

# Forecasts and Analyzes of China's Birth Rate

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Abstract: As China's birth rate declines, the country faces increasingly serious social problems. Inspired by the era of big data, the study collected fertility data from 1949 to 2022 from China's National Bureau of Statistics. The number of samples is 74. Organize the data into a time series, and the autoregressions moving average (ARIMA) model was used to predict the trend of birth rate. In accordance with the Akaike Information Criterion (AIC) guidelines, the final best model is ARIMA (0,1,2). The prediction of this model showed that the number of birth rate from 2023 to 2027 would be a relatively stable trend with a slight increase probably. The study is also a summary of the strengths and weaknesses of the model. Hopefully, the model can be improved in the future and the application of time series method to predict the trend of birth rate can provide effective guidance for the formulation of childbirth policies.

## 1 INTRODUCTION

In 2021, for the first time since the founding of China, there was negative population growth. Birth rate only 8 per 1,000. According to the United Nations, India's birth rate in 2021 is 16.4 per 1,000, more than double China's; the United States' birth rate of 11.1 per 1,000 is also much higher than China's. China's birth rate has become the lowest among populous countries. However, the introduction of new policies has failed to reverse the decline in the birth rate. Birth rate lower in 2022 than in 2021. The lowest record was broken, once again. According to the survey results, the number of women of childbearing age in China has declined and fertility intentions are low. It has brought serious social pressure to China. For example: population aging, workforce shortage, social security pressure. China's birth rate is not optimistic, Projecting birth rate by mathematical modeling in China is meaningful. It is meaningful to utilize mathematical models for forecasting the birth rate in China. Many scholars have done research in this area.

Using 11 years of data from Beijing, Zhao and Sun developed a grey forecast model to predict age-specific fertility rates (Zhao and Sun 2015). In 2017, Li et al. predicted that China's population would grow negatively by 2025 (Wang 2017). However, the population is already showing negative growth, by 2021. This result points to a more rapid decline in the birth rate. In China, the change in fertility policy from

“one-child” to “two-child” in response to the birth rate problem has done little to raise the birth rate (Yage 2017). The idea that policy changes will not increase fertility in the short term is also supported by Wang's article (Wang 2018). Xue's study also concluded that China's fertility rate is difficult to increase (Xue 2018). Zheng et al (2019) looked at the impact of policies on fertility in highly educated groups. The conclusion was also that there was almost no effect. The three articles examine fertility intentions from the aggregate to the individual and conclude that the policy has not led to an increase in birth rate. Wang analyzed the time series using a Holt smoothing model and recovered the data from 2016 onwards (Wang 2020). Li used an Autoregressive Integrated Moving Average (ARIMA) - Back Propagation Neural Network (BP) model to predict provincial total fertility rates (Li 2021). Study on the prediction of the number of elderly people using the Grey Prediction Model GM (1,1) and the Support Vector Regression (SVR) Model (Wang et al 2023). The article used the Grey Prediction Model and the Leslie Matrix Population Simulation Prediction Model to predict the population of China (Chen 2016). The multiple linear regression model is used to select the most influential factors that can be used to predict the future trend of population ageing in China (Tao et al 2017). The article selected different models to process the data and compare the superiority of the models (Yan 2018).

Choosing the right model for different types of data can improve accuracy. Time series analysis is an analytical method that does not depend on explanatory variables. This paper uses the ARIMA model in time series analysis. Finally, the optimal model is selected to be used to predict birth rate trends.

## 2 METHODOLOGY

### 2.1 Data Source

The birth rate dataset used in this study were acquired from the National Bureau of Statistics of China. The original data saved in .xlsx format.

### 2.2 Dataset Introduction

The birth rate is the number of births per 1,000 of a country's population, averaged over the year. For example, China's birth rate in 2022 will be 6.77 per 1,000, meaning that the country will have an average of 6.77 births per 1,000 people in 2022. This study examines the yearly birth rate spanning from 1949 to 2022, with a total of 74 datasets at hand. Sequence diagram were plotted with these data in Figure 1. Plot the autocorrelation diagrams (Figure 2).

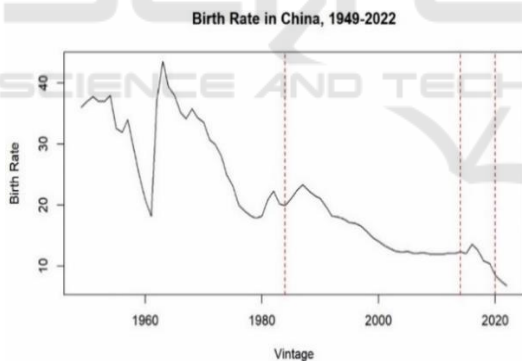


Figure 1: Birth Rate in China, 1949-2022 (Original).

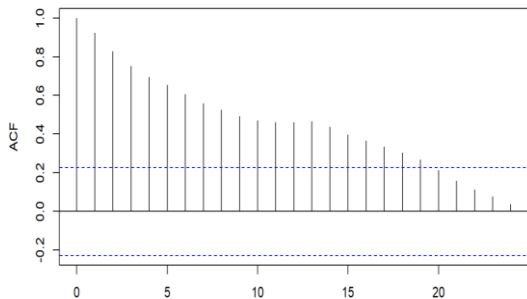


Figure 2: ACF of the Time Series (Original).

In Figure 1, The three vertical lines represent 1984 (the year when the family planning policy was introduced), 2014 (the year when the "two-child" policy was introduced), and 2020 (the year when the "three-child" policy was introduced). From 1949 to 1971, China's birth rate was almost above 30 per thousand. Since 1972, China's birth rate has been below 30 per thousand; since 1991, it has been below 20 per thousand; and since 2020, it has been below 10 per thousand. 1963 marked the apex of birth rates in China followed by a consistent decrease in the subsequent years. The decline has been particularly significant in the past few years. In count after count, birth rate has hit historic lows. The birth rate for 2022 is a mere 6.77. The time series depicted in Figure 1 and Figure 2 display non-stationarity.

### 2.3 Method Introduction

A time series is created when alterations in a variable are recorded in chronological sequence. Time series analysis involves the analysis of a series of observations, as well as forecasting future changes. The ARIMA model is commonly employed in the analysis of non-stationary time series.

The ARIMA (p, d, q) model is structured as follows:

$$\begin{cases} \Phi(B)\nabla^d x_t = \Theta(B)\varepsilon_t \\ E(\varepsilon_t) = 0, Var(\varepsilon_t) = \sigma_\varepsilon^2, E(\varepsilon_t \varepsilon_s) = 0, s \neq t \\ E(x_t \varepsilon_t) = 0, \forall s < t \end{cases} \quad (1)$$

$\nabla^d = (1 - B)^d$ ,  $\Phi(B) = 1 - \phi_1 B - \dots - \phi_p B^p$ , is the autoregressive coefficient polynomial of the model.  $\Theta(B) = 1 - \theta_1 B - \dots - \theta_q B^q$ , is the moving average polynomial of the model".

The modelling process for the time series is shown in Figure 3.

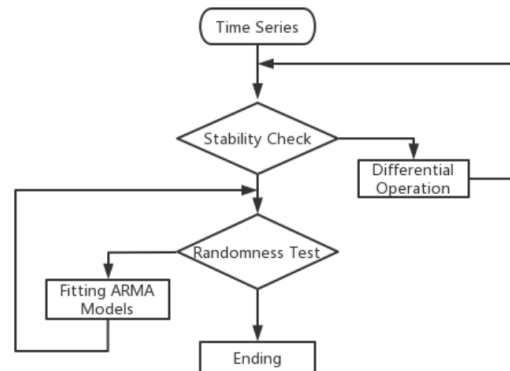


Figure 3: Modelling Procedure (Original).

### 3 RESULTS AND DISCUSSION

#### 3.1 Data Preprocessing

Of the 74 data used in this paper, there are no outliers and no missing values. Based on the timeliness of the time series, this paper uses the entire dataset for the modelling process.

#### 3.2 Stability Check

From Figure 1, the birth rate is on a downward trend. It does not fulfil the characteristic of a smooth time series with a mean value. The next step is to perform an Augmented Dickey Fuller (ADF) test on the series. The results showed p-value more than 0.05. Both results indicate that the time series is not stability. Therefore, this set of time series should be analyzed using the ARIMA model.

#### 3.3 Smooth Processing

The time series has a clear trend feature. Low-level difference processing can generally extract trend data to be used for smoothing the time series. Plot the timing diagrams (Figure 4), autocorrelation diagrams and partial autocorrelation diagrams (Figure 5) after first order differencing. The x-axis of Figure 5 shows the delay cycles, while the vertical axis represents the autocorrelation coefficient and the partial autocorrelation coefficient. The dotted line indicates the coefficient's two-fold standard deviation.

From Figure 4, The time series fluctuates above and below a certain value. It is consistent with the characteristic of a smooth time series having a mean value.

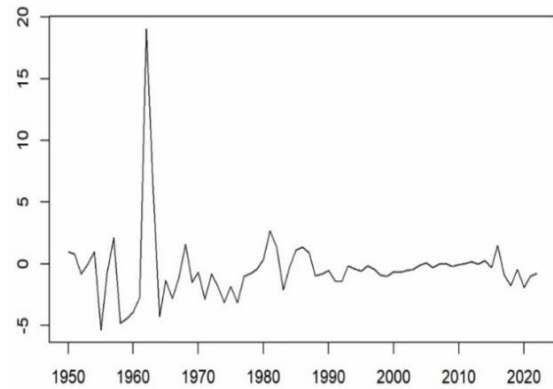


Figure 4: Timing Diagrams after First Differencing (Original).

Next, ADF test is performed on the time series. The results showed p-value less than 0.05. In summary, the time series after first order differencing tends to be stationary. The next step is the construction of an ARMA model for the smoothness time series.

#### 3.4 Randomness Test

To guarantee that the modelling is valid, the sequence must be examined for Ljung-Box. The p-value for the LB statistic is significantly below 0.05. So, the series is not a white noise series. This result indicates that the time series has modelling significance can be modelled.

#### 3.5 Determining Coefficients

From Figure 5, almost all of the ACF-value are within the dotted line. ACF chart displaying the features of truncated tails. The PACF-value fluctuate up and down frequently. It's a sign of a truncated tail. So, the

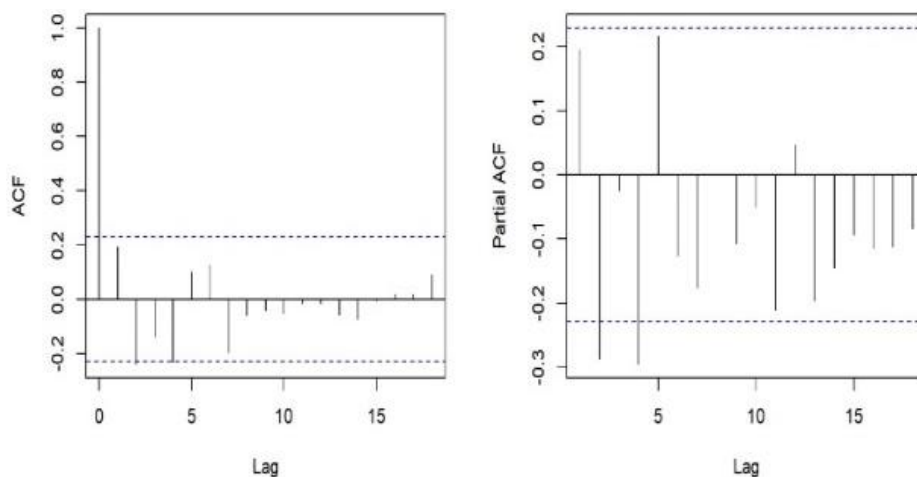


Figure 5: ACF and PACF of the Time Series (Original).

Table 1: AIC of Models.

	ar1	ma1	ma2	AIC
ARIMA (0,1,1)	-	0.4326	-	360.53
ARIMA (0,1,2)	-	0.2964	-0.2866	357.08
ARIMA (1,1,1)	-0.3698	0.737	-	358.56
ARIMA (1,1,2)	0.4224	-0.1034	0.4689	358.26
ARIMA (1,1,0)	0.2089	-	-	363.84

model ARIMA (0,1,1) is established, at first. Due to the high degree of randomness in the observations, this approach is not rigorous. Similar coefficients are therefore modelled for comparison. The study relies on the Akaike Information Criterion (AIC) guidelines to assist in the determination of coefficients. The results of these models are shown in Table 1. The ARIMA (0,1,2) model has the lowest AIC-value of 357.08. The optimal model ARIMA (0,1,2) was finally established. The two coefficients in the model are 0.2964 and -0.2688.

### 3.6 Model Evaluation

Testing for pure randomness on the residual series to determine whether the model has been complete in extracting the data. The results showed that the p-value of the LB statistic was greater than 0.05. The residual sequence is a white noise sequence. Models can be used to predict future trends.

### 3.7 Trend Forecasts

The model was used to predict the birth rate over the next five years. The projections are shown in Figure 6. The observed and predicted values are very similar. The predictions are almost always within the range of the confidence intervals. Projections for the next five years are almost stable at around 7 per 1,000. The projections show no upward trend.

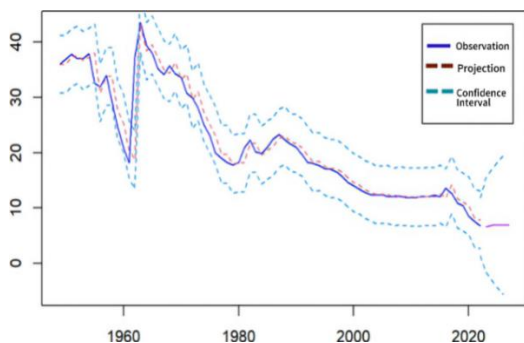


Figure 6: Prediction of the Brith Rate (Original).

The projections for the next five years are specified in the table 2. The table also demonstrates the 80% confidence intervals.

Table 2: Prediction of the Brith Rate from 2023 to 2027.

Vintage	Predictive Value	Upper Limit	Lower Limit
2023	6.61	10.04	3.19
2024	6.94	12.54	1.33
2025	6.94	13.53	0.35
2026	6.94	14.38	-0.51
2027	6.94	15.14	-1.27

Then a new time series is created. Next rebuild the ARIMA model use to forecast future trends. The optimal model is also the ARIMA (0,1,2). The two coefficients in the model are 0.2900 and -0.2933. Plotting new projections (Figure 7). The projections for the next five years are also almost stable. The projections also do not show an upward trend. The projections for 2021 and 2022 are significantly higher than the actual values. Predictions are greater than 8 per 1,000.

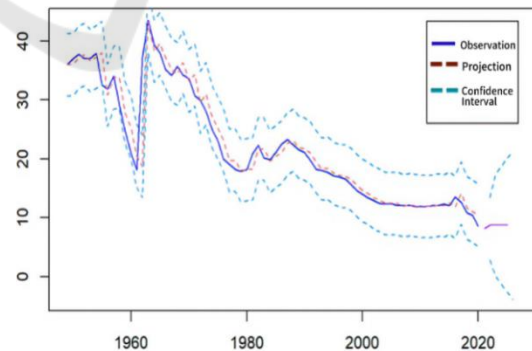


Figure 7: Another Prediction of the Brith Rate (Original).

Table 3 shows the projections for the next seven years in contrast to the above projections. The table also demonstrates the 80% confidence intervals. The difference between the two predictions is about two thousandths of a cent.

Table 3: Prediction of the Brith Rate from 2021 to 2027.

Vintage	Predictive Value	Upper Limit	Lower Limit
2021	8.15	11.62	4.68
2022	8.72	14.38	3.06
2023	8.72	15.35	2.09
2024	8.72	16.20	1.24
2025	8.72	16.96	0.48
2026	8.72	17.66	-0.21
2027	8.72	18.30	-0.86

Table 4 shows observed and projected values for 2021 and 2022. Predicted values are higher than observed values. The difference between the two predictions is about two thousandths of a cent.

Table 4: Prediction of the Brith Rate from 2021 to 2027.

Vintage	Predictive Value	Observed Value
2021	8.15	7.52
2022	8.72	6.77

#### 4 CONCLUSION

The study builds an ARIMA model on the time series created from 74 data points to predict trends in fertility, and screen for the optimal model using the AIC criterion. The ARIMA (0,1,2) model has the lowest AIC value of 357.08. The model is used to predict future fertility trends and it is found that the fertility rate does not show a short-term upward trend. Birth rates are all below 7 per 1,000 live births for the next five years. Re-modelling excluding the data points after the policy change results in a birth rate above 8 per 1,000 in 2021 and 2022. The projections for 2021 and 2022 are significantly higher than the actual values. This result suggests that policy changes have failed to raise the birth rate. The rate of fertility decline in China is accelerating. It also shows that China's social problems have not been solved.

Time series analysis is good at extracting seasonal and trend information. The analysis of external factors is not perfect. The reason for the decline in the birth rate may have been influenced by external factors, such as new crown pneumonia. For the impact of policy, this paper also fails to take into account in the form of variables. For these reasons, the accuracy of the model may be reduced. It is hoped that the study will inform policy development and allow for more accurate modelling in the future.

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