

Study on the Influencing Factors and Prediction of Air Quality in California Based on Multiple Linear Regression and Gaussian Process Regression Models

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Keywords: Air Quality, California, Multiple Linear Regression, Gaussian Process Regression.

Abstract: In current environmental science and public health research, air pollution is a key issue in the process of global industrialization and urbanization, and thus systematic studies on air quality are of great importance. This study is devoted to analyzing the historical air quality data in California from 1980 to 2022, using multiple linear regression and Gaussian process regression models to thoroughly investigate the impacts of major pollutants on air quality and their interactions, and to forecast air quality for the next three years. The research identifies an overall improving trend in air quality, particularly marked by a significant short-term enhancement during the COVID-19 pandemic due to reduced human activities. However, as economic activities resume, future air quality may face emerging challenges. Additionally, the significant influence of interactive effects among pollutants reveals the complexity of air quality management. The findings of this study provide robust data support and a theoretical basis for formulating scientific environmental policies and improving air quality, emphasizing the necessity for adaptive strategies and proactive monitoring to ensure sustainable air and environmental health.

1 INTRODUCTION

The examination and evaluation of air pollution throughout the United States have been rising in the field of environmental science as well as public health research. In global industrialization and urbanization, air quality problems are one of the main challenges that create a danger to the preservation balance within ecosystems and human life (Zhang et al. 2022). It is suggested that factors affecting air quality in California will be examined, as well as predicting their future trends.

The primary causes of air pollution are vehicle exhausts, industrial processes, and energy supply which comprise a gamut of particulate matter and gases (Laurent et al. 2016). According to research conducted, air pollution is closely related to rising diseases of the respiratory system and cardiovascular problems as well as death rates (Manisalidis et al. 2020). Hence, a comprehensive analysis of the quality of air in California is necessary for successful implementation and further development (Bigazzi & Rouleau 2017).

California stands out in terms of the frequency of air quality monitoring and the completeness of data. This selection is based on the degree of attention to air quality monitoring, aiming to deeply understand the dynamics of air quality in the U.S. from diverse perspectives. The substantial differences in population distribution, economic development levels, and geographic characteristics within California provide a multifaceted viewpoint for this research (Liu et al. 2021). For instance, California's high level of industrialization and dense population render it an important case study for environmental challenges in the urbanization process (Arfanuzzaman & Dahiya 2019).

The air quality data from 1980 to 2022 by a public data platform for this study used a quantitative analysis method. Firstly, statistical methods that are multiple linear regression unveil the main causes of air pollution (Lei et al. 2019), and Gaussian process regression is used for analysis to reveal how it will change in the future based on historical patterns (Rahman et al. 2015).

The importance of this study lies in developing a relevant research framework for environmental

science and acting as an important source of guidance to policymakers and public health officials. When using predictive modeling, this study presents a scientific foundation for developing environmental preservation and public wellness strategies. This study integrates these diverse and complicated drivers to gain a deeper insight into the dynamics of air quality, offering an empirical foundation for improving environmental management strategies as well as those associated with public health planning (Zhu et al. 2018, Yang & Wang 2017).

In conclusion, this study can have many theoretical as well as practical effects towards the building of better environments where air quality in California and worldwide is improved. It has a profound role in solving environmental problems and ensuring the health of an individual.

2 METHODOLOGY

2.1 Data Source and Description

The data used in this study is sourced from the Kaggle open data platform, involving Air Quality Index

(AQI) data for California from 1980 to 2022. These records are provided by the United States Environmental Protection Agency (EPA) and various state environmental monitoring agencies, encompassing detailed air quality readings from multiple monitoring stations. The dataset, recorded annually, includes records of key air pollutants such as Carbon Monoxide (CO), Nitrogen Dioxide (NO₂), Ozone, PM_{2.5}, and PM₁₀.

2.2 Indicator Selection and Description

In this study, the selection of indicators is divided into quantitative and qualitative data, as shown in Table 1. Quantitative data includes estimated population figures, annual sums of AQI median values, maximum values, total days exceeding standards, and related data for specific pollutants. These indicators directly reflect the status and trends of air quality. Qualitative data, on the other hand, includes the classification levels corresponding to air quality, which can more intuitively discern the air quality's relative standing.

Table 1: Indicator system and description.

Data type	Indicator name	Description of indicators
quantitative data	Pop_Est	Population Estimate
	Dys_w_AQI	Sum Number of Days with Air Quality Index
	Dys_Blw_Thr	Sum Number of Days where AQI was below or at the 'Moderate' threshold
	Dys_Abv_Thr	Sum Number of Days where AQI was above the 'Moderate' threshold
	Pc_Dys_Blw_Thr	Dys_Blw_Thr/ Dys_w_AQI represents the percentage of days with AQI <100
	Good Days	Sum Number of Good Days
	Moderate Days	Sum Number of Moderate Days
	Unhealthy for Sensitive Groups Days	Sum Number of Unhealthy for Sensitive Groups Days
	Unhealthy Days	Sum Number of Unhealthy Days
	Very Unhealthy Days	Sum Number of Very Unhealthy Days
	Hazardous Days	Sum Number of Hazardous Days
	Days CO	Sum Number of Days CO was main pollutant
	Days NO2	Sum Number of Days NO2 was main pollutant
	Days Ozone	Sum Number of Days Ozone was main pollutant
	Days PM2.5	Sum Number of Days Particulate Matter with diameter of 2.5 micrometers or smaller was main pollutant
Days PM10	Sum Number of Days Particulate Matter with a diameter of 10 micrometers or smaller was main pollutant	
qualitative data	AQI Color	The five categories of Green, Yellow, Orange, Red, Purple, and Maroon represent AQI values of 0 to 50, 51 to 100, 101 to 150, 151 to 200, 201 to 300, 301 and higher respectively.

Note: 'Days' represents the total sum of days for all reporting counties in a given year for the state of California.

2.3 Methodology Introduction

This study initially undertakes a visualization analysis of the data to gain an intuitive understanding, which facilitates subsequent investigation of the factors affecting air quality and the prediction of future trends. Subsequently, Multiple Linear Regression (MLR) analysis was employed to explore various factors impacting air quality, formalized as

$$y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \dots + \beta_nx_n + \varepsilon \quad (1)$$

where y represents the dependent variable, x_i denotes the i th independent variable, β_i is the corresponding coefficients, and ε signifies the error term, assumed to be normally distributed. In practice, coefficients are commonly estimated using the least squares fitting method,

$$\hat{\beta}_0, \hat{\beta}_1 \dots \hat{\beta}_n = \operatorname{argmin}_{\beta_0, \beta_1 \dots \beta_n} [(\sum_{i=1}^n y_i - \hat{y}_i)^2] \quad (2)$$

This phase of the study takes into account variables such as population and pollutants to identify and quantify their impact on air quality. Finally, the research employs Gaussian Process Regression (GPR) based on historical data to predict future trends of days with AQI below the 'moderate' threshold. GPR is a non-parametric Bayesian regression method, which assumes a prior distribution over the functions modeled as

$$f(X) \sim GP(m(X), k(X, X^T)) \quad (3)$$

where $m(X)$ is the mean function of the independent variables, and $k(X, X^T)$ is the covariance function, with the research adopting the Quadratic Rational Kernel, expressed as

$$k(X, X^T) = \left(1 + \frac{\|X - X^T\|^2}{2\alpha l^2}\right)^{-\alpha} \quad (4)$$

where the parameters α and l control the mixture of length-scales and smoothness of the function. Parameters are typically estimated using maximum likelihood methods. For a new prediction point x^* , GPR updates the posterior probability using Bayes' theorem $p(f(x^*)|X, Y, x^*)$, combining the observed data Y and prior distribution to determine the predictive distribution for x^* .

3 RESULTS AND DISCUSSION

3.1 Visualization Analysis

Prior to establishing relevant models, visualizing data

serves as a foundation for subsequent in-depth analyses, providing a scientific basis for further quantitative analysis and the formulation of effective air quality management strategies. Initially, box plots were drawn to depict the distribution of days across six air quality categories: good, moderate, unhealthy for sensitive groups, unhealthy, very unhealthy, and hazardous, as shown in Fig. 1.

From Figure 1, it can be observed that 'Good Days' and 'Moderate Days' are prevalent, indicating that in many years, the majority of days in California have good air quality, signifying clean air for residents most of the time. However, the occurrence of days categorized as unhealthy for sensitive groups, unhealthy, very unhealthy, and hazardous, although fewer, still indicates periods of deteriorating air quality that warrant attention.

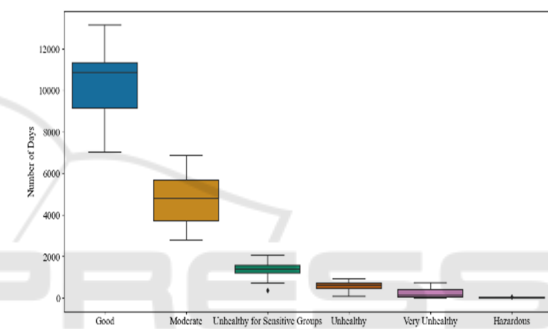


Figure 1: Distribution of Air Quality Category Days (Picture credit: Original).

To further explore the trends in air quality changes, related line plots were made, as shown in Figure 2. Pc_Dys_Blw_Thr represents the percentage of days with air quality below the moderate threshold, while Pc_Dys_Abv_Thr represents the percentage of days above the moderate threshold.

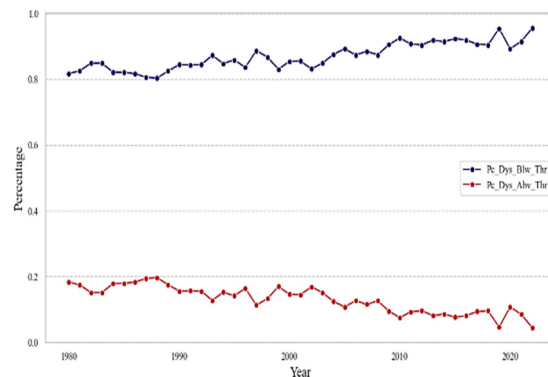


Figure 2: Trends in Air Quality Changes (Photo/Picture credit: Original).

From Figure 2, it is evident that over time, the percentage of days with air quality below the moderate threshold generally exhibits an upward trend, while the percentage of days above the threshold shows the opposite trend. This may reflect the combined impact of various factors such as environmental policies, urbanization, population growth, and climate change.

Finally, as illustrated in Figure 3, the matrix scatter plot displays the distribution of days for five major pollutants in California each year and the relationships between different pollutants.

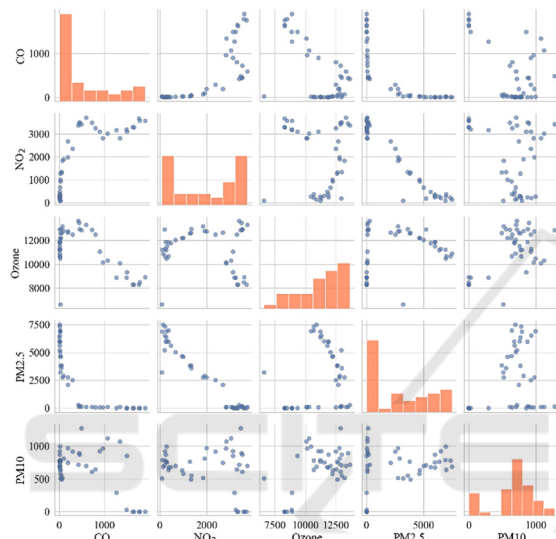


Figure 3: Matrix Scatter Plot of Major Pollutant Days (Photo/Picture credit: Original).

The diagonal histograms reveal certain pollutants, such as PM2.5 and PM10, have a broad range of distribution, indicating significant variability in the number of days they affect each year. The scatter plots indicate some linear correlations between the days of certain pollutants, suggesting that the interactive effects between these pollutants need to be considered in subsequent regression analyses.

3.2 Exploration of Influencing Factors

Based on the characteristics of the data, a preliminary correlation between various pollutants, estimated population, and Pc_Dys_Blw_Thr can be observed, along with certain interactions among different pollutants. Consequently, this study has decided to establish a multiple linear regression model to investigate the functional relationship between Pc_Dys_Blw_Thr and various pollutants as well as estimated population values. After several trials and to avoid the issue of heteroscedasticity, this study has

employed robust standard errors (Croux et al. 2004) during the regression process. The standardized regression results obtained through the STATA software are as follows:

$$y = -3.384x_1 + 0.121x_2 - 0.573x_3 - 0.392x_3x_4 - 0.302x_4x_5 \quad (5)$$

where y is the dependent variable Pc_Dys_Blw_Thr, x_1, x_2, x_3, x_4 and x_5 represent Days CO, Days Ozone, Days PM2.5, Days NO2, and Days PM10, respectively.

For the linear regression, the model achieved a Prob > F value of $0.000 < 0.05$, indicating that at a 95% confidence level, the model passes the joint significance test. The adjusted R-squared is 0.9072, demonstrating the model's reliability in explaining the variance in the dependent variable. The corresponding regression coefficient tests are presented in Table 2.

Table 2: Regression Coefficient Table.

	Beta Coef.	Robust Std. Err.	t	P > t
x_1	-3.384	0.000	-3.87	0.000***
x_2	0.121	0.000	0.80	0.015**
x_3	-0.573	0.000	-2.01	0.001***
x_3x_4	-0.392	0.000	-4.01	0.000***
x_4x_5	-0.302	0.000	-2.05	0.001***
cons	0.000	0.033	29.06	0.000***

Note: ***, ** and * represent significance levels of 1%, 5% and 10%, respectively

At a 95% confidence level, all regression coefficients and the constant term have p-values less than 0.05, indicating that the null hypothesis is rejected and the results have passed the significance test. This signifies that the regression coefficients are highly reliable. Building upon this, the study produced a regression residual plot and conducted a multicollinearity test using STATA software, respectively shown in Figure 4 and Table 3.

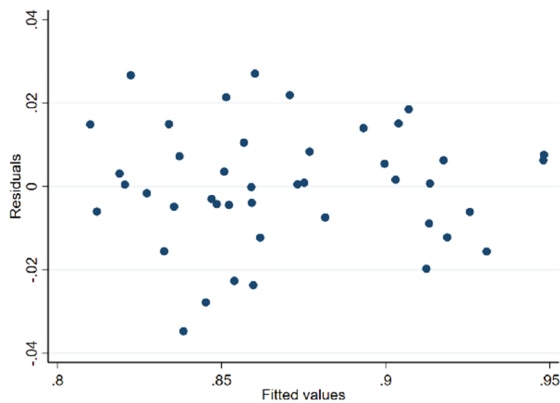


Figure 4: Regression Residual Plot (Picture credit: Original).

Table 3: Multicollinearity Test.

Variable	VIF
x_1	8.19
x_3	7.55
x_2	3.13
x_4x_5	3.10
x_3x_4	1.86

From Figure 4, it is observed that all residuals are evenly distributed between -0.04 and 0.04, indicating a minimal heteroscedastic effect in the model. Table 3 shows that the highest Variance Inflation Factor (VIF) is less than 10, suggesting that the regression equation does not suffer from severe multicollinearity issues.

In investigating the factors affecting air quality in California, standardized regression results revealed a significant negative correlation between the number of days of major pollutants like CO and PM2.5 and the percentage of days with air quality below the moderate threshold. Specifically, CO exhibited the most substantial negative impact on air quality, underscoring the importance of reducing emissions of these pollutants to improve air quality.

Regarding the positive correlation between ozone and air quality, although the impact is relatively small, it might reflect that under conditions of good air quality, favorable sunlight and temperature conditions are conducive to photochemical reactions in the air, which may increase the concentration of ground-level ozone, thereby affecting the ozone levels in the air to a certain extent (Yu et al. 2021).

The significance of interaction terms further emphasizes the impact of interactions between different pollutants on air quality. Notably, the negative coefficient for the interaction between PM2.5 and NO2 suggests that these pollutants may

partially offset each other's impact when present together, reducing their individual negative effects on air quality. This is consistent with the visualization of scatter plots where PM2.5 and NO2, as major pollutants, show negative correlations. As such, the air quality management strategies should account for cross-impacts of pollutants instead of controlling them individually. For instance, lower concentrations of PM2.5 or nitrogen dioxide could improve air quality in isolation; however, the consideration of interactions between pollutants even on high pollution days is more effective for preventing deterioration of the air quality.

3.3 Forecasts of Air Quality Trends

In the field of machine learning, the generalization ability of a model is particularly important when making predictions on data. To better measure the model's generalization ability and predictive performance, this experiment divides the dataset into a training set and a test set with an 8:2 ratio. The training set is used to train the established model, while the test set is used to evaluate the model's generalization ability. As the predictive variable (Pc_Dys_Blw_Thr) in this study is continuous, a quadratic rational Gaussian process regression model is adopted. Commonly used evaluation metrics in regression models include Root Mean Square Error (RMSE), Mean Absolute Error (MAE), Mean Squared Error (MSE), and Coefficient of Determination (R^2) (Tatachar 2021).

After multiple trials, the evaluation metrics for the test set of the trained model, Series Fitting Plot, and Residual Plot were obtained, respectively shown in TABLE 4, Figure 5, and Figure 6.

Table 4: Test Set Evaluation Metrics.

RMSE	MSE	MAE	R^2
0.0061	3.668e-04	0.0018	0.97

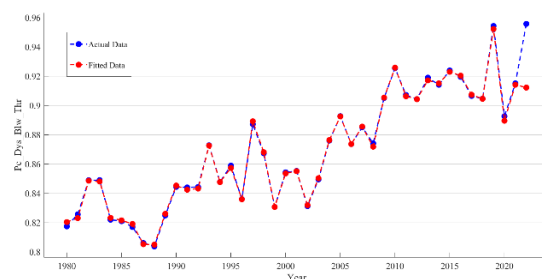


Figure 5: Series Fitting Plot (Picture credit: Original).

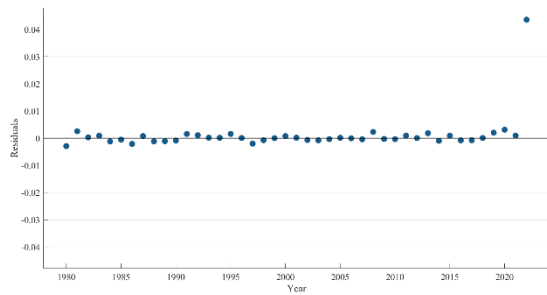


Figure 6: Residual Plot (Picture credit: Original).

The observations from the graphs and tables indicate that the test set error is quite small, and the coefficient of determination is high. Figure 5 shows good fitting, and the scatter distribution in the residual plot is relatively uniform, suggesting that the model has strong generalization ability and can be used to predict the future trend of Pc_Dys_Blw_Thr.

Utilizing the trained quadratic rational Gaussian process regression model, predictions for the percentage of days below the moderate threshold from 2023 to 2025 were made, and the results are presented in Figure 7.

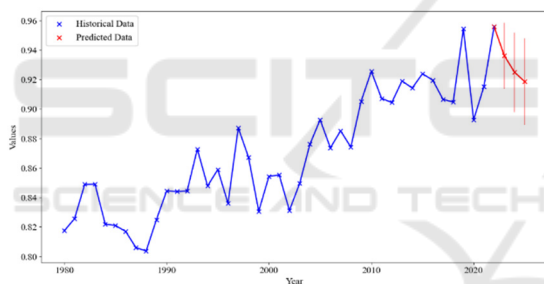


Figure 7: Three-Year Prediction Plot for Pc_Dys_Blw_Thr (Picture credit: Original).

Through the analysis of historical data from California from 1980 to 2022, the study has found that despite annual fluctuations, the overall level of air quality in California has been gradually improving over time. This improvement can be attributed to increasingly stringent environmental policies, technological advancements, and a heightened public awareness of the importance of clean air over the past few decades.

In particular, air quality is predicted to fall very rapidly during 2020–2022, which was one of the main results achieved by this research work. It was a time when the epidemic of COVID-19 spread all over the world, which resulted in unprecedented lockdown measures across borders and regions such as California (Johnson et al. 2021). The active measures about restrictions of traffic flows, industrial activity

suspension, and other SWMs had a direct influence on pollutant emission decrease that provided marked precipitous air quality improvement in the short run. Nevertheless, since the epidemic has gradually subsided and economic activities come back to life by 2023-2025 years as predicted in this model air quality index has lowered. This entails that a lack of constant control and amelioration measures may result in further human activities becoming instrumental in poor air quality performance.

Accordingly, while the occurrence of a pandemic may result in short-term improvements as regards air quality management and improvement California will need to continue focusing on such aspects. This entails implementing sustainable pollution control policies, increasing the adoption of renewable energy, and reducing emissions from environmentally unfriendly forms of transport as a measure to educate citizens on conserving nature. Second, controlling and evaluating the patterns as well as those that influence air quality are needed for developing policies and fine-tuning them to ensure timely delivery through appropriate measures. With these measures, air quality improvement becomes sustainable in ensuring good public health and maintaining a healthy environment.

In this holistic and proactive research approach, the changes in air quality in California can be fully understood and anticipated for a chance to stage scientifically effective policies on environmental measures as well as strategies for managing quality.

4 CONCLUSION

This research systematically assesses the air quality data in California from more than four decades of measurements and identifies the association between pollutant emissions, and interactive effects among various pollutants' impact on ambient air equality. By developing accurate data analysis and modelling, the research points out some short-term air quality improvements during COVID-19 while forecasting potential risks in post-recovery. These results underscore the importance of ongoing surveillance and necessary policy changes that are critical inputs for public health, as well as environmental stewardship. The results of the study also contribute to science by offering a scientific argument for strengthening air quality management techniques. California and worldwide, thereby promoting research-related areas. The research concludes that people should take more note of the eventual effects derived from an altered composition of pollution

sources, technological innovations preferences, and policy modifications caused by altering climate change on both air quality management systems as well as health measures. By developing new and innovative ideas, people can deal better with challenges regarding natural environments to protect average human health to assure the future of the Earth.

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