowadays, primarily due to the deep learning paradigm. This approach enables the model to learn patterns on a different level of abstraction. However, our approach is not of this kind. The deep learning models use the same input set all the time; our model reduces the set in the course of the learning process.

A typical example of the slightly different neural network model with unsupervised learning is the ART2 algorithm and model (Carpenter and Grossberg, 1987), which is capable of solving cluster analysis task, and its operation can be modified by adjusting the sensitivity of the model to differences in input data. The higher the sensitivity, the more output categories or clusters the system creates.

The Kohonen map (Kohonen, 1982) was introduced in the 1980s as most basic models of neural networks and is classified into a group of Self-organizing maps. In some ways, the Kohonen map can remind us of the ART2 model. The similarity lies in the same requirements on input data (number vectors). Similar is also the structure of the network, which is essentially two-layer. However, Kohonen map used 2D second layer and is focused on the visual interpretation of the output and is therefore useful both for the better understanding of the task and, e.g., for use in a dynamic online environment. An example of such usage can be monitoring the state of the system and its dynamics (Jelínek, 1992).

We can find also works concentrating on hierarchical usage of Kohonen maps. In (Rauber et al., 2002) the hierarchy is constructed dynamically in the case of clustering very different input patterns into one output cell. However, our model is based on supervised learning and uses of extended information about correct input classification for hierarchical reduction of the input set. Modification of Self Organizing Maps for supervised learning based on RBF is shown in (Fritzke, 1994), our model uses a different approach to that problem.

3 KOHONEN MAP

The core activity of the Kohonen map is assigning input patterns to the cells of the second layer (i.e., the output clusters representing by these cells) based on the similarity of patterns.

The input layer of the Kohonen map is composed of the same number of cells as the dimension n of the input space R^n is. The output layer is two-dimensional and is also referred to as the Kohonen layer. This structure was chosen concerning output visualization. The input and output layers are fully interconnected from the input to the output one with links whose weights are interpretable as the centroid of the input patterns cluster represented by the selected cell of the output layer. The number of output layer cells is the model parameter.

In the production phase, test patterns are submitted at the input of the model. Their distance (here the Euclidean one) is calculated from the output layer cell centroids, and the input pattern is assigned to the output cell, from which it has the smallest distance. Assigning the input pattern to the output cell can be visualized in the output layer as shown in Figure 1.

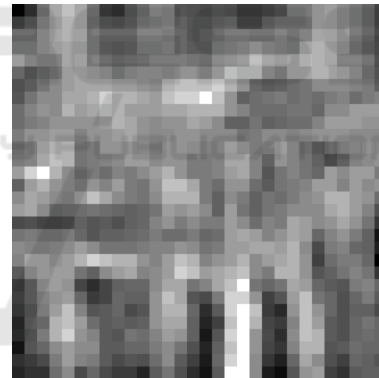


Figure 1: Kohonen layer visualized according to the number of patterns represented by cells (the more patterns, the darker color).

The learning of the Kohonen map is an extension of the production phase and is iterative. During it, the values of the weights leading to the cell representing the pattern are modified (the winning cell, the pattern was assigned to it) so as the weights to the cells in its neighborhood. The centroids of all these cells move towards the vector representing the pattern according to the formula (1).

$$c_i^{new} = (1 - \alpha)c_i^{old} + \alpha \cdot s_i \quad (1)$$

In it the α is the learning coefficient for the winning cell, usually with the value from the interval (0,1), c_i is the i th coordinate of the cell's centroid, and s_i is the i th coordinate of the given input pattern.

The values of weights leading to the neighbor cells in Kohonen layer are modified according to the same formula, but with a different learning coefficient value α_{ij} adjusted to respect the distance of a particular cell from the winning one:

$$\alpha_{ij} = \frac{\alpha}{(1 + d_{ij})} \quad (2)$$

Coordinates i and j are taken relative to the winning cell with position [0, 0]. The distance d_{ij} from the winning cell in these relative coordinates is then calculated as Euclidean one. The neighborhood of the winning cell is defined by the limit value of $d_{ij} \leq d_{max}$.

The Kohonen map also includes a mechanism to equalize the frequency of cell victory in the output layer. For each of them, the normalized frequency of their victories in the representation of the training models f_q is calculated with the normalized value in the interval (0; 1). This is then used to modify the distance of the pattern from the centroid.

$$w_{pq} = d_{pq}(f_q + K) \quad (3)$$

In the formula (3), w_{pq} is the modified pattern p distance from centroid q , d_{pq} the Euclidean distance of them and K a global model parameter to limit the effect of the equalization mechanism. The calculated distance w_{pq} is then used in the learning process. The described mechanism ensures that during the learning the weights of the whole Kohonen layer will gradually be adjusted. The size of this layer together with the number P of input patterns determines the sensitivity of the network to the differences between the input patterns.

It was also necessary to choose the appropriate criterion for determining the end of learning (Jelínek, 2018). It is based on the average normalized distance v in the 2D layer through which the pattern "shifts" between the two iterations as shown in the formula (4).

$$v = \frac{1}{\sqrt{2}NP} \sum_P \sqrt{\Delta i^2 + \Delta j^2} \quad (4)$$

The distance is calculated on the square-shaped Kohonen layer (with N cells on the side) between the two iterations of the input set P . The v value is

compared to the maximum allowable value v_{max} indicating the average maximum shift of patterns

allowed in one iteration. For the learned model with a frequency equalization mechanism, the v will be only a small value.

The main parameters of the Kohonen maps are the learning coefficient α , the way of setting the decrease of this coefficient for the cells around the winning cell, the size of the neighborhood given by d_{max} and the number of cells in the two-dimensional output layer. Also, the behavior of the model influences the value v_{max} and the coefficient K in formula (3) and its possible change over time.

4 MODEL MODIFICATIONS

Due to previous experience with the use of Kohonen maps and their application potential, the modified learning algorithm and the multilevel structure of the model were designed for them. This paper presents the current state of the model together with experiments aimed at an examination of the benefits of the proposed modifications.

4.1 Modified Learning Method

The goal of learning is to get an adjusted model that is capable of specific generalization, i.e., adequate responses to patterns that have not been trained on. The model described above used unsupervised learning, modification using supervised learning applicable to classification tasks will be introduced.

At the learning stage, the first change was in the fact that after finding the winning cell in the Kohonen layer, the model also stores the classification of the training patterns that were assigned to it. With the help of a known classification of the training set, for each output cell we can determine the percentage (or probability) rate of output categories in that cell, which can be used in the production phase to evaluate the test patterns in one of these two ways (Jelínek, 2018):

- *Probability evaluation.* We select the most likely category, so the test input pattern is always classified. The assumption here is the same distribution of *a priori* probabilities of output categories.
- *Absolute evaluation.* We only evaluate a test pattern if it is assigned to a winning cell representing only one category. A significant percentage of input patterns can thus be left unclassified.

Both mentioned ways are used in the production phase of the hierarchical model (absolute evaluation in intermediate steps, probability evaluation in the final step where it is necessary to evaluate all patterns). So the modified model already uses at the production stage additional output information.

It has also been shown in the course of model experiments, that classification task on data with complex transformation $R^n > R^m$ tend to a state where the same classified patterns are assigned to output layer cells that are often very distant from each other. This phenomenon affects the overall efficiency of the model that must respect this fragmentation.

The effort was to limit this behavior by using the output categorization directly in the model's learning phase. In this case, the model is trained on data that are a conjunction of the original input and the desired output (classification). For example, if we have a classification task performing the transformation $R^d > B^l$, where B^l represents a one-dimensional binary space (one binary coordinate), the model will be taught on the input set $R^d \cap B^l$. In the production phase, the last coordinate b_l is not used in the calculations because the input test vectors will not contain it (their classification is not known).

The described modification significantly changes the model settings, but it has turned out to be a positive change under certain conditions. The critical factor here is to what extent the output (often binary) classification should be projected into the training input. If this projection is in full a binary value and inputs from R^d are normalized to a range (0; 1), the model settings are distorted too much, and the model is not capable of generalizing. Therefore, the new reduction factor u was implemented to limit this projection according to formula (5)

$$inp_{x+|R|} = ub_x, \quad (5)$$

where $inp_{x+|R|}$ is the value of the input of the model (preceded by the coordinates of the original input from the R space) and b_x is the original classification ($b_x = 0$ or $b_x = 1$ for pure binary classification). The factor u has a value from the interval (0; 1) and represents the next parameter of the model.

4.2 Model with Hierarchy Structure

The fundamental change in the work with the Kohonen map is its repeated use with a different training set. This set can be, e.g., quite uneven regarding the representation of output categories or too large for the actual size of the Kohonen layer. The modified model addresses this problem by gradually reducing this set by eliminating correctly classified

training patterns at the end of each learning iteration. In the next iteration is a new instance of the map already learned with a training set containing only problematic (not yet categorized) patterns. The underlying idea of this approach is to use Kohonen map internal mechanisms so that the map in every step refines its classification capabilities.

Thus, in each model step, a separate Kohonen map is used. After learning, the cells of the Kohonen layer are analyzed, and it is examined whether only one output category is assigned to the given cell. If this is the case, we can say that the map can uniquely and correctly classify these patterns in accordance with the desired output and they can be excluded from the training set (Figure 2). The successful classification is considered as:

- *Basic classification.* Assignment of the pattern to a cell representing only patterns of the same category.
- *Strict classification.* Assignment of the pattern to a cell according to the previous bullet and additionally adjacent to only the same (representing the same category) or empty cells (not representing any pattern).

The selection of one of the above classification methods is a parameter of the model.

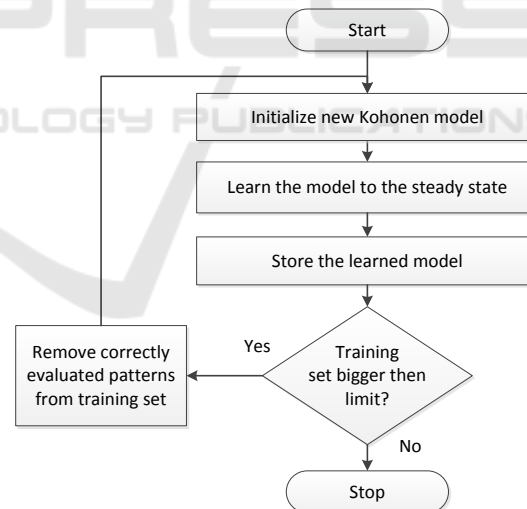


Figure 2: Learning phase of the modified model (Vochozka et al., 2017).

For the real use of the proposed model, two criteria are crucial. The first one is the criterion of learning termination in each step (level) of hierarchical model learning. The criterion of the maximum average shift distance between the 2D layer cells defined in formula (4) was used.

The second criterion is that of the overall ability of the whole set of learned sub-models to correctly

classify the training and later the test set of patterns and can be implemented in several ways. The minimum size of the training set, which still makes sense for learning, was used in the model. Its higher value reduces the number of hierarchical classification steps but also limits the sensitivity of the model.

In the production phase (Figure 3), the classification method differs depending on whether we are in the last hierarchical step or not. For the last model in the hierarchical structure, the probability evaluation is always used, where the pattern is assigned to the most likely category resulted from the learning process.

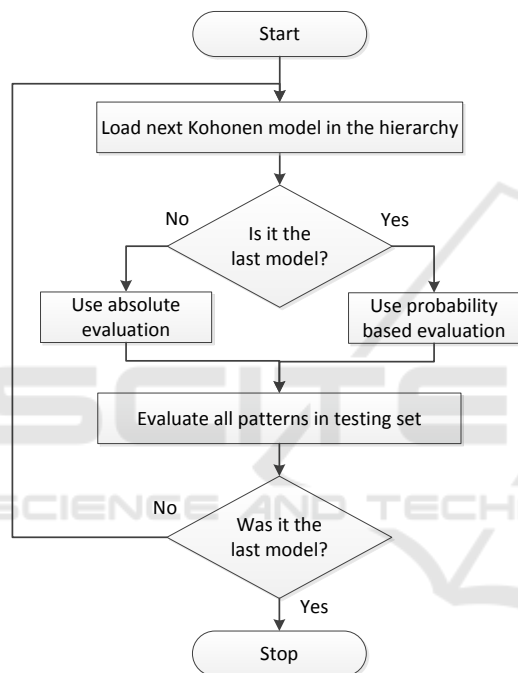


Figure 3: Production phase of the modified model (Vochozka et al., 2017).

The modified model was set up using 11 parameters including both the Kohonen map original ones (used in each iteration) and the other ones characterizing the hierarchical model's operation.

5 EXPERIMENTS

The experiments carried out were aimed at confirming the preliminary hypothesis that both modifications of the Kohonen map model are beneficial to the generalization quality and hence the classification of the test set of patterns. The first group of experiments was focused on model behavior

with artificial data; the second group concentrated on a comparison of results on standard datasets.

The first dataset was created to represent a complex nonlinear transformation from the input space R^d to the space B^l (Jelínek, 2018). 10,000 training and test patterns were generated with random values of the coordinates from R^d space uniformly generated in the interval (0; 1).

One test set and two training sets were created. From the training sets one was for the classical learning of the model (only inputs from R^d) and the other one extended with the output b_l (the network input dimension increased to R^5 where the fifth coordinate was b_l). Experiments have been optimized for maximizing the number of adequately classified test patterns.

As mentioned above, the model has adjustable parameters that significantly affect its results. Manually searching for optimal setup would be a lengthy process, and therefore, a superstructure of the model was used implementing an optimization mechanism based on genetic algorithms.

Two variants of the model's setting have been researched. The first one focused on modified model learning and worked with a single level of the hierarchical model (as if the model was not hierarchically modified). The second variant also involved a hierarchical modification of the model structure, and the maximum number of levels was limited to 10.

The best results are presented in the following Table 1. These are the best from 406 experimental settings of the model calculated by the genetic algorithm for each variant.

Table 1: Best results for different settings (Jelínek, 2018).

Parameter	Max. 1 level		Max. 10 levels	
	classic	extended	classic	extended
Number of 2D cells	40*40	35*35	40*40	35*35
Classification criterion	basic	strict	strict	Strict
Reduction factor	-	0.2	-	0.3
Real levels	1	1	10	3
Total learning iterations	33	118	238	515
Test patterns correctly classified	7998	8472	7985	8643
Model success [%]	79.98	84.72	79.85	86.43

It is clear from the table that the use of the modified learning process brings a significant improvement in the classification capabilities of the network over the original learning process. The key

output is the finding that to achieve better results with normalized data, the output values used for learning (initially 0 and 1) must be reduced by the reduction factor. Its appropriate setting was found by genetic algorithm and was 0.2 or 0.3 (see the Reduction factor row in Table 1).

The different number of 2D cells in different scenarios also shows that model with extended input set was able to obtain best results in the scenario with fewer cells in the 2D layer, than the model with standard input. The learning and overall performance of the model with extended input were thus more effective.

The sample visual outputs of the 2D network shown in Figure 4 demonstrate the effect of modified learning. The cells representing the patterns rated 0 are light grey, the patterns rated 1 are black. We get "clean" colors for cells containing input patterns included in only one category, for cells containing patterns of different categories the color is mixed, which respects the number of patterns in a cell with different output categories. The influence of additional output information on the final network setting is quite apparent (right), and the fragmentation from using the classical learning algorithm (left) almost did not occur.

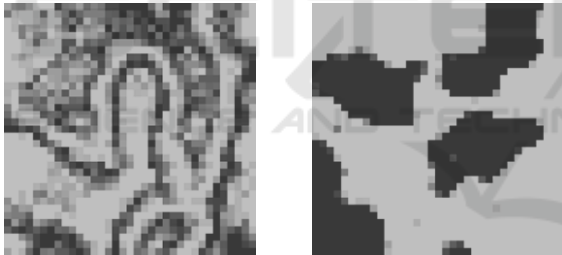


Figure 4: Influence of modified learning algorithm (Jelínek, 2018).

The results can still be improved by using a hierarchical modification of the model; the added value, however, is not so high in this case (quality improvement of 1.71 %). The question, however, is whether the appropriate data was used to maximize it. In this case, the training set was evenly generated, but the benefit could be more significant with data with unequally represented output categories or different *a priori* probabilities of them.

The second group of experiments was aimed at comparing model results with other approaches on standard datasets. They were obtained from the UCI Machine Learning Repository (Dheeru and Taniskidou, 2017). Three sets were selected with different focus and number of input and output attributes.

The first set is the Letter Recognition Data Set (Lett) presented in (Frey and Slate, 1991). Input data derive from black and white images of 26 alphabet letters written in 20 different fonts; more images were obtained by inserting random noise into existing ones. Each input vector contains 16 values resulting from the calculation of one-bit raster image values; the output consists of a single value - the letter captured on the figure. The set contains a total of 20 000 images. The rule-based classification method is also presented in (Frey and Slate, 1991); the best rate of correctly classified patterns is 82.7%.

To verify the presented model two disjoint sets were created - for training (16000 patterns) and testing (4000 patterns). The output was modified to 26 single-bit attributes (only one output value is one for each letter, others are zero). Since the output is, unlike the model description, not B^l but B^{26} , it was necessary to select the winning attribute for the output. The highest output attribute value does it. Similar procedures also were used in the experiments described below.

Experiments with this dataset did not reach the expected values and did not achieve the reference value mentioned in (Frey and Slate, 1991). The main reason for this is difficult to identify, but it can be due to the model parameter's limits, especially in conjunction with the $R^{16} > B^{26}$ nonlinear transformation. Inputs were pre-processed here, which has reduced their number but has increased the requirements on generalization capabilities of the model too.

The second dataset was the Semeion Handwritten Digit Data Set (Sem) described and used in (Buscema, 1998). The set contains 1593 digital black and white images in a 16x16 resolution. The output is the only value identifying the digit. The article also states the best classification using a combination of several neural networks at 93.09%.

The input for our model was 256 binary attributes (picture 16 x 16) and output ten binary values with the same meaning as in the previous set and with the same criterion for the best output selection. For the training of the model, 1200 patterns were randomly selected, for testing the remaining 393 ones (as recommended).

The results obtained with this dataset have already met the expectations. The model was able to exceed the reference value in the classification quality (Buscema, 1998), and the influence of the extended input data on the outputs of learning the model was also positive.

The last used dataset was designed for testing of accurate detection of room occupancy from data obtained from several types of sensors. The set was

published in (Candanedo and Feldheim, 2016) along with an extensive set of experimental results. The data are already divided into a training set of 8143 patterns and two test sets (Occ 1 and Occ 2) of 2665 and 8926 patterns. The best-achieved classification results for Occ 1 were 97.9% and for Occ 2 99.33%.

The original data were adapted for the use in our experiment. The input was seven real normalized values, and the output was one of two categories (room occupied, empty).

The expected results were calculated for the Occ 1 test set; the model again improved the best result described in (Candanedo and Feldheim, 2016), both for the classic and extended training set. For Occ 2, however, the best classification was achieved using standard input. This result has shown that the model can achieve outstanding results even without additional input information thanks to the hierarchical structure of the model.

The worse outcome for the extended input can be caused by the data character - fragmentation of categories within the 2D layer was not significant, and the model did not use this information. Instead, it was forced to process more input data. Also, perhaps a smaller size of the training set was not enough to learn the given input-output transformation. The results of the experiments are summarized in Table 2.

Table 2: Results of experiments on standard datasets.

<i>Data Set</i>	<i>Let</i>	<i>Sem</i>	<i>Occ 1</i>	<i>Occ 2</i>
Best reference result [%]	82.7	93,1	97.9	99,3
Best result with classic input [%]	42.0	94.7	99.6	99.9 *
Best result with extended input [%]	55.0 *	96.9 *	100.0 *	97.8
Training vectors	16000	1200	8143	8143
Testing vectors	4000	393	2665	8926
<i>Settings for best dataset result (*)</i>				
Input dimensions	16	256	7	7
Number of 2D cells	20 * 20	40 * 40	10 * 10	20 * 20
Classification criterion	strict	strict	strict	strict
Reduction factor	0.1	0.6	0.3	0.7
Real levels	8	7	4	10
Total learning iterations	2723	186	2887	2399

6 CONCLUSIONS

This paper introduces a modified learning algorithm for the Kohonen map, which enables solving of classification tasks with this network. The core of the modification is the use of an extended training set using the output categorization of the training patterns for the learning process. Modifications were made even in setting the criteria for completing model learning (criterion of minimal pattern shift in the 2D layer). A visual superstructure of the model was developed to allow a detailed study of the dynamics of the model setup process, and the obtained knowledge could be used to better understanding of the learning process and the nature of input data.

The second significant modification is the design and description of the behavior of a hierarchical classification model based on modified Kohonen maps. The training set is gradually reduced during the process of learning, increasing the sensitivity of the network to differences in input data. An algorithm for the production phase of the model was developed, based on the learned Kohonen map sub-models.

The model was described by a set of parameters, whose values had to be empirically determined. Therefore, genetic algorithms have been used to find optimal values.

Two groups of experiments were carried out with the modified model. Experiments on artificial dataset were focused on model in-depth behavior to verify the benefits of the proposed modifications. They confirmed the positive influence of the training set extended by the outputs and the hierarchical structure of the model for better performance of the classification model. The overall classification quality was improved by 6.58% on the generated data with nonlinear randomly selected transformation function $R^d > B^l$. The benefit of the hierarchical structure would probably be higher when using data unevenly covering the input space.

The experiments on standard datasets were used to obtain result comparable with other research and to show the practical usability of the model. Three datasets were used in four experiments. In three of them, the presented model exceeded the best classification quality mentioned in the references.

Although the described model gives better results with unprocessed data than literature references, there is still the space for improvement of its concept. We can find open questions in the definition and possible dynamic modification of the neighborhood of the winning cell, the type of distance calculation used in the 2D layer, or the criteria for completing the individual steps of the hierarchical learning process.

It will also be necessary to examine the impact of the input data structure on the results achieved.

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