

Automatic Offset Detection in GPS Time Series by Change Point Approach

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Abstract: This paper deals with the problem of automatic detection of offsets in GPS time series, which is of interest both in active volcanic and tectonic areas, where they often signal either the opening of eruptive fissures or seismic and aseismic dislocations. The problem is tackled by using the Change Point Detection (CPD) approach. Results show that CPD algorithms are suitable both in off-line and on-line frameworks. In particular, we show that CPD algorithms could contribute to the implementation of a warning system of volcanic intrusive activity.

1 INTRODUCTION

The Global Positioning System (GPS) has become an essential tool for ground deformation monitoring in areas subject to the risks of natural disasters, such as active volcanic and tectonic ones. Detection of potentially hazardous events (such as earthquakes and volcanic eruptions), as quickly as possible, can be useful for safeguarding human lives and infrastructures. However, data available in real time by GPS monitoring networks are not themselves enough for a reliable evaluation of the phenomena in progress, unless appropriate analysis tools be available too. One of the problems that prevent an effective use of GPS sub-daily solutions for real time applications, is that they are usually affected by a significant amount of noise. In particular, the shorter is processed period, the higher is the level of noise affecting the GPS solutions. Thus, the algorithms for detecting true displacement transients must be as robust as the sampling time is lower. Due to the large number of noise sources, often not well known, GPS noise is generically modeled as a mixture of white noise, flicker noise and random walk noise (Mao et al., 1999).

Offsets are one of the components of GPS time series, sometimes considered as a source of noise, which could contribute to degrade the accuracy of GPS time series. They can be due to the equipment

problems, such as antenna or receiver changes, but also to natural phenomena, such as post seismic effects of earthquakes and, in volcanic areas, to the opening of eruptive fissures. Offsets can have various sizes, from very small, which are very difficult to detect in presence of noise, to quite large, which, on the contrary, can be easily detected. In Gazeaux et al. (2013) results of a competition, launched to various research teams, with the purpose of assessing the effectiveness of methods to detect and remove offsets, are reported. In the competition, the data set, consisting of simulated GPS time series, was made available to the GPS analysis community without revealing the offsets, and several groups conducted blind tests with a range of detection approaches. The results of this experiment showed that manual methods, where offsets are hand-picked, almost always give better results than automated or semi-automated methods. However, while hand picked methods can be considered for off-line applications, they have no utility for monitoring purposes, where automatic approaches are mandatory.

This paper deals with the problem of automatic detection of offset both in daily and high rate (sub-daily) GPS time series, reporting a case study concerning offset detection in data recorded at the Mount Etna volcanic area. The task was tackled by using the Change Point Detection (CPD) approach, already widely described in literature. A recent survey of methods for CPD can be found in Aminikhanghahi and Cook (2017). This paper is organized as follows:

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in section 2 a general model of GPS time series is described, while in section 3 the mathematical background about change point detection algorithms is reported. In section 4 the off-line CPD approach was applied to detect offsets in daily GPS time series. In section 5, the results of a case study concerning on-line transient detection in sub-daily GPS time series at Mount Etna is reported. Finally, the conclusions are drawn in section 6.

2 A GENERAL MODEL OF GPS TIME SERIES

In order to describe more precisely what is referred to as offset in GPS time series, it can be useful to know that GPS time series can be modeled as described in equation (1).

$$x(t_i) = x_0 + bt_i + \sum_{j=1}^l a_j H(t_j - T_j) + \sum_{n=1}^m A_n \sin(\omega_n t + \varphi_n) + n_i(t_i) \quad (1)$$

where, for the epoch t_i :

- the first term x_0 is the site coordinate,
- the second term bt_i is the linear rate,
- the third term, consists by a sum of l Heaviside step functions $H(t_j - T_j)$, each having amplitude a_j .
- the fourth term consists of m periodic components, mainly the annual and semiannual signals, where $\omega_n = 2\frac{2\pi}{n} \text{rad/year}$
- the final term, $n_i(t_i)$, is the noise component of the GPS times series.

The first four terms of this model, which represent the deterministic part of the model, are easy to understand. In particular, the Heaviside step functions $a_j H(t_j - T_j)$ attempt to model what are referred in this paper as offsets. The noise term, which is the stochastic model term, is some time obscure, since it attempts to model the effects of several phenomena, such as propagation effects of GPS signals, multipath etc. Several papers have been devoted in literature to characterize the noise term, based on the approaches described in Mao et al. (1999) and Williams et al. (2004). These approaches, applied also recently (Birhanu et al., 2018), consist in characterizing the term $n_i(t_i)$ as a combination of white noise, flicker noise, with a spectral density proportional to $1/f$, and random walk noise, with a spectral density proportional to $1/f^2$, being f the frequency. However, since

this aspect is outside the scope of this paper, we do not enter into more details.

3 CHANGE POINT DETECTION

A change point represents a transition between different states in a process that generates the time series. Change point detection can be defined as the problem of choosing between two alternatives: no change occurred and the alternative hypothesis, a change occurred. CPD algorithms are traditionally classified as online or offline. Offline algorithms consider the whole data set at once and try to recognize where the change occurred. Thus, the objective, in this case is to identify all the sequence change points in batch mode. In contrast, online, or real-time, algorithms run concurrently with the process they are monitoring, processing each data point as it becomes available, with the goal of detecting a change point as soon as possible, after it occurs, ideally before the next data point arrives. In practice, no CPD algorithm operates in perfect real time because it must wait for new data before determining if a change point occurred. However, different online algorithms require different amounts of new data before a change point can be detected. Based on this observation an on-line algorithm which needs at least ϵ samples in the new batch of data to be able to find a change is usually denoted as ϵ -real time. Therefore, off-line algorithms can then be viewed as ∞ -real time while the best on-line algorithm is 1-real time, because for every data point, it can predict whether or not a change point occurs before the new data point. Smaller ϵ values may lead to stronger, more prompt change point detection algorithms.

To find a change point in a time series, a global optimization approach can be employed on the following basic algorithm:

1. Choose a point and divide the signal into two sections.
2. Compute an empirical estimate of the desired statistical property for each section.
3. At each point within a section, measures how much the property deviates from the empirical estimate and at the end, add the deviation for all points.
4. Add the deviations section-to-section to find the total residual error.
5. Vary the location of the division point until the total residual error attains a minimum.

As mentioned above, the search for a change point k can be formulated as an optimization problem where

the cost function $J(k)$ to minimize can be written, in the general case as

$$J(k) = \sum_{i=1}^{k-1} \Delta(x_i; \chi([x_1, \dots, x_{k-1}])) + \sum_{i=k}^N \Delta(x_i; \chi([x_k, \dots, x_N])) = \quad (2)$$

where $\{x_1, x_2, \dots, x_N\}$ is the time series, χ is the chosen statistic and Δ is the deviation measurement. In particular, when χ is the mean, the cost function assumes the following form:

$$J(k) = \sum_{i=1}^{k-1} (x_i - \langle x \rangle_1^{k-1})^2 + \sum_{i=k}^N (x_i - \langle x \rangle_k^N)^2 \quad (3)$$

where the symbol $\langle \cdot \rangle$ indicates the mean operator. Another aspect to be considered, when formulating the optimization problem, is that signals of practical interest have more than one change point. Furthermore, the number of change points K is often not known a priori. To handle these features, the cost function can be generalized as

$$J(K) = \sum_{r=0}^{K-1} \sum_{i=k_r}^{k_{r+1}-1} \Delta(x_i; \chi([x_{k_r}, \dots, x_{k_{r+1}-1}])) + \beta K \quad (4)$$

where k_0 and k_K are respectively the first and the last sample of the signal. In expression (4) the term βK is a penalty term, linearly increasing with the number of change points K , which avoid the problem of overfitting. Indeed, in extreme case (i.e. $\beta = 0$), $J(K)$ reaches the minimum value (i.e. 0) when every point becomes a change point (i.e. $K = N$). The CPD algorithm considered in this work was implemented in Matlab following the description given by Killick et al. (2012) and Lavielle (2015). Recent developments concerning algorithms for CPD can be found in Soh and Chandrasekaran (2017) and Celisse et al. (2018).

4 OFF-LINE DETECTION OF OFFSETS

To the purposes of this paper, both daily and 10-minute sampled GPS time series recorded by the GPS monitoring network (Figure 1) have been considered. As for the daily solutions, the used GPS time series were recorded from January 2011 to November 2018 by five stations, referred to as ECNE, ECPN, EINT, EPDN and EPLU (see the map in Figure 1), all located in the summit area of the volcano.

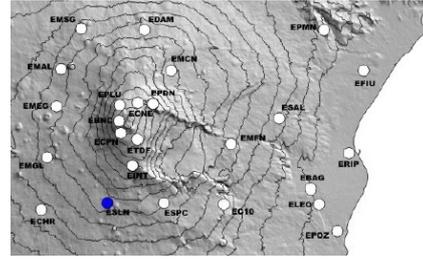


Figure 1: The GPS measuring network managed by INGV.

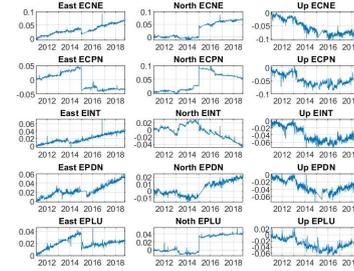


Figure 2: East, North and Up daily GPS components recorded at five stations.

As concerning 10-minute sampled data, they were recorded at 19 stations from August 2018 to December 2018.

The data set of daily GPS data, without any pre-processing, except filling missing data by linear interpolation, is shown in Figure 2. As it can be seen, offsets are evident in the East and North components, while periodic fluctuations, mainly due to mass loading, are particularly evident on the Up component, i.e. in direction of the gravity field Liu et al. (2017). Thus, it is a common practice to process separately the horizontal (i.e. the East and North) and the vertical components. Moreover, in order to just detect offsets in time series of displacements, it is suitable to reduce the data dimensionality by neglecting the displacement direction, thus composing the east and north components into the horizontal displacement strength. The CPD algorithms can operate both by fixing the maximum number of change points to be detected (K), or the maximum acceptable residual error (i.e. fixing a threshold on $J(K)$). The first choice is appropriate when operating off-line, since one can estimate the number of offsets, for instance by visual inspection of the time series. If this choice is performed, the indicated number of offsets will be detected and ordered by amplitude from larger to smallest. The choice of operating by threshold is instead more appropriate when an estimation of the number of offsets in the GPS time series cannot be easily performed. As an example, in order to detect only the most significant offset in the whole time interval, from January

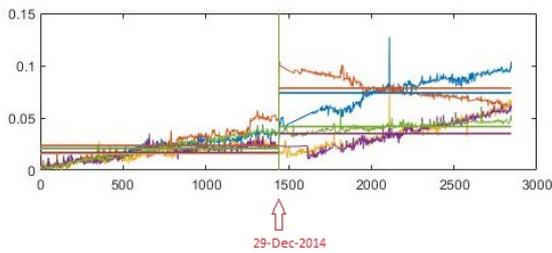


Figure 3: Off-line detection of the largest offset in the GPS displacement strength daily component.

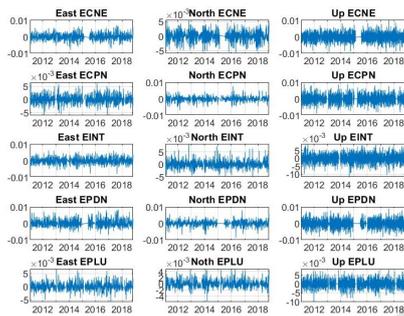


Figure 4: Residuals, after removing the linear trends.

2011 to November 2018, we can set to 1 the maximum number of change points, thus obtaining the result shown in Figure 3. It can be interesting to observe that the time stamp associated with this offset was 29-Dec-2014, which corresponds to the day after the starting of the eruptive event occurred at Mount Etna on 28-Dec-2014 Gambino et al. (2016). Therefore, the off-line CPD algorithm was able to detect the offset due to the eruption event.

Running the CPD algorithm with an appropriate maximum number of offsets, or specifying a maximum threshold on the cost function, can be very useful for off-line detrending of GPS time series. Indeed, after offsets are detected, the linear trends obtained interpolating samples between consecutive change points, can be removed, giving the results shown in Figure 4. Residuals from detrending can then be used to characterize the noise source for the study area by using strategies described in Mao et al. (1999), Williams et al. (2004), or Birhanu et al. (2018).

5 ON-LINE DETECTION OF OFFSETS

Daily GPS time series, considered in the previous section, are not appropriate to the purpose of implementing a warning systems based on offset detection, since 1 day is a quite long time for detecting very fast phe-

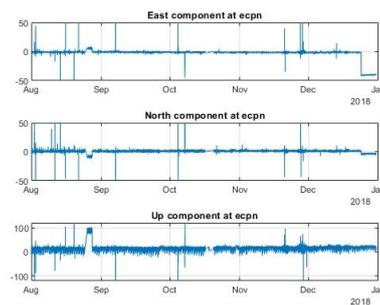


Figure 5: The East, North and Up GPS component measured at the ECPN stations.

nomena such as the opening of an eruptive fissure, which may onset in times of the order of a few tens of minutes. For this purpose, we used the time series coming from 10-minute kinematic GPS solutions to detect possible offsets. To this end, one of the main problems to deal with is the pervasive presence of outliers due to the quite poor geodetic quality of real time GPS positioning. As an example, we report in Figure 5 the GPS components measured at one of the summit stations referred to as ECPN. As it is possible to see, the time series are affected by a considerable number of outliers, whose value may exceed several times the variance of the signal. A strategy to deal with outliers is, obviously, to detect them and remove or replace. As for outlier detection purposes, several criteria have been proposed, as for instance to consider outliers the samples which exceed more than a multiple of standard deviation from the mean of the series. As concerning the replacement criteria, a variety of approaches there exists such as filling with a specified scalar value or with the center value or with the previous non-outlier value etc. For instance, the results of detecting and filling outliers, in a off-line framework, at the ECPN station by using the criterion of considering outliers the samples exceeding three standard deviations from the mean and filling them with the center values, gives the result shown in Figure 6. It is possible to see that the algorithm efficiently removes and fill the outliers that satisfy the mentioned criteria. Of course, for on-line offset detection, the filling outliers algorithm must be accordingly implemented. This means that a new sample will be added to a batch of data after processing it to see if it is an outlier.

To measure the performances of the on-line CPD algorithm, we considered the ϵ index (see section 3), i.e. the number of samples in the new batch of data required by the algorithm to detect an offset. Moreover, we have identified as target the offset mentioned above, occurred on 24-Dec-2018, which, based on information issued by the Istituto Nazionale di Geofisica e Vulcanologia AA.VV (2018), responsible for

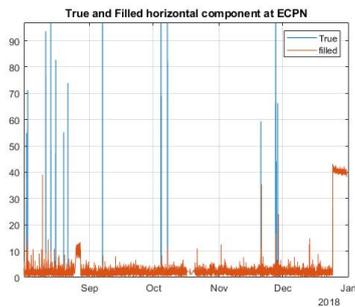


Figure 6: True and filled GPS displacement strength component at the ECPN station.

studying and monitoring Mount Etna, can be associated to an eruptive event. A description of such event is summarized as follows. Shortly after 11:00 (hereinafter all the times are expressed in GMT), an eruptive fissure opened up at the southeastern base of the New Southeast Crater, from which a violent Strombolian activity emerged, which rapidly formed a gaseous plume rich in dark ash. A second small eruptive fissure simultaneously opened slightly more to the north, between the New Southeast Crater and the Northeast Crater, which produced only a weak Strombolian activity, lasting a few tens of minutes. At the same time, also the Northeast Crater and the Bocca Nuova produced a continuous Strombolian activity of variable intensity. Overall, the ash cloud generated by the eruptive vents produced a very consistent dark ash plume, driven by the wind in the south-easter quadrant of the volcano. In the following two hours the eruptive fissure spread south-eastwards, exceeded the edge of the western wall of the Valle del Bove, until it reaches a minimum altitude of about 2400 meters above sea level. From this description it is possible to understand the complexity of the involved phenomena. The effects of this eruptive event on the GPS signal can be recognized in both the east and north components, mainly at seven of the nineteen recording stations, as shown in Figure 7. For the sake of simplicity, the east and north components were merged to obtain the displacement strength. The Figure shows that among the nineteen stations, the first and most intense offset is recorded by the ECPN station. Of the remaining stations, only six others record the ground breaking phenomenon in various ways, and in any case with some delay, compared to the ECPN station. It could be interesting to know that there are no appreciable evidences of the occurring of the eruptive event in the Up components (see Figure 7, at the bottom). Thus, if we want to make a hand-picking of the phenomenon, putting ourselves in the best conditions, we must consider the recording of the ECPN station. The data tips shown in Figure 8, allows to place the phenomenon as occurred starting at

10:59. For the purposes of this paper it was impor-

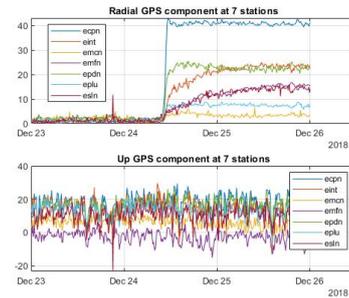


Figure 7: Horizontal displacement strength and up components at seven stations, immediately before and after the starting of the eruptive event occurred on December 24, 2018.

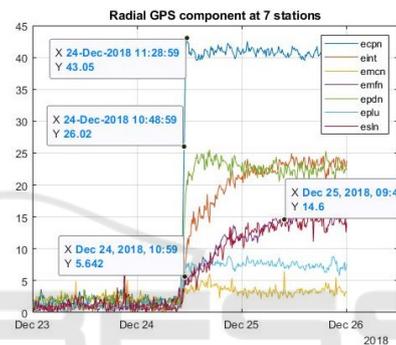


Figure 8: Horizontal displacement strengths at 7 stations, with data tips.

tant to evaluate the delay with which the online CPD algorithm indicated the offset, compared to the hand-picking we carried out. To this end, we set up the following procedure:

1. Consider the longest batch of data prior to the hand-picking, ending at the sample before the hand-picking date and verify that the CPD algorithm does not detect any offset.
2. Add to the batch of data one sample and test if the on-line CPD algorithm detects the event.
3. If the offset is found, the procedure stops and the number of samples supplied is assumed as the ϵ index values, otherwise go back to step 2.

For making the experiment, we have considered data recorded not only at the seven stations where the phenomenon is quite evident, but at all the nineteen available stations, since in general we must presume that we do not know what stations will provide useful information to detect an event. For warning purposes, it is important to recognize the incoming of the phenomena as soon as possible, but this capability depends on both the features of the CPD algorithm and the level of noise affecting the data. As a general rule

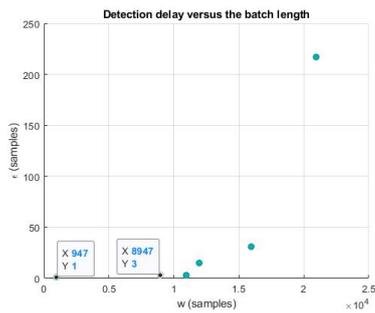


Figure 9: Detection delay versus the windows length.

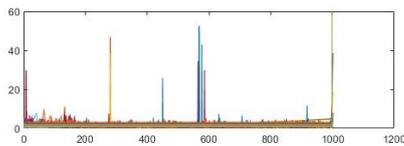


Figure 10: On-line detection by using a batch of data with $w = 1000$.

the length of the data batch should be a compromise between the sensitivity and specificity of the CPD algorithm, i.e. the need of having a prompt detection and that of avoiding false offsets. In order to determine the length w of the batch that provides the lowest delay value ϵ , we performed numerical simulations whose results are shown in Figure 9. From data tips it is possible to see that with a batch length w of about 1000 samples the detection delay is the shortest possible ($\epsilon = 1$), which becomes $\epsilon = 3$ with a batch of about 9000 samples. For larger w the delay increases almost exponentially. Thus we have considered $w = 1000$. Following this choice, the considered batch of data and the time of detection are shown in Figure 10. A detail of the CPD output is shown in Figure 11, where it is possible to appreciate the promptness of the CPD algorithm as the level of the recorded signal changes. Therefore, we can conclude that the on-line CPD algorithm detected the offset with no delay, compared with the hand-picking performed in the best conditions, i.e. by using data recorded by the station that detected the event as first.

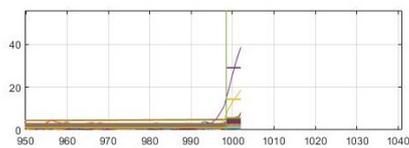


Figure 11: A detail of the CPD offset detection.

6 CONCLUSIONS

In this paper we proposed the use of CPD algorithms for automatic detection of offsets in GPS time series. These algorithms have been considered both in off-line and on-line frameworks. The off-line use of CPD algorithms allows an effective detection of offsets and therefore the removal of linear trends. This task is preliminary in order to analyze the features of the noise source in a given area. Furthermore, it is to bearing in mind that a manual detrending of GPS time series, is quite tedious and time consuming. Despite this undoubted advantage, the most interesting application of the CPD algorithms seems to be their use for on-line detection of offsets. Indeed, in this framework, they can significantly contribute to the implementation of a warning system for monitoring volcanic activity, in the wake of what was proposed by Cannavo et al. (2017) and Hajian et al. (2018). Indeed, experimental results, despite limited to an individual case study, show that on-line CPD algorithms are promising tools for monitoring the opening of eruptive fissures, in useful time to the onset of such a rather complex phenomenon.

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REFERENCES

AA.VV (2018). Etna weekly bulletin n. 52/2018. *Istituto Nazionale di Geofisica e Vulcanologia*, 52:1–11.

Aminikhanghahi, S. and Cook, D. J. (2017). A survey of methods for time series change point detection. *Knowledge Information Systems*, 51:339–367.

Birhanu, Y., Williams, S., Bendick, R., and Fisseh, S. (2018). Time dependence of noise characteristics in continuous gps observations from east africa. *Journal of African Earth Sciences*, 144.

Cannavo, F., Cannata, A., Cassisi, C., Grazia, G. D., Montalto, P., Prestifilippo, M., Privitera, E., Coltelli, M., and Gambino, S. (2017). A multivariate probabilistic graphical model for real-time volcano monitoring on mount etna. *J. Geophys. Res.Solid Earth*, 122:3480–3496.

Celisse, A., Marot, G., Pierre-Jean, M., and Rigaiil, G. (2018). New efficient algorithms for multiple change-point detection with reproducing kernels. *Computational Statistics and Data Analysis*, 128:200–220.

Gambino, S., Cannata, A., Cannavò, F., Spina, A. L., Palano, M., Sciotto, M., Spampinato, L., and Barberi,

- G. (2016). The unusual 28 december 2014 dike-fed paroxysm at mount etna: Timing and mechanism from a multidisciplinary perspective. *Journal of Geophysical Research: Solid Earth*, 121(3):2037–2053.
- Gazeaux, J., Williams, S., King, M., Bos, M., Dach, R., Deo, M., Moore, A. W., Ostini, L., Petrie, E., Roggero, M., Teferle, F., Norman, O., German, W., and Frank, H. (2013). Detecting offsets in gps time series - first results from the detection of offsets in gps experiment. *Journal of Geophysical Research Solid Earth*, 118:2397–2407.
- Hajian, A., Cannavo, F., Greco, F., and Nunnari, G. (2018). Classification of mount etna (italy) volcanic activity by machine learning approaches. *Annals of Geophysics*, 61.
- Killick, R., Fearnhead, P., and Eckley, I. (2012). Optimal detection of changepoints with linear computational cost. *Journal of the American Statistical Association*, 107:1590–1598.
- Lavielle, M. (2015). Using penalized contrasts for the change-point problem. *Signal Processing*, 85:1501–1510.
- Liu, B., Dai, W., and Liu, N. (2017). Extracting seasonal deformations of the nepal himalaya region from vertical gps position time series using independent component analysis. *Advances in Space Research*, 60:2910–2917.
- Mao, A., Harrison, C. A., and Dixon, T. (1999). Daily clearness index profiles cluster analysis for photovoltaic system. *Journal of Geophysical Research*, 104:2797–2816.
- Soh, Y. S. and Chandrasekaran, V. (2017). High-dimensional change-point estimation - combining filtering with convex optimization. *Applied and Computational Harmonic Analysis*, 43:122–147.
- Williams, S. P., Bock, Y., Fang, P., Jamason, P., Nikolaidis, R. M., Prawirodirdjo, L., Miller, M., and Johnson, D. J. (2004). Error analysis of continuous gps position time series. , *J. Geophys. Res.*, 109.