Forecasting Cost-Push Inflation with LASSO over Ridge Regression

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Keywords: Consumer Price Index, Cost-Push Inflation, Economy, Forecasting, Machine Learning, Novel Least Absolute Shrinkage and Selection Operator, Prediction, Ridge Regression.

Abstract: This study undertook an experimental analysis to forecast Cost-push Inflation using the Novel LASSO regression algorithm, contrasting it with the Ridge algorithm. Moreover, future Consumer Price Index (CPI) values were determined. To achieve maximum accuracy in predicting Cost-Push Inflation, the performance of the Novel LASSO algorithm (N=21) was evaluated against the Support vector regression algorithm (N=21). Sample sizes were determined utilising G-power, considering a pretest power of 0.80 and an alpha of 0.05. Notably, the mean accuracy value for the Novel LASSO algorithm stood at 81.95%, surpassing the Support vector regression algorithm's 75.57%. Statistical analysis highlighted a significant difference between the two methods (p=0.001, p<0.05), emphasising the superior accuracy of the Novel LASSO approach.

1 INTRODUCTION

The primary purpose of software is to obtain the desired output by pairing input with a chosen algorithm. In contrast, ML creates an algorithmic model by combining data and output (Choi et al. 2016). It's a computer science branch where computers are allowed to learn, rather than being explicitly programmed. Machine learning plays a role in our daily lives, for instance in detecting potential fraudulent activities, predicting traffic, and forecasting gambling outcomes (Devillers, Vidrascu, and Lamel 2005). Sudden inflationary shifts can impact a country's economy, thus controlling inflation is paramount to avoid upheaval. Annually, governments predict CPIs using various constraints to maintain stability. The Consumer Price Index (CPI) serves as a barometer for a country's inflation rate. Relying solely on annual CPI predictions might be problematic due to their potential influence on the global economy (Shapiro and Wilcox 1996). Therefore, leveraging historical data to forecast the future is essential to prevent significant disruptions. Inflation denotes the rate of price increase or decrease for products over time, crucial for assessing a country's cost of living-a primary consideration for migrants. Cost-push inflation, a result of increased raw material and wage costs, drives up product and service prices, impacting the economy. CPI measurements can capture these inflation types. This study focuses on Cost-push inflation since predicting

it could help avert significant disasters (Diewert and Erwin Diewert 2001). Resolving this issue entails inputting data into an algorithm to produce an output (Klutse, Sági, and Kiss 2022). In the domain of inflation prediction via supervised machine learning algorithms, various papers are accessible on platforms like Google Scholar, IEEE, Springerlink, and ScienceDirect. To be precise, 6000 articles on Google Scholar, 90 on Springerlink, 3500 on ScienceDirect, and 125 on IEEE. In the near future, supervised machine learning algorithms might be instrumental in predicting the Consumer Price Indices of different countries. A pivotal reference for this study explored numerous methods for accurately predicting inflation and poverty rates using machine learning models (Bryan and Cecchetti 1993). The challenge in this research was the multifactorial environment of inflation data prediction. This study achieved an impressive 93.75% accuracy. Another noteworthy article, cited 63 times, discusses forecasting inflation and unemployment using the Ridge regression algorithm (Sermpinis et al. 2014).

The current system for predicting Cost-push inflation employs machine learning algorithms like Ridge regression, linear, and Support vector regression algorithms. However, these have shortcomings. Due to frequently fluctuating data points, achieving accuracy is challenging. These three algorithms typically exhibit a larger margin of error compared to the Novel LASSO (Plakandaras et al. 2017). Algorithmic accuracy varies due to data point

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similarities. Notably, the Novel LASSO outperforms existing systems in terms of accuracy. The ultimate aim of this research is to refine CPI forecasts using the Novel LASSO regression.

2 MATERIALS AND METHODS

The solution-seeking analysis for this issue was conducted at the Machine Learning Lab, SSE, SIMATS. This lab is equipped with top-tier systems to facilitate the above study and ensure precise results. This review involved two collections, each with a sample size of 21. These figures were determined using a G-Power value of 80%, an alpha of 0.05, a beta of 0.2, and a 95% confidence interval (Kane, Phar, and BCPS).

The research utilised a dataset in CSV (Comma Separated Values) format, encompassing the consumer price index data of 270 countries over 64 years. This dataset was sourced from Kaggle (Rathore 2022). It details the CPIs of numerous countries for specific years, offering insights into their economic structures. Moreover, it's instrumental for forecasting the future CPIs of any given country.

For the analytical process, Google Colab was employed, a platform analogous to the Jupyter Notebook environment but with the distinction of operating entirely in the cloud. This online tool allows for the creation, implementation, and sharing of Python-based code, ideal for machine learning applications. Essential Python libraries, such as Numpy, Pandas, and Matplotlib, were utilised to implement machine learning methods and visualise inflation forecasts.

2.1 Novel Least Absolute Shrinkage and Selection Operator Algorithm

Novel LASSO employs the principle of shrinkage and falls under sample preparation group 1. In this context, shrinkage refers to the reduction of data points towards their average value. The method uses regularization to enhance the interpretation of the model (Kapetanios and Zikes 2018). Among the different regression algorithm models, the Novel LASSO stands out for its aptitude in subset variable selection, delivering forecasts with greater accuracy. It operates using the L1 regularization technique, which adds a penalty proportional to the absolute magnitude of coefficients (Campos, McMain, and Pedemonte 2022). Given that CPI values are continuous but distinct, the Novel LASSO regression is especially suited for inflation prediction. This approach draws potential error values towards a central reference, typically the mean. The formula for L-1 regression is depicted in Equation 1, while Table 1 provides a detailed breakdown of the Novel Least Absolute Shrinkage and Selection Operator algorithm's procedure.

L-1 Regression formula:

 $W = (RSS \text{ or Least Squares}) + \lambda * (Aggregate of absolute values of coefficients})$ (1) where,

- 1. RSS stands for Residual sum of squares
- 2. Lambda represents the aggregate of shrinkage in the Novel LASSO regression equation.

2.2 Ridge Regression Algorithm

In this context, the data values are continuous, lending an edge to the Ridge regression algorithm, which places it in sample preparation group 2. The Ridge regression algorithm is adept at addressing data points afflicted by multicollinearity, by fine-tuning the model. In contrast to the proposed regression algorithm, Ridge regression employs the L-2 regularization technique. The associated formula for this technique is as follows:

$$l^{2} = \operatorname{argmin}_{\boldsymbol{\beta}} \min \boldsymbol{\Sigma}_{i} (y_{i} - \boldsymbol{\beta}^{*} x_{i})^{2} + \boldsymbol{\lambda} \boldsymbol{\Sigma}_{k=1}^{k} \boldsymbol{\beta}_{k}^{2}$$
(2)

The tuning parameter, denoted as λ , governs the relative influence of the two terms in ridge regression. This approach is akin to linear regression, wherein a modest bias is incorporated to facilitate more sustainable long-term predictions. Ridge regression determines an outcome by identifying the optimal line or boundary. This boundary delineates the n-dimensional space into classes, allowing for the addition or determination of a data point based on historical data points (Pavlov and New Economic School 2020). The L-2 regularization's computational formula is represented by Equation 2. The steps for executing the Ridge regression algorithm are detailed in Table 2.

2.3 Statistical Analysis

The analysis for this investigation was conducted using IBM SPSS version 2.3. Within SPSS, a dataset comprising 21 sample sizes, each with Consumer Price Indexes (CPIs), was prepared for both the Novel LASSO and Ridge regression algorithms. The dataset covered attributes such as 270 countries spanning 64 years. Herein, the Consumer Price Index is the dependent variable, whilst the independent variables encompass factors like wage increases, taxation measures, demand-supply dynamics, economic margins, and governmental regulations.

3 RESULTS

Table 1 outlines the procedure for the Novel LASSO Algorithm. The process begins by initialising the standard libraries, followed by training the model using the dataset of Consumer Price Indexes.

Table 2 details the steps involved in the Ridge Regression Algorithm. Similar to the Novel LASSO, it commences with the initialisation of the standard libraries and then proceeds to train the model using the dataset of Consumer Price Indexes.

Table 3 offers a comparative analysis of the accuracy between raw data from both the Novel

LASSO regression algorithm and the Ridge Regression Algorithm.

Table 4 provides group statistical values for both algorithms. These statistics include the mean, standard deviation, and standard error mean. The dataset is further analysed using an independent sample T-test, with confidence set at 95%.

Table 5 showcases the results from the independent t-sample test for the two algorithms. The table furnishes details on the mean of loss, as well as a comparative accuracy analysis between the two algorithms. Both the T-test for equality of means and the Levene's test for equality of variance are presented. Importantly, the table highlights a statistically significant difference between the Novel LASSO algorithm and the Ridge Regression algorithm, as evidenced by a p-value of 0.001 (p<0.05).

Table 1: Proposed algorithm is the Novel LASSO regression algorithm procedure. Afterwards the Novel LASSO algorithm takes the subsets of the problem to get the unique solution in order to predict future Consumer Price Index of Cost-Push Inflation.

	Input: Consumer Price Index Dataset								
	Output: Accurate prediction of CPI's								
1.	Required packages are imported								
2.	Kaggle is used to download dataset.								
3. ma	First the rows and columns were preprocessed. After that, the missing variables were handled in order to ke it error free.								
Δ	Training of Novel LASSO model for getting the accuracy values.								
ч.									
 5.	Model has been tested with the dataset.								
ч. 5. 6.	Model has been tested with the dataset. Accuracy of Novel LASSO is calculated.								

Table 2: Represents the procedure of the Ridge Regression Algorithm. First initialization of the standard libraries is done and the model is trained with the dataset of Consumer price indexes. Testing and training are two sets of the models for the dataset and these are assigned to different functions to calculate the accuracy.

	Input: Consumer Price Index Dataset							
	Output: Accurate prediction of CPI's							
1.	Required packages are imported.							
2.	Kaggle is used to download dataset.							
3.	All the rows and columns were preprocessed after which missing variables were handled.							
4.	Training of Ridge regression model.							
5.	Model has been tested with the data set.							
6.	Accuracy of Ridge regression is calculated.							
7.	Estimation of accuracy from loss value.							

1 70 81 2 71 79 3 73 78 4 75 77 5 76 75 6 77 74 7 78 73 8 79 72 9 80 70 10 81 69 11 82 68 12 83 67 13 84 65 14 85 64 15 86 63 16 87 62 17 88 61 18 89 59 19 91 57 20 92 56 21 94 55	S.No	Novel LASSO Algorithm Accuracy (%)	Ridge Regression Accuracy (%)	
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16 87 62 10 17 88 61 18 89 59 19 91 57 20 92 56	14	85	64	
17 88 61 18 89 59 19 91 57 20 92 56	15	86	63	
18 89 59 19 91 57 20 92 56	16 A	87		ATIONS
19 91 57 20 92 56	17	88	61	
20 92 56	18	89	59	
	19	91	57	
21 94 55	20	92	56	
	21	94	55	

Table 3: Depicts the raw data table of accuracy between Novel LASSO regression algorithm and Ridge Regression Algorithm.

Table 4: Lists the group statistics values for the two algorithms along with the mean, standard deviation, and standard error mean. The dataset is subjected to an independent sample T-test with a 95% confidence level.

	Group	N	Mean	Std deviation	Std.Error Mean
A	Novel LASSO	21	81.95	6.895	1.505
Accuracy	RIDGE	21	67.86	7.914	1.727

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Table 5: Depicts an independent t-sample test for algorithms. Mean of loss and comparative accuracy analysis between the two algorithms are provided. T test for equality of means and Levene's test for equality of precision are provided. It shows that there is a statistical significance difference between the Novel LASSO algorithm and Ridge Regression algorithm with p=0.001 (p<0.05).

		Levene's test for equality of precision		T test for equality of means						
								95% confidence intervals of difference		
		F	Sig.	t	dt	Sig. (2- tailed)	Mean Difference	Std. Error difference	Lower	Upper
	Equal variances assumed	.634	.431	6.154	40	.001	14.095	2.291	9.466	18.725
Accuracy	Equal variances not assumed			6.154	39.264	.001	14.095	2.291	9.463	18.727

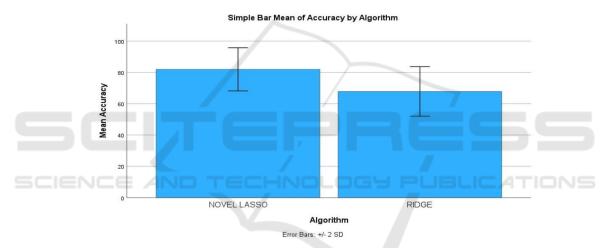


Figure 1: Comparison of Novel LASSO regression (81.95) and Ridge regression (67.86) with respect to mean accuracy. The accuracy value of the Novel LASSO algorithm is better than the Ridge regression algorithm and the standard deviation of LASSO is better than Ridge. X-axis: Novel LASSO vs Ridge regression algorithm. Y-axis: Mean accuracy of data +/- 2 SD.

Figure 1 visually compares the mean accuracy and mean loss of the Novel LASSO Algorithm and Ridge Regression Algorithm.

4 DISCUSSION

The results from the Sample T-Test analysis allow for an effortless determination of the significance value. With a significance value of 0.611, which is greater than 0.05, there is no significant difference between the groups for the selected dataset, as highlighted in Table 5. The accuracy of the Ridge regression stands at 67.86%, lower than that of the Novel LASSO regression, which is 81.95% (p > 0.05).

This paper's ultimate aim is to accurately forecast the Cost-push inflation rate from the provided dataset. By utilising the Consumer Price Index (CPI), predictions for a specific year are made by averaging data points to their mean (Stewart and Reed 2000). Future CPIs can also be calculated, considering both independent and dependent variables (Fixler 2009). A failure to address Cost-push inflation can result in severe economic repercussions (Huang and Mintz 1990). This could adversely affect countless individuals, especially in countries with a lower cost of living. A spike in the prices of daily essential raw materials, such as gold, steel, and petrol, can lead to public unrest (Seelig 1974), with demands for pay raises potentially resulting in company closures or layoffs.

According to a study by Pavlov in 2020 (Pavlov and New Economic School 2020), the accuracy rate for Ridge regression is approximately 74.956%. In contrast, the Novel LASSO delivers more accurate values with an accuracy rate of 81.95%. With a comprehensive database spanning 60 years and covering 268 countries with recorded CPIs, accurate prediction becomes more feasible. The proposed model boasts superior accuracy coupled with a lower processing rate, attributable to the use of extensive databases. For improved speed and accuracy, smaller databases are favoured (Ho 1982). Despite the wealth of data, many researchers have argued that various predictive models are not designed for accurately forecasting a country's CPI for a particular year. Ridge regression's drawbacks include its timeconsuming nature and its less intuitive user interface, especially when compared to the Novel Least Absolute Shrinkage and Selection Operator. This implies that implementing the Ridge regression algorithm is cumbersome, time-intensive, and generally inferior to the Novel LASSO regression algorithm. Looking forward, the Novel LASSO regression algorithm is poised to be the go-to tool for running ML models, aiming to forecast inflation rates and predict economic stability.

5 CONCLUSION

The intricate dynamics of inflation prediction, especially in the context of the Cost-push inflation rate, represent a vital area of study in economic research. The stakes are high: accurate prediction methodologies can inform policy decisions, streamline financial forecasting, and foster economic stability. Our exploration into this domain yielded several key observations that shaped the findings and contributed to our understanding of the topic.

- Database Depth: The expansive database spanning over 60 years and covering 268 countries provided a robust foundation for analysis. Such a comprehensive data set ensures that the algorithms can train and test on varied and representative data, enhancing the generalisability of the results.
- Impact of Raw Materials: The volatility in the prices of essential raw materials, such as gold and petrol, underscores the importance of accurate inflation prediction. These fluctuations have a ripple effect on the economy, affecting wage demands, consumer prices, and corporate profitability.

- Economic Implications: A misstep in predicting Cost-push inflation can lead to adverse economic repercussions. Failing to account for inflationary pressures can imperil economic health, affecting trade balances, purchasing power, and even leading to recessions.
- Algorithmic Advantages: The Novel LASSO algorithm's inherent design, which focuses on both feature selection and regularisation, lends it an edge over other algorithms. Its ability to reduce model complexity while retaining significant variables makes it particularly effective for complex economic predictions.
- Usability Concerns: Beyond mere accuracy, the ease of use and processing time of an algorithm play a significant role in its real-world application. As observed, Ridge regression, despite its merits, is more time-consuming and less user-friendly compared to Novel LASSO.
- Future Scope: The continual evolution of machine learning models hints at the possibility of even more refined and accurate prediction models in the future. Keeping abreast of these developments will be crucial for maintaining the edge in economic forecasting.

In light of the above points, the outcome of the present study of Cost-push inflation prediction is encouraging. With the Ridge regression algorithm delivering a mean accuracy of 67.86% and the Novel LASSO algorithm presenting a commendable mean accuracy of 81.95%, the latter clearly stands out. Hence, it is concluded that the Novel LASSO Algorithm exhibits superior accuracy when juxtaposed with the Ridge regression algorithm. This distinction, coupled with the aforementioned insights, paves the way for more informed decisions in economic modelling and forecasting.

REFERENCES

- Bryan, Michael F., and Stephen G. Cecchetti. 1993. "The Consumer Price Index as a Measure of Inflation." w4505. National Bureau of Economic Research. https://doi.org/10.3386/w4505.
- Campos, Chris, Michael McMain, and Mathieu Pedemonte. 2022. "Understanding Which Prices Affect Inflation Expectations." *Economic Commentary (Federal Reserve Bank of Cleveland)*. https://doi.org/10.26509/frbc-ec-202206.
- Choi, Sun, Young Jin Kim, Simon Briceno, and Dimitri Mavris. 2016. "Prediction of Weather-Induced Airline

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Delays Based on Machine Learning Algorithms." 2016 IEEE/AIAA 35th Digital Avionics Systems Conference (DASC). https://doi.org/10.1109/dasc.2016.7777956.

- Devillers, Laurence, Laurence Vidrascu, and Lori Lamel. 2005. "Challenges in Real-Life Emotion Annotation and Machine Learning Based Detection." Neural Networks: The Official Journal of the International Neural Network Society 18 (4): 407–22.
- Diewert, W. Erwin, and W. Erwin Diewert. 2001. "The Consumer Price Index and Index Number Purpose." *Journal of Economic and Social Measurement*. https://doi.org/10.3233/jem-2003-0183.
- Fixler, Dennis. 2009. "Incorporating Financial Services in A Consumer Price Index." Price Index Concepts and Measurement. https://doi.org/10.7208/chicago/9780226148571.003.0

007.

G. Ramkumar, R. Thandaiah Prabu, Ngangbam Phalguni Singh, U. Maheswaran, Experimental analysis of brain tumor detection system using Machine learning approach, Materials Today: Proceedings, 2021, ISSN 2214-7853,

https://doi.org/10.1016/j.matpr.2021.01.246.

- ho, Yan-Ki. 1982. "A Trivariate Stochastic Model For Examining The Cause Of Inflation In A Small Open Economy: Hong Kong." *The Developing Economies.* https://doi.org/10.1111/j.1746-1049.1982.tb00831.x.
- Huang, Chi, and Alex Mintz. 1990. "Ridge Regression Analysis of the Defence-growth Tradeoff in the United States." Defence Economics. https://doi.org/10.1080/10430719008404676.Kane, Sean P., Phar, and BCPS. n.d. "Sample Size Calculator." Accessed April 18, 2023. https://clincalc.com/stats/samplesize.aspx.
- Kapetanios, George, and Filip Zikes. 2018. "Time-Varying Lasso." *Economics Letters*. https://doi.org/10.1016/j.econlet.2018.04.029.
- Klutse, Senanu Kwasi, Judit Sági, and Gábor Dávid Kiss. 2022. "Exchange Rate Crisis among Inflation Targeting Countries in Sub-Saharan Africa." *Risks*. https://doi.org/10.3390/risks10050094.
- Kumar M, M., Sivakumar, V. L., Devi V, S., Nagabhooshanam, N., & Thanappan, S. (2022). Investigation on Durability Behavior of Fiber Reinforced Concrete with Steel Slag/Bacteria beneath Diverse Exposure Conditions. Advances in Materials Science and Engineering, 2022.
- Pavlov, Evgeny, and New Economic School. 2020. "Forecasting Inflation in Russia Using Neural Networks." *Russian Journal of Money and Finance*. https://doi.org/10.31477/rjmf.202001.57.
- Plakandaras, Vasilios, Periklis Gogas, Theophilos Papadimitriou, and Rangan Gupta. 2017. "The Informational Content of the Term Spread in Forecasting the US Inflation Rate: A Nonlinear Approach." Journal of Forecasting. https://doi.org/10.1002/for.2417.
- Rathore, Bhupesh Singh. 2022. "World Inflation Dataset 1960-2021."

https://www.kaggle.com/bhupeshsinghrathore/world-inflation-dataset-19602021.

- S. G and R. G, "Automated Breast Cancer Classification based on Modified Deep learning Convolutional Neural Network following Dual Segmentation," 2022 3rd International Conference on Electronics and Sustainable Communication Systems (ICESC), Coimbatore, India, 2022, pp. 1562-1569, doi: 10.1109/ICESC54411.2022.9885299.
- Seelig, Steven A. 1974. "Rising Interest Rates And Cost Push Inflation." *The Journal of Finance*. https://doi.org/10.1111/j.1540-6261.1974.tb03085.x.
- Charalampos Sermpinis, Georgios, Stasinakis, Konstantinos Theofilatos. Andreas and Karathanasopoulos. 2014. "Inflation and Unemployment Forecasting with Genetic Support Regression." Journal of Forecasting. Vector https://doi.org/10.1002/for.2296.
- Shapiro, Matthew, and David Wilcox. 1996. "Mismeasurement in the Consumer Price Index: An Evaluation." https://doi.org/10.3386/w5590.
- Stewart, Kenneth J., and Stephen B. Reed. 2000. "Data Update Consumer Price Index Research Series Using Current Methods (CPI-U-RS), 1978-1998." *Industrial Relations*. https://doi.org/10.1111/0019-8676.00158.