Research on the Influencing Factors of GDP in Anhui Province Based on Statistical Analysis

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Abstract: This article is based on the statistical data of Anhui Province from 2003 to 2022, aiming to explore the influencing factors of Anhui Province's GDP. The data comes from the Anhui Provincial Bureau of Statistics, and five impact indicators are selected: total import and export volume, number of colleges and universities, per capita consumption expenditure of urban residents, general budget revenue, and highway mileage. First, Pearson correlation analysis was performed on the data set and it was found that there is a strong correlation between different indicators. Then the factor analysis method was used to reduce the dimensionality of the above indicators, and two factors, social finance and social construction, were obtained. Finally, a binary linear regression model with standardized GDP as the dependent variable and the above two factors as independent variables was established through multiple linear regression analysis. These analyzes provide an important basis for an in-depth understanding of the influencing factors of Anhui Province's GDP, identify the main factors and put forward guiding suggestions, which will help relevant departments formulate targeted policies to promote economic growth in Anhui Province.

1 INTRODUCTION

Regional GDP refers to the final results of the production activities of all resident units in the region within a certain period of time. The GDP of a region is equal to the sum of the added value of various industries and is usually used to reflect the level of economic development of a region (Dynan and Sheiner 2018). The Anhui Provincial National Economic and Social Development Statistical Bulletin in 2022 stated that the province's gross product (GDP) for the whole year was 4.5045 billion yuan, an increase of 3.5% over the previous year (Wang et al 2023). Anhui's economy has achieved a historic transformation from "being in the middle in terms of total volume but lagging behind in per capita" to "being in the forefront in terms of total volume and being in the middle on per capita", and its economic strength has achieved a major leap (Wang and Shi 2021). However, compared with other economically developed provinces and cities in the "Yangtze River Delta" region, there is still a large gap (Ren and Zhou 2022). Additionally, Anhui Province's digital economy has developed rapidly in recent years, but there is still the problem of unbalanced development between the north and the south (Luo

2019). In order to implement comprehensive highquality development and build a modern and beautiful Anhui, Anhui's economy must maintain a stable and positive development trend. Therefore, it is of great significance to explore the influencing factors of GDP in Anhui Province, and to adopt and implement relevant effective economic measures to promote the economic development of Anhui Province.

There is no shortage of statistical research on the factors influencing Anhui Province's economic vitality in China. For example, by establishing a stepwise regression model, Ren and Zhou proposed that per capita consumption expenditure and technology contract turnover have a greater impact on Anhui Province's GDP (Wang et al 2021). In addition, Jingyu Luo established a factor analysis model on the comprehensive urban strength of 16 cities in Anhui Province and concluded that social welfare investment and sustainable development capabilities affect economic development to a certain extent (Wang and Cai 2022). Wang et al. established evaluation indicators through emergy models and obtained that the slow improvement of ecological civilization caused by the large proportion of the secondary industry is a major obstacle to Anhui's economic development. Thus, there is an urgent need

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variable name	impact indicators (unit)
ν	GDP of Anhui Province (100 million yuan)
x_1	total import and export volume (100 million U.S. dollars)
x_2	number of colleges and universities
x_3	per capita consumption expenditure of urban residents (yuan)
x_4	general budget revenue (100 million yuan)
x_{5}	highway mileage (thousand kilometers)

Table 1: Variable names.

to optimize the industrial structure and develop a circular economy (Trani and Holsworth 2010). Moreover, Wang and Cai also acquired good results by establishing the entropy weight TOPSIS model. They concluded that the main factors affecting regional economic vitality are the four categories of economic efficiency, science and technology and education, opening up to the outside world, and the living standard of residents. Among them, the two aspects of science and technology, education investment and opening up have greater weight (Zhang et al 2020). Based on the existing research results, this article selects five indicators: total import and export volume, number of colleges and universities, per capita consumption expenditure of urban residents, general budget revenue, and highway mileage to explore the statistical data of relevant indicators from 2003 to 2022. This article innovatively selects the number of colleges and universities and highway mileage as some of the impact indicators. As the development of higher education and highway construction can greatly affect the local economy (Cheng 2023). It is planned to conduct a series of statistical analyzes based on the inherent relationship between the data.

2 METHODOLOGY

2.1 Data Source

The data used in this article all come from the Anhui Statistical Yearbook published by the Anhui Provincial Bureau of Statistics over the years. The data on the five impact indicators released by it from 2003 to 2022 were integrated to obtain the data set used in the study.

2.2 Data Preprocessing

This article takes Anhui Province's GDP as the explained variable and the five selected impact indicators as explanatory variables. Since the selected unit of the original highway mileage data is 10,000

kilometers, all data are decimals. Now it is expanded ten times and the unit of 1,000 kilometers is selected to ensure the readability and beauty of the data. The variables are named as shown in Table 1 below.

2.3 Descriptive Statistical Analysis

First, SPSS was used to conduct descriptive statistical analysis on the data, and the following Table 2 was obtained. It can be seen from Table 2: (1) The skewness of general budget revenue is close to 0, and it is basically symmetrically distributed; the skewness of GDP and total import and export volume are both large positive values, and they are right-skewed data. Except for the total import and export volume, the kurtosis of the rest of the data is negative, indicating that the data is more distributed in parts farther from the mean. (2) For the number of colleges and universities and highway mileage, the standard deviation and coefficient of variation of these two data are small, indicating that the growth of these two data is relatively gentle; the coefficient of variation and standard deviation of other data are large, indicating that the data distribution is highly discrete.

The above data can illustrate that Anhui Province's economy has been developing steadily and for the better in the past 20 years, and residents' quality of life has improved.

In view of the obvious differences between the various indicators used in this article and the measurement units of GDP, direct statistical analysis will be inconsistent with the actual situation, making the conclusion erroneous. Therefore, before subsequent analysis, the data were first standardized by Z-score. Record the standardized GDP as y^* , and the five standardized impact indicators are $x_1^*, x_2^*, x_3^*, x_4^*, x_5^*.$

In the following, correlation analysis, factor analysis and multiple linear regression analysis will be carried out in sequence according to the internal relationship of the data.

variable name	maximum value	minimum value	mean	standard deviation	median	kurtosis	skewness	coefficient of variation (CV)
y	45045.02	4307.8	20863.02	13255.162	19462.85	-1.097	0.417	0.635
x_1	1131.27	59.43	426.152	314.033	418.295	0.259	0.897	0.737
x_2	121	73	107.7	16.442	117.5	-0.408	-1.104	0.153
x_3	26832	5064.34	15185.98	7037.696	15559.365	-1.225	0.149	0.463
x_4	3589.1	220.75	1828.154	1192.308	1933.895	-1.575	0.009	0.652
x_{5}	5.5	1.1	3.405	1.39	3.35	-1.249	-0.193	0.408

Table 2: Descriptive statistics.

3 RESULTS AND DISCUSSION

3.1 Correlation Analysis

Since the data taken are all continuous numerical data, the Pearson correlation coefficient can be used for correlation analysis. Pearson correlation analysis is a statistical method used to measure the strength and direction of a linear relationship between two variables. This method is based on the concept of covariance, which measures whether the changing trends of two variables are consistent. To facilitate the use of notation, let $y^* = x_0^*$.

And let $(x_i^*, x_j^*)(i, j = 0, 1, 2, \dots, 5, i \neq j)$ be a two-dimensional population. Obtain observation data from it: $(x_{i,1}^*, x_{j,1}^*)$, $(x_{i,2}^*, x_{j,2}^*)$, \cdots , $(x_{i,20}^*, x_{j,20}^*)$ $(n =$ 20). Denote,

$$
\bar{x}^{(i)} = \frac{1}{n} \sum_{k=1}^{n} x_{i,k}^*, \ \bar{x}^{(j)} = \frac{1}{n} \sum_{k=1}^{n} x_{j,k}^* \tag{1}
$$

Correlation Coefficient is usually represented by r , and its calculation formula is:

$$
r_{x_i^* x_j^*} = \frac{s_{x_i^* x_j^*}}{\sqrt{s_{x_i^* x_i^*} s_{x_j^* x_j^*}}} \tag{2}
$$

In formula (2),

$$
S_{x_i^* x_j^*} = \frac{1}{n-1} \sum_{k=1}^n \left(x_{i,k}^* - \bar{x}^{(i)} \right) \left(x_{j,k}^* - \bar{x}^{(j)} \right) \tag{3}
$$

$$
S_{x_i^* x_i^*} = \frac{1}{n-1} \sum_{k=1}^n (x_{i,k}^* - \bar{x}^{(i)})^2, S_{x_j^* x_j^*} = \frac{1}{n-1} \sum_{k=1}^n (x_{j,k}^* - \bar{x}^{(j)})^2
$$
\n(4)

They represent the covariance of x_i^* , x_j^* and the variance of x_i^* , x_j^* respectively.

It is generally believed that when the absolute value of the Pearson correlation coefficient is greater than 0.5, it is considered that there is a strong linear relationship between the two variables; when the absolute value of the Pearson correlation coefficient is between 0.3 and 0.5, it is considered that there is a moderate degree of linear relationship between the two variables. linear relationship; when the absolute value of the Pearson correlation coefficient is less than 0.3, it is considered that the linear relationship between the two variables is weak and there is no linear relationship.

Perform hypothesis testing on correlation, assuming the null hypothesis is $H_0: \rho_{x_i^*x_j^*} = 0$, and the alternative hypothesis is $H_1: \rho_{x_i^*x_j^*} \neq 0$. When (X_i, X_j) is a two-dimensional normal population, and H_0 is true, the statistic $t = \frac{r_{x_i^*x_j^*} \sqrt{n-2}}{\sqrt{n-2}}$ $\frac{x_i x_j}{\sqrt{1 - r_{x_i^* x_j^*}^2}} \sim t(n-2)$.

Assuming that the t value obtained from actual observation data is t_0 , then $p = P_{H_0}(|t| \ge t_0)$. At the significance level $\alpha = 0.05$, H_0 is rejected when $p <$ α . And it is considered that x_i^* , x_j^* are related and the calculated correlation coefficient reflects the strength of the linear correlation between the two variables.

The correlation coefficients between pairs of y^* , x_1^* , x_2^* , x_3^* , x_4^* , x_5^* are obtained by solving. The obtained correlation coefficient matrix is shown in Table 3 below.

It can be seen from the correlation coefficient matrix in Table 3 that the ν values of the correlation coefficient test between each variable are all less than the significance level $\alpha = 0.05$. Therefore, the null hypothesis is rejected. Therefore, it can be supposed that there is a correlation between variables, and the calculated correlation coefficient reflects the strength of the linear correlation between the two variables.

Table 3: Correlation coefficient matrix.

	v^*	x_1^*	x_2^*	x_3^*	x^*_4	x_{5}^{*}
ν^*		$0.974**$	$0.808**$	$0.992**$	$0.985**$	$0.967**$
x_1^*			$0.754**$	$0.959**$	$0.939**$	$0.914**$
x_2^*				$0.86**$	$0.868**$	$0.905**$
x_3^*					$0.993**$	$0.984**$
x_4^*						$0.985**$
x_5^*						

Note: ** indicates significant correlation at the 0.05 level

Noting that the values of the correlation coefficients are all greater than 0.5, it can be considered that there is a strong positive linear relationship between the variables. This shows that there is strong collinearity among the five different impact indicators selected in this article. In order to further select factors that influence GDP with greater weight, the five influencing indicators need to be dimensionally reduced to eliminate strong collinearity and make the final conclusion accurate and effective. The purpose is achieved through factor analysis below.

3.2 Factor Analysis

Since the number of selected impact indicators is small, it is determined that the number of public factors to be selected in the factor analysis of this article is 2, recorded as F_1, F_2 . That is, the five impact

indicators $x_1^* \sim x_5^*$ are dimensionally reduced into two public factors F_1, F_2 through factor analysis to facilitate subsequent multiple linear regression analysis.

The orthogonal factor analysis model based on this study is,

$$
\begin{cases}\n x_1^* = a_{11}F_1 + a_{12}F_2 + \varepsilon_1 \\
 x_2^* = a_{21}F_1 + a_{22}F_2 + \varepsilon_2 \\
 & \vdots \\
 x_5^* = a_{51}F_1 + a_{52}F_2 + \varepsilon_5 \\
 & \text{Expressed in matrix as: } \begin{bmatrix} x_1^* \\ x_2^* \\ \vdots \\ x_5^* \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ \vdots & \vdots \\ a_{51} & a_{52} \end{bmatrix} \begin{bmatrix} F_1 \\ F_2 \end{bmatrix} + \varepsilon_1\n\end{cases}
$$

 $\mathsf I$ ε_2 ⋮ ε_5 , abbreviated as $x_{5\times1}$ ^{*} = $A_{5\times2}F_{2\times1}$ + $\varepsilon_{5\times1}$. In

addition, equation (2) should also satisfy: ① $Cov(F, \varepsilon) = 0$, that is, F and ε are uncorrelated; ② F_1 , F_2 are uncorrelated and both have variances of 1; $\textcircled{3}\varepsilon_1, \varepsilon_2, \ldots, \varepsilon_5$ are uncorrelated and have different variances. The corresponding steps and results of factor analysis are as follows:

Applicability test: The test results are shown in Table 4 below.

From Table 4, it can be seen that the KMO value is 0.83 greater than 0.6, and the Bartlett sphericity test shows that the p value is equal to 0.000 and less than 0.05, which is significant. Therefore, this problem can be considered suitable for factor analysis.

Table 4: Applicability test results.

Factor extraction: The variance explanation table obtained from data processing is shown in Table 5 above.

It can be observed from Table 5 that the cumulative contribution rate of the first two components reaches 98.695%, which is higher than 95%, and the contribution rate of the last three components can be approximately ignored. Therefore, it is feasible to select two public factors.

Factor rotation and naming: Further process the data to obtain the rotated factor loading coefficient table, as shown in Table 6 below.

Table 6: Rotated component matrix.

Note that in Table 6, the public factor F_1 in the rotated component matrix has large loadings on the three indicators x_1 (total import and export volume), x_3 (per capita consumption expenditure of urban residents), and x_4 (general budget revenue). It reflects relevant information at the macroeconomic and trade levels, so F_1 can be named the social financial factor. The other public factor F_2 has large loadings on the two indicators x_2 (number of colleges and universities) and $x₅$ (highway mileage), which reflects relevant information at the level of social infrastructure construction, so F_2 can be named the social construction factor.

Factor score calculation: The calculated component score coefficient matrix is shown in Table 7 below:

From Table 7, the linear combination expression of the two public factors regarding each indicator is obtained, namely:

$$
\begin{cases}\nF_1 = 0.847x_1^* - 0.852x_2^* + 0.382x_3^* + 0.294x_4^* + 0.068x_5^* \\
F_2 = -0.7x_1^* + 1.325x_2^* - 0.126x_3^* - 0.021x_4^* + 0.25x_5^*\n\end{cases}
$$
\n(6)

3.3 Multiple Linear Regression Analysis

In order to avoid severe collinearity affecting the analysis results, the social financial factor F_1 and social construction factor F_2 after factor analysis dimensionality reduction are selected as independent variables, and the standardized GDP data y^* is used as the dependent variable to conduct multiple linear regression analysis.

Through the above analysis, it can be roughly concluded that F_1, F_2 and y^* have a strong linear relationship. Under this premise, a multiple linear regression model can be established:

$$
y^* = \beta_0 + \beta_1 F_1 + \beta_2 F_2 + \varepsilon, \ \varepsilon \sim N(0, \sigma^2) \quad (7)
$$

In equation (3), β_i ($i = 1,2$) represents the regression coefficient, and β_0 represents the intercept. Then use the least squares method to estimate β_i ($i = 1,2$), β_0 . Find the optimal function by minimizing the sum of squared errors. Solve the approximate solution $\hat{\beta}$ of the coefficient matrix $\beta =$

$$
(\beta_0, \beta_1, \beta_2)^T
$$
 through matrix operations $\hat{\beta}$ =
\n $(F^T F)^{-1} F^T Y^*$ where $Y^* = \begin{bmatrix} y_1^* \\ y_2^* \\ \vdots \\ y_{20}^* \end{bmatrix}$, $F =$

 \vert 1 f_{11} f_{12} f_{21} ⋮ 1 ⋮ $J_{20,1}$ f_{22} $J_{20,2}$ The results of the multiple linear

regression analysis are shown in Table 8 below:

Table 8: Regression coefficient.

	Beta		Significance
(constant)		0.000	1.000
F,	0.871	45.455	0.000
F,	0.485	25.324	0.000

It can be concluded from Table 8 that the approximate solution $\hat{\beta} = (0.0.871, 0.485)^T$ of the coefficient matrix. Subsequent model testing will be performed on this model to ensure that the model is successfully established. $H_0: \beta_0 = \beta_1 = \beta_2 = 0, H_1:$ There is at least one $\beta_i \neq 0$. Under the condition of H_0 , construct the test statistic $F = \frac{MS_R}{MS_E} =$ $S_R/(3-1)$ $\frac{S_{R/(3-1)}}{S_{E/(20-3)}} \sim F(3-1,20-3)$. In the above formula. Where $S_R = \sum_{i=1}^{20} (\hat{y}_i^* - \bar{y}^*)^2$ is the regression sum of squares, $S_E = \sum_{i=1}^{20} (y_i^* - \hat{y}_i^*)^2$ is the residual sum of squares.

It can be obtained from the ANOVA table in SPSS that the p value of this test is approximately $0.000 <$ $\alpha = 0.05$. It means that the regression coefficient corresponding to at least one independent variable is not equal to 0, that is, there is a linear relationship between at least one independent variable and the dependent variable, and the model is successfully established.

Meanwhile, it is not difficult to find from Table 8 that the calculated p values corresponding to β_1, β_2 are all 0.000 and less than $\alpha = 0.05$, indicating that the model is well established and has a reasonable binary linear relationship. The linear regression effect of independent variables F_1, F_2 on y^* is significant. The resulting binary linear regression equation is as follows,

$$
\hat{y}^* = 0.871F_1 + 0.485F_2 \tag{8}
$$

 \hat{y}^* is the approximate estimate of the dependent variable. For multiple linear regression, the modified multiple determination coefficient is used to determine the degree of linear regression, as shown in the following formula, where $S_T = S_R + S_E$, and $R_a^2 = 1 - \frac{S_E/20 - 2}{S_T/20 - 1}.$

Since the basic assumption of the linear regression model also requires that each random error ε_i (*i* = 1,2, … ,20) is independent of each other, the Durbin-Watson test is used to test the independence of the errors. Construct the DW statistic as shown in the following formula:

$$
DW = \frac{\sum_{i=2}^{20} (\hat{\varepsilon}_i - \hat{\varepsilon}_{i-1})^2}{\sum_{i=1}^{20} \hat{\varepsilon}_i^2}
$$
(9)

The results of the goodness-of-fit judgment and Durbin-Watson test are obtained as shown in Table 9 below:

Table 9: Model summary.

Model R			R Square Adjusted R Square DW	
	0.997	0.994	0.993	0.964

From Table 9, the calculated $R_a^2 = 0.994$ is very close to 1, which demonstrates that the linear fitting effect is very good. The model is reasonably established and can make more effective predictions.

The obtained Durbin-Watson test result is 0.964, which conforms to the value range of $0 <$ DW $<$ 4. However, there is a weak positive correlation between the residuals of two adjacent points, which can be approximately regarded as the absence of serial autocorrelation, that is, each random error can be considered independent of each other.

Finally, residual analysis is performed. In order to test whether the studentized residuals, that is, the regression standardized residuals, obey the standard normal distribution, a normal P-P plot is made for the regression standardized residuals, as depicted in Figure 1. In order to test that the variances of the normal distributions obeyed by the random errors ε_i (*i* = 1,2, ..., 20) are the same, in other words, they have variance consistency. Make a residual scatter plot with the fitted value of the dependent variable as the abscissa, as depicted in Figure 2.

Figure 1: Normal P-P diagram (Picture credit: Original).

Figure 2: Residual scatter plot (Picture credit: Original).

As can be seen from Figure 1, the residual points are basically distributed along the diagonal straight line, indicating that the expected cumulative

probability closely matches the observed cumulative probability. Therefore, it follows the normal distribution. It can be found in Figure 2 that the standardized residual scatter points are distributed around the 0 value, roughly within a band-shaped area, and there is no obvious trend. This means that the variances of the random errors are homogeneous, there is no heteroscedasticity problem, and the fit is good.

4 CONCLUSION

This article obtains a series of research results through statistical data analysis of Anhui Province's GDP and five impact indicators. After conducting descriptive statistics on the data, it was found through correlation analysis that there is strong correlation and collinearity between the indicators. In order to eliminate the impact of collinearity on the results, the five indicators were dimensionally reduced through factor analysis and finally two common factors were obtained. These two public factors are named social financial factors and social construction factors respectively. Finally, by establishing a multiple linear regression model, the binary linear regression equation of standardized GDP with respect to the above two factors was obtained. After testing, it can be proved that the equation has a good fitting degree.

It can be seen from the obtained regression equation that Anhui Province's GDP has a certain positive linear correlation with social macroeconomics, such as consumption, trade, and social infrastructure, such as school and highway construction. Therefore, in order to implement economic construction as the center and promote high-quality economic development in Anhui Province, the following guiding opinions are put forward for reference.

Deepen opening to the outside world and expand foreign trade cooperation: Promote the in-depth integration of Anhui Province with the international market and strengthen economic and trade cooperation with countries along the Belt and Road. It is recommended to formulate more flexible trade policies, attract foreign investment and technology introduction, and improve the level of opening up to the outside world. At the same time, we will strengthen the development of cross-border ecommerce and digital economy and improve the efficiency of import and export.

Stimulate residents' consumption vitality: Stimulate residents' consumption by increasing residents' income levels and improving employment

rates. Encourage the development of cultural tourism, health care and other consumer fields, and cultivate new consumption growth points. In addition, promote consumer confidence, strengthen brand building, and improve product and service quality.

Increase public budget investment: Increase government financial investment, especially in the fields of education, medical care, science and technology and other social undertakings. Increase support for innovative enterprises and scientific research institutions to promote technological innovation and industrial upgrading. At the same time, the fiscal expenditure structure should be optimized to ensure the effectiveness and sustainability of capital investment.

Accelerate the construction of transportation infrastructure and improve the connectivity of the province: Improve infrastructure levels and shorten transportation time between urban and rural areas and between provinces. Accelerate the planning and construction of transportation infrastructure such as highways and railways, promote smooth logistics, and promote coordinated development of industries. This will help reduce logistics costs, improve production efficiency, and enhance Anhui Province's competitiveness in the global value chain.

Optimize the education system and promote talent cultivation: Increase investment in higher education and improve the overall level of educational resources. At the same time, enterprises are encouraged to cooperate with universities to strengthen the integration of industry, education, research and application, and improve the practicality and employment rate of higher education. Cultivate more high-quality talents, provide intellectual support for upgrading the economic structure, and build an innovation highland.

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