

Graph Convolutional Networks and Particle Competition and Cooperation for Semi-Supervised Learning

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Abstract: Given the substantial challenges associated with obtaining labeled data, including high costs, time consumption, and the frequent need for expert involvement, semi-supervised learning has garnered increased attention. In these scenarios, Graph Convolutional Networks (GCNs) offer an attractive and promising solution, as they can effectively leverage labeled and unlabeled data for classification. Through their ability to capture complex relationships within data, GCNs provide a powerful framework for tasks that rely on limited labeled information. There are also other promising approaches that exploit the graph structure for more effective learning, such as the Particle Competition and Cooperation (PCC), an algorithm that models label propagation through particles that compete and cooperate on a graph constructed from the data, exploiting similarity relationships between instances. In this work, we propose a novel approach that combines PCC, GCN, and dimensionality reduction approaches for improved classification performance. The experimental results showed that our method provided gains in most cases.

1 INTRODUCTION

In computer science, classification tasks have advanced significantly over the last decade, driven by diverse approaches and deep learning models. However, despite these strides, performing classification with limited labeled data remains an intricate challenge, as deep models often require extensive data for training. In this context, semi-supervised learning (SSL) has emerged as a promising solution, positioned between supervised and unsupervised methods, SSL proves effective in handling substantial amounts of unlabeled data along with a modest quantity of labeled data. A key motivation for adopting SSL lies in the difficulty in obtaining labeled data, which is typically more arduous compared to acquiring unlabeled data. SSL techniques are particularly

useful for datasets with limited labeled data due to the high cost and time required for labeling.

In scenarios with limited labeled data, most supervised methods struggle to perform effectively due to their dependency on extensive labels. SSL overcomes this limitation by exploiting the underlying structure of data distributions. It uses labeled data to guide the learning process while also taking advantage of the unlabeled data to better understand the latent patterns present in the dataset (Wang et al., 2024).

Among the diverse techniques employed in SSL, pseudo-labeling stands out as an intuitive strategy. Based on the principle of proximity, pseudo-labeling assumes that an unlabeled instance is likely to share the same class as its closest labeled neighbor. By assigning pseudo-labels to such instances, the method incorporates unlabeled data into the training process, gradually enhancing the model's robustness and generalization capabilities.

In addition to the various SSL techniques, graph-based methods, such as Particle Competition and Cooperation (PCC) and Graph Convolutional Networks (GCNs), use graph structures to model relationships between instances, enhancing learning from

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labeled and unlabeled data. PCC is an algorithm that models label propagation through particles that compete and cooperate on a graph constructed from the data, exploiting similarity relationships between instances (Breve et al., 2012). On the other hand, GCNs learn node representations by aggregating neighborhood information (Kipf and Welling, 2017). Unlike traditional classifiers, GCNs require two inputs: feature representations and a graph that encodes contextual relationships. The graph is fundamental for enabling GCNs to consider neighborhood context, enhancing their classification capabilities.

Despite their potential, most GCN models are evaluated on scenarios where the graph is already available, such as citation datasets (e.g., Cora, CiteSeer) (McCallum et al., 2000; Giles et al., 1998). This limitation highlights the need to develop strategies that effectively encode similarity information in graph structures and feature representations.

In this work, we propose a novel approach for semi-supervised classification that combines the PCC algorithm with GCNs, integrating dimensionality reduction techniques such as t-SNE and UMAP. The main contributions of this work are:

- Combination of semi-supervised classifiers (PCC and GCN) with dimensionality reduction approaches (t-SNE and UMAP) for improving classification.
- Leverages dimensionality reduction techniques in conjunction with the semantic embeddings produced by the PCC classifier to enhance the training of the GCN model.
- Exploits dimensionality reduction methods to construct a more effective graph, improving the training process for both the PCC and GCN classifiers.

The remainder of this paper is organized as follows: Section 2 reviews the literature; Section 3 presents the formal notation used along with the paper; Section 4 discusses the proposed approach; Section 5 presents the experimental evaluation; Finally, in Section 6, we discuss the conclusions.

2 RELATED WORK

Recently, (Anghinoni et al., 2023) presented a novel approach to improving Graph Neural Networks (GNNs), the Transductive Graph Neural Network with Graph Dynamic Embedding (TransGNN), which introduces a new message-passing technique based on the Particle Competition and Cooperation (PCC)

model, originally designed for community detection in graphs. Traditional GNNs primarily learn from data attributes and relationships through message passing, but they often face the issue of over-smoothing, where node representations become indistinguishable. TransGNN incorporates a two-step learning process: first, it performs transductive learning on the network, using the PCC-based message passing to propagate learned information to the nodes. This is followed by the standard inductive learning used in conventional GNNs. The approach addresses over-smoothing and demonstrates improved classification accuracy, reduced computational cost, and effective learning with limited labeled data.

Despite the similarities between our approach and TransGNN, there are key differences in how PCC and the graph structure are employed. TransGNN incorporates PCC during the training phase as a dynamic message-passing mechanism, allowing the graph structure to evolve throughout the process. In contrast, our approach constructs the graph using a reduced representation of the original features. This graph serves two purposes: it provides the structural input for the GCN and is used by PCC to generate additional features, capturing local and global relationships. Additionally, the original features are reduced using UMAP, and the UMAP-reduced features are concatenated with the PCC output to form a combined feature representation. Unlike TransGNN, which focuses on dynamic graph adaptation, our method emphasizes the integration of dimensionality reduction techniques and semi-supervised classifiers to enhance performance in scenarios with limited labeled data.

Recent work in the literature (Benato et al., 2024) proposed an approach that combines pseudo-labeling and dimensionality reduction to improve classification in scenarios with limited labeled data. Their methodology leverages 2D projections to capture the data structure and guide the pseudo-labeling process. The study demonstrates that high-quality projections facilitate manual and automatic labeling and contribute to building more robust classifiers by integrating visualization techniques with active learning.

Our approach diverges from this by employing a fixed graph structure for GCN training, where dimensionality reduction techniques, such as UMAP, are integrated into the pipeline. The UMAP-reduced features are combined with additional features generated through PCC, emphasizing the interplay between graph-based learning and feature engineering.

In addition, the Optimum-Path Forest (OPF) classifier (Amorim et al., 2016) has been explored as a semi-supervised method that iteratively assigns labels based on confidence.

3 PROBLEM DEFINITION

In this section, we begin by presenting a formal definition of the semi-supervised learning classification task based on graphs, largely following the conventions outlined in (Kipf and Welling, 2017; Li et al., 2018).

Let \mathcal{G} represent an undirected graph, defined as $\mathcal{G} = (\mathcal{V}, \mathcal{E}, \mathbf{X})$, where \mathcal{V} denotes the node set, \mathcal{E} represents the edge set, and \mathbf{X} is a feature matrix. The node set \mathcal{V} is given by $\{v_1, v_2, \dots, v_n\}$, and the edge set is defined by pairs $(v_i, v_j) \in \mathcal{E}$, represented by a non-negative adjacency matrix $\mathbf{A} = [a_{ij}] \in \mathbb{R}^{n \times n}$. The feature matrix \mathbf{X} is defined as $[\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n]^T \in \mathbb{R}^{n \times d}$, where \mathbf{x}_i is a d -dimensional feature vector representing node v_i .

Let $\mathcal{Y} = \{y_1, y_2, \dots, y_c\}$ denote a set of labels assignable to nodes $v_i \in \mathcal{V}$. The node set can be further delineated as $\{v_1, v_2, \dots, v_L, v_{L+1}, \dots, v_n\}$, indicating a partially labeled dataset, with $\mathcal{V}_L = v_i, i = 1^L$ representing the labeled subset and $\mathcal{V}_U = v_i, i = L+1^n$ the unlabeled subset. Typically, in semi-supervised classification, $|\mathcal{V}_L| \ll |\mathcal{V}_U|$.

Formally, the training set is seen as a labeling function $l: \mathcal{V}_L \rightarrow \mathcal{Y}$, where $y_i = l(v_i)$ for all $v_i \in \mathcal{V}_L$. The objective is to learn a function $\hat{l}: \mathcal{V}_U \rightarrow \mathcal{Y}$ to predict the labels of unlabeled nodes in \mathcal{V}_U .

4 PROPOSED APPROACH

This section presents the proposed approach, and is divided as follows: Section 4.1 provides an overview of the methodology. In Section 4.2, we discuss the PCC algorithm. Section 4.3 details the graph construction process. The use of dimensionality reduction is explained in Section 4.4. Finally, Section 4.5 discusses the Graph Convolutional Networks (GCNs).

4.1 Overview and Main Ideas

The main idea of the proposed approach is to improve the effectiveness of semi-supervised classification by employing a novel workflow that combines the PCC classifier and dimensionality reduction approaches for training a GCN model. Figure 1 presents the proposed workflow. Step (A) performs dimensionality reduction over the original dataset features. Step (B) builds a kNN graph from the features generated in the previous step. The PCC classifier is executed in step (C), which uses the kNN graph as input and generates a new set of embeddings as output. Step (D) uses dimensionality reduction (e.g., UMAP or t-SNE)

on the original features and the output is concatenated with the PCC features. Finally, step (E) trains a GCN model considering the concatenated features from PCC and dimensionality reduction and the kNN graph generated in (B). The result is the classification of the elements in the test set.

4.2 Particle Competition and Cooperation

The semi-supervised learning particle competition and cooperation (PCC) approach (Breve et al., 2012) can be outlined as follows. Each node in an undirected and non-weighted graph represents a data item, and edges connect nodes representing similar data items. Initially, a particle is assigned to each labeled node. These particles navigate through the nodes using a random-greedy strategy, selecting the next node to visit among the neighbors of the current node. Particles associated with nodes of the same label form teams, cooperating to dominate the unlabeled nodes. Conversely, particles from different teams compete for control over the nodes.

Each node maintains a set of domination levels, representing the influence of different teams of particles. As particles traverse the graph, they increase their team's domination level in the visited nodes while decreasing those of other teams. Ultimately, each node is labeled based on the team with the highest domination level.

In a formal description, for every node v_i within the graph \mathbf{G} , a particle ρ_i is instantiated with its initial position set to v_i . Each particle ρ_j possesses a variable $\rho_j^{\text{st}}(t) \in [0, 1]$, denoting its strength, and determining its influence on the node it visits. Particles commence with maximum strength, $\rho_j^{\text{st}}(0) = 1$. Additionally, each particle ρ_j maintains a distance table $\rho_j^{\text{d}}(\mathbf{t}) = \rho_j^{d_1}(t), \rho_j^{d_2}(t), \dots, \rho_j^{d_n}(t)$, where each element $\rho_j^{d_i}(t) \in [0, n-1]$ signifies the distance from the particle's initial node v_j to any node v_i . This distance table dynamically updates as the associated particle traverses the graph.

Every node v_i possesses a domination vector $\mathbf{v}_i^{\text{oc}}(\mathbf{t})$, with each element $v_i^{\text{oc}_c}(t) \in [0, 1]$ representing the domination level of team/class c over node v_i . The total sum of domination levels for each node remains constant, ensuring that $\sum_{c=1}^C v_i^{\text{oc}_c} = 1$.

In nodes corresponding to labeled data items, domination levels remain constant, reflecting complete dominance by the associated class and no influence from other classes. Conversely, nodes representing unlabeled data items exhibit variable domination levels. Initially, all classes' domination levels are uni-

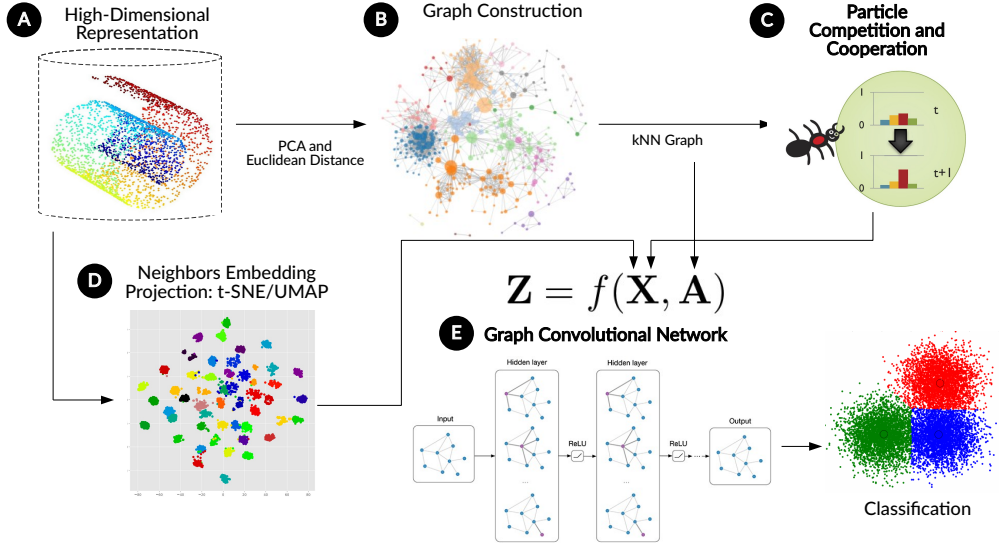


Figure 1: Our proposed Graph Convolution Networks and Particle Competition and Cooperation for improved classification.

formly set, but these levels are subject to change as particles visit the nodes. Thus, for each node v_i , the domination vector \mathbf{v}_i^{ω} is initialized as follows:

$$\mathbf{v}_i^{\omega c}(0) = \begin{cases} 1 & \text{if } x_i \text{ is labeled and } y(x_i) = c \\ 0 & \text{if } x_i \text{ is labeled and } y(x_i) \neq c \\ \frac{1}{C} & \text{if } x_i \text{ is unlabeled} \end{cases} \quad (1)$$

Whenever a particle ρ_j visits an unlabeled node v_i , the node's domination levels undergo the following update process:

$$\mathbf{v}_i^{\omega c}(t+1) = \begin{cases} \max\{0, v_i^{\omega c}(t) - \frac{\Delta_v \rho_j^{\omega}(t)}{C-1}\} & \text{if } c \neq y(\rho_j) \\ v_i^{\omega c}(t) + \sum_{r \neq c} v_i^{\omega r}(t) - v_i^{\omega r}(t+1) & \text{if } c = y(\rho_j) \end{cases} \quad (2)$$

where $0 < \Delta_v \leq 1$ is a parameter regulating the rate of change, and $y(\rho_j)$ represents the class of particle ρ_j . Upon visiting node v_i , particle ρ_j adjusts the node's domination levels as follows: it elevates the domination level of its class ($v_i^{\omega c}$ where $c = y(\rho_j)$) while simultaneously reducing the domination levels of other classes ($v_i^{\omega c}$ where $c \neq y(\rho_j)$). Notably, this update procedure does not apply to labeled nodes, as their domination levels remain fixed.

The strength of a particle can vary based on the domination level of its corresponding class at the node it currently occupies. In each iteration, the particle's strength is adjusted according to $\rho_j^{\omega}(t) = v_i^{\omega c}(t)$, where v_i denotes the visited node, and $c = y(\rho_j)$.

During each iteration, a particle ρ_j selects a node v_i to visit from among the neighbors of its current node. The probability of selecting a node v_i is determined by two factors: a) the domination of the parti-

cle's class on that node, denoted by $v_i^{\omega c}$, and b) the inverse of its distance, $\rho_j^{d_i}$. This probability is expressed as:

$$p(v_i | \rho_j) = (1 - p_{\text{grd}}) \frac{W_{qi}}{\sum_{\mu=1}^n W_{q\mu}} + p_{\text{grd}} \frac{W_{qi} v_i^{\omega c} (1 + \rho_j^{d_i})^{-2}}{\sum_{\mu=1}^n W_{q\mu} v_{\mu}^{\omega c} (1 + \rho_j^{d_{\mu}})^{-2}}, \quad (3)$$

where q is the index of the node being visited by particle ρ_j , c is the class label of particle ρ_j , $W_{qi} = 1$ if there is an edge between the current node and the node v_i , and $W_{qi} = 0$ otherwise. After applying (2), a particle remains on the selected node only if its class domination level is the highest on that node. Otherwise, a "shock" occurs, prompting the particle to revert to the previous node and await the next iteration. The parameter p_{grd} , ranging between 0 and 1, controls the balance between randomness and greediness in the probabilities. A value of 0 implies uniform probabilities among neighbors, while a value of 1 indicates strong influence from domination levels and distances.

The algorithm's termination is based on the stabilization of average maximum domination levels across nodes, indicating dominance by a single class. Further details can be found in (Breve et al., 2012).

4.3 Graph Construction

Principal Component Analysis (PCA) (Jolliffe and Springer-Verlag, 2002) reduces the dimensionality from the input dataset. Previous work (Breve and Fischer, 2020) has shown that PCC benefits from the use

of only a few principal components to build its input graph, instead of all the original dimensions, in most scenarios. As previously mentioned, the unweighted and undirected graph is built by representing each dataset instance as a graph node. Edges connect each node to its k -nearest neighbors, according to the Euclidean distance among the original data points projected onto the selected principal components space. In this paper, the 10 principal components and $k = 5$ are used throughout all the simulations.

4.4 Neighborhood Embedding Projection

In general, methods based on neighbor embedding assign probabilities to neighborhood relationships to model attractive and repulsive forces between neighboring and non-neighboring points in projections (Ghojogh et al., 2021). This framework is foundational for non-linear dimensionality reduction (Damrich et al., 2022) and connects to various research fields. Two methods have become standard for visualizing high-dimensional data (Damrich et al., 2022): t-distributed Stochastic Neighbor Embedding (t-SNE) (van der Maaten and Hinton, 2008) and Uniform Manifold Approximation and Projection (UMAP) (McInnes et al., 2018).

The t-distributed stochastic neighbor embedding (t-SNE) (van der Maaten and Hinton, 2008) is an extension of the original Stochastic Neighbor Embedding (SNE) technique (Hinton and Roweis, 2002). SNE is a probabilistic approach aimed at mapping data into a low-dimensional space while maintaining local neighborhood relationships. It does this by defining a probability distribution that reflects the potential neighbors in the high-dimensional space and then approximates this distribution within the low-dimensional projection. However, t-SNE (van der Maaten and Hinton, 2008) was specifically developed to overcome a known optimization issue in SNE, called the crowding problem. t-SNE's main innovations include a symmetrized version of the SNE cost function and the use of a Student's t-distribution instead of a Gaussian, making the method not only more straightforward to optimize but also less prone to clustering points too closely together (van der Maaten and Hinton, 2008).

Uniform Manifold Approximation and Projection (UMAP) (McInnes et al., 2018) is a manifold learning technique designed for dimensionality reduction. It is built upon a sophisticated mathematical foundation, that includes concepts from manifold theory and topological data analysis. UMAP exploits local manifold approximations and fuzzy topological representations

for both high and low-dimensional data. Following this, it optimizes the projection layout by minimizing cross-entropy between these topological representations (McInnes et al., 2018; Ghojogh et al., 2021). Unlike t-SNE, UMAP is not restricted by the embedding dimension, making it versatile for general-purpose dimensionality reduction.

Several studies have explored the use of dimensionality reduction techniques as a preprocessing step in information retrieval tasks, demonstrating improvements in data distribution and feature quality (Leticio et al., 2024; Kawai et al., 2024). In our approach, we apply these techniques to transform the original high-dimensional representations into more compact and informative embeddings, preserving the proximity relationships among samples.

The resulting embeddings provide a more structured representation of the data, serving as input to a GCN. By applying dimensionality reduction before the GCN, we aim not only to reduce the computational complexity of the model but also to highlight relevant structures in the data, facilitating the GCN's ability to learn effective representations.

4.5 Graph Convolutional Networks

In recent years, there has been significant interest in exploiting deep learning techniques for graph-structured data (Cai et al., 2018). Among these techniques, Graph Convolutional Networks (GCNs), introduced by (Kipf and Welling, 2017), have emerged as a relevant graph-based neural network model. GCNs learn node embeddings (representation) by iteratively aggregating information from neighboring nodes, and incorporating the graph structure into the neural network model. In their first application, a two-layer GCN model was utilized for semi-supervised node classification, considering a graph represented by a symmetric adjacency matrix \mathbf{A} .

The network can be formulated as a function of both the feature matrix \mathbf{X} and the adjacency matrix \mathbf{A} : $\mathbf{Z} = f(\mathbf{X}, \mathbf{A})$, where $\mathbf{Z} = [\mathbf{z}_1, \mathbf{z}_2, \dots, \mathbf{z}_n]^T \in \mathbb{R}^{n \times c}$ represents the matrix of node embeddings, and each \mathbf{z}_i is a c -dimensional vector learned for the node v_i .

As a preprocessing step, the normalized adjacency matrix is computed as $\hat{\mathbf{A}} = \tilde{\mathbf{D}}^{-1/2} \tilde{\mathbf{A}} \tilde{\mathbf{D}}^{-1/2}$, where $\tilde{\mathbf{A}} = \mathbf{A} + \mathbf{I}$ and $\tilde{\mathbf{D}}$ is the degree matrix of $\tilde{\mathbf{A}}$. Then, the function $f(\cdot)$ which represents the two-layer GCN model is: $\mathbf{Z} = \log(\text{softmax}(\hat{\mathbf{A}} \text{ReLU}(\hat{\mathbf{A}} \mathbf{X} \mathbf{W}^{(0)} \mathbf{W}^{(1)})))$.

The matrix $\mathbf{W}^{(0)} \in \mathbb{R}^{d \times H}$ defines the neural network weights for an input-to-hidden layer with H feature maps, while $\mathbf{W}^{(1)} \in \mathbb{R}^{H \times c}$ is a hidden-to-output matrix. Both matrices $\mathbf{W}^{(0)}$ and $\mathbf{W}^{(1)}$ are trained us-

ing gradient descent, considering the cross-entropy error over all labeled nodes $v_l \in \mathcal{V}_L$. The softmax activation function is applied row-wise to yield a probability distribution over the c class labels for each node, ensuring that the probabilities sum to 1 per node. Following the logarithm function, each node v_i is assigned a label corresponding to the class with the less negative value in its embedding representation \mathbf{z}_i .

Building on the success of GCNs (Kipf and Welling, 2017), various related models have been proposed (Kipf and Welling, 2017; Velickovic et al., 2018; Klicpera et al., 2019a; Wu et al., 2019; Bianchi et al., 2019; Li et al., 2018; Bai et al., 2019; Klicpera et al., 2019b). Some of these models focus on the structure of network models (Wu et al., 2019; Bianchi et al., 2019; Klicpera et al., 2019a; Bai et al., 2019), while others present contributions in training methodologies and manifold information (Li et al., 2018; Klicpera et al., 2019b).

For the node classification task, we used the GCN by integrating the original features provided by the datasets with those generated by Particle Competition and Cooperation (PCC). We constructed the feature matrix \mathbf{X} by concatenating the original features, reduced or not in dimensionality through neighborhood embedding projections (Section 4.4), with the PCC features, which capture correlations between the data. This strategy allows the GCN to leverage both the original features of the data and the correlation information provided by PCC.

The adjacency matrix \mathbf{A} is obtained from the graph built by PCC, as detailed in Section 4.3. In this unweighted and undirected graph, the nodes represent the dataset instances, and the edges connect each node to its k nearest neighbors based on the Euclidean distance of the data points projected onto the principal components selected by PCA.

It is important to highlight that dimensionality reduction methods are used to reduce the dimensionality of the original features before their concatenation in the matrix \mathbf{X} , while PCA is applied during the graph construction by PCC.

5 EXPERIMENTAL EVALUATION

In this section, we present the experimental evaluation of our approach. Section 5.1 describes the datasets and experimental protocol, followed by parameter settings in Section 5.2. The results and comparisons are presented in Section 5.3.

5.1 Datasets and Experimental Protocol

The experimental analysis was conducted on seven datasets: g241c, g241n, Digit1, USPS, COIL, COIL2, and BCI. Most datasets contain 1500 points and 241 dimensions, except for BCI, which has 400 points and 117 dimensions. Each dataset has two splits, one split with 10 labeled points and another with 100.

The majority of these datasets are binary, except for COIL, which contains 5 classes. COIL2 is a binary version of COIL. Table 1 summarizes the characteristics of the datasets used in the experiments.

Table 1: Characteristics of the Datasets.

Dataset	Points	Dimensions	Labeled Splits
g241c (set 5)	1500	241	10, 100
g241n (set 7)	1500	241	10, 100
Digit1 (set 1)	1500	241	10, 100
USPS (set 2)	1500	241	10, 100
COIL (set 6)	1500	241	10, 100
COIL2 (set 3)	1500	241	10, 100
BCI (set 4)	400	117	10, 100

5.2 Parameters Settings

Two parameters were considered regarding parameter settings: learning rate and number of neurons. The impact of these parameters was evaluated by varying its value until a suitable value was found. Figure 2 shows the impact of the learning rate on accuracy. The tested values were 0.1, 0.01, 0.001, 0.0001, and 0.00001, with the best value being 0.001. Figure 3 presents the evaluation of different numbers of neurons in the hidden layer. The values tested were 16, 32, 48, 64, 80, 96, and 112. The best accuracy was obtained with 96 neurons.

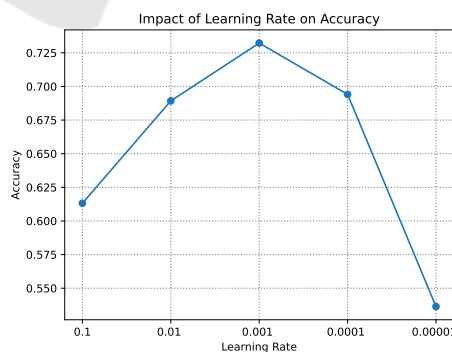


Figure 2: Impact of learning rate on accuracy.

5.3 Results and Comparisons

This section discusses about the accuracy results of the proposed approach. Table 2 presents the classification accuracy across all datasets, each evalu-

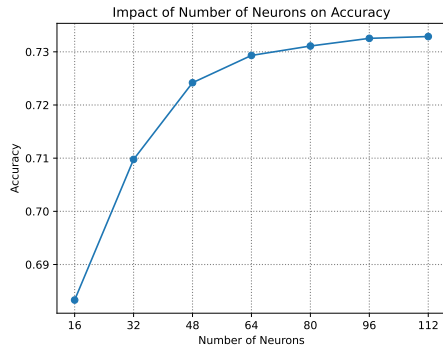


Figure 3: Impact of the number of hidden neurons on accuracy.

ated with 10 and 100 labeled instances. The methods compared include the baseline GCN (Kipf and Welling, 2017), the Particle Competition and Cooperation (PCC) approach (Breve et al., 2012), and combinations of PCC with GCN enhanced by dimensionality reduction techniques t-SNE and UMAP.

The results indicate that the combination of PCC, GCN, and UMAP achieves the highest mean accuracy (0.7569), outperforming standalone GCN and PCC. With 10 labeled instances, this approach has the best accuracy in four datasets, and with 100 instances, it maintains top performance in most cases.

Additionally, the use of dimensionality reduction improves GCN’s classification, demonstrating its effectiveness in enhancing the classification capabilities of GCNs. These findings suggest that combining PCC with GCN and employing dimensionality reduction not only leverages structural information from the graph but also enhances feature representation, leading to improved classification accuracy.

Furthermore, an evaluation of three GCN models was considered: GCN (Kipf and Welling, 2017), SGC (Wu et al., 2019), and APPNP (Klicpera et al., 2019a). The analysis was done by applying the proposed approach, with the same parameters and datasets, in these different models and analyzing the mean. Table 3 contains the evaluation result. Note that GCN has better accuracy in most of the cases.

6 CONCLUSIONS

This work proposed a novel approach combining PCC and dimensionality reduction to improve semi-supervised classification in GCNs. By applying t-SNE and UMAP to reduce the original features and concatenating them with the embeddings generated by PCC, which uses PCA for graph construction, we enriched the feature representation fed into GCNs. Experimental results demonstrated that this combina-

Table 2: Evaluation and comparison of the proposed approach in different datasets.

Dataset	Labeled Set Size	GCN	PCC	PCC+ GCN	PCC+ t-SNE	PCC+ UMAP
Digit1	10	82.26	88.33	86.77	91.70	91.77
USPS	10	76.96	80.10	77.92	75.09	83.08
COIL2	10	57.43	59.32	57.37	60.81	61.69
BCI	10	51.46	51.04	51.57	50.38	50.56
g241c	10	75.99	72.22	75.89	75.16	73.68
COIL	10	32.22	38.03	32.51	37.46	39.68
g241n	10	72.64	68.65	72.68	71.47	68.76
Digit1	100	95.90	97.19	97.40	97.86	97.61
USPS	100	93.61	94.33	94.19	92.86	94.37
COIL2	100	87.48	91.87	87.37	90.49	92.05
BCI	100	54.32	53.22	54.50	52.44	52.94
g241c	100	81.70	82.36	81.69	82.94	82.82
COIL	100	72.40	81.22	72.84	71.61	80.41
g241n	100	90.56	89.59	90.55	90.08	90.36
Mean	-	73.21	74.82	73.80	74.30	75.70

Table 3: Evaluation of different GCN models in combination with UMAP low-dimensional embeddings.

Dataset	Labeled Set Size	PCC+ GCN	PCC+ SGC	PCC+ APPNP
Digit1	10	91.77	69.94	92.31
USPS	10	83.08	71.85	80.64
COIL2	10	61.69	046.7	60.75
BCI	10	50.56	49.97	50.72
g241c	10	73.68	56.62	74.04
COIL	10	39.68	25.75	37.65
g241n	10	68.76	55.45	67.52
Digit1	100	97.61	75.09	97.55
USPS	100	94.37	75.70	93.90
COIL2	100	92.05	67.24	90.75
BCI	100	52.94	50.11	52.58
g241c	100	82.82	68.64	82.86
COIL	100	80.41	36.71	74.84
g241n	100	90.36	66.25	90.31
Mean	-	75.70	58.86	74.74

tion outperformed standalone methods, particularly in scenarios with limited labeled data.

Future work could explore alternative dimensionality reduction methods or optimize feature concatenation strategies. Applying this approach to datasets with diverse characteristics would further validate its robustness and adaptability. Additionally, investigating alternative graph construction methods may yield new insights.

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