

PROBABILISTIC APPEARANCE-BASED NAVIGATION OF A MOBILE ROBOT

Controlling a Robot in Route Following

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Abstract: In this work, a solution to the problem of multi-robot following routes is proposed using an appearance-based method. In this approach, several images are stored along the route to follow, using an uncalibrated forward-looking camera. To extract the most relevant information, an incremental PCA process has been implemented. This incremental process allows adding new locations to the PCA database without necessity of creating it from the scratch. Then, the follower robots can follow the route while a leader one is still recording it. These follower robots, using this database, make first an auto-location process to know their current position and then a control phase to compute the necessary steering speed to tend to the route and follow it till the end. Both speeds are obtained also through the visual information in an appearance-based approach. The problem of 'visual aliasing', typical in office environments, is avoided with a probabilistic approach that, using a Markov-process model, makes the localization more robust. The experimental results have shown how this is a simple but robust and powerful approach for routes in an office environment.

1 INTRODUCTION

In the last years, some applications that require the use of a team of robots have emerged. They require the coordination between the members of the team. In some applications, the use of collaborative robotics clearly improves the performance, comparing to a single robot carrying out the same task. As an example, (Thrun, 2002) presents a probabilistic EKF algorithm where a team of robots builds a map online, while simultaneously they localize themselves. (Fenwick, 2002) takes into account the problem of the concurrent mapping and localization with extra positional information available when multiple vehicles operate simultaneously. In (Ho, 2005), a map is built using visual appearance. From sequences of images, acquired by a team of robots, subsequences of visually similar images are detected and finally, the local maps are joined into a single map.

A typical problem in collaborative robotics implies a path following e.g. to perform a surveillance task in an office environment or an assembly or delivery task in an industrial environment. Also, the problem of formations,

where a team of robots must navigate keeping a relative position in a structure of robots, can be seen as a problem of path following, where one or several robots must follow the path the leader is recording.

In the case of route following, to carry out the navigation of a robot from one point to another in an environment, a map is required. In the last years, intensive research on this field, using SLAM techniques (Simultaneous Localization And Mapping) has been developed. This approach tries to build a global map of the environment while simultaneously determining the location of the robot. Usually, these approaches rely on the extraction of several landmarks or characteristic points of the environment both natural or artificial, as (Thrun, 2002) does.

However, the problem of route following can be solved without necessity of creating complex maps of the environment. It is just needed a teaching step, where the route to follow is learned, and a navigation step, where the second robot follows the route just comparing its current sensory information with the data stored in the database. Classical approaches in this field are model-based approaches, where the extraction of several landmarks or feature

points along the images allows computing the image Jacobian, that relates the change of the coordinates in the image with the changes in motion in the ground plane. Then, using the principles of visual servoing, the second robot can follow the route, as in (Burschka, 2001). Also, in the behaviour-based control (Balch, 1998), some features of the images are extracted to carry out the localization and navigation of the members of a team in a formation problem. However, other approaches suggest that these processes could be achieved just comparing the general visual information on the images, without necessity of extracting any feature. These appearance-based approaches are specially useful for complicated scenes in unstructured environments where appropriate models for recognition are difficult to create. As an example, (Matsumoto, 1999) addresses a method consisting on the direct comparison of low-resolution images. This method may lead to errors when the size of the route is quite long so other features must be added to make the method more robust, such as histogram, texture and density of edges, (Zhou, 2003). However, these features contain no geometric information so they are useful just for localization but not for navigation.

When working with the whole images, the complexity of the problem can be reduced by means of the PCA (Principal Components Analysis) subspace as in (Kröse, 2004) or (Maeda, 1997), where through PCA techniques a database is created using a set of views with a probabilistic approach for the localization. In classical PCA approaches, all the views along the route must be available before the compression can be done so the navigation of the second robot cannot begin until the leader has finished learning the route. Actually, a new model must be built from the scratch when we want to include information about new locations in the map. These problems can be overcome using an incremental PCA method, as shown in (Payá, 2007).

In this paper, we present an appearance-based method for route following where incremental PCA has been used to build the database, and a probabilistic Markov process has been implemented for robot localization during the navigation. First, the representation of the environment along the route is detailed. Then, in section 3, the basics of localization and control in route following are outlined. In the 4th section, the probabilistic approach to make navigation more robust is presented and to finish, the results and conclusions of the work are shown.

2 REPRESENTATION OF THE ENVIRONMENT

The philosophy of the appearance-based methods consists in working with the general visual information of the images, without extracting any interesting point. Thus, this family of methods presents the disadvantages of the size of the database necessary to retain all the information of the environment and the computational cost of the comparisons between the whole images.

When working with 64x64 images, the data vectors fall in a 4096 dimensional space. However, all these data are generated from a process with just three degrees of freedom (position and orientation of the robot). This way, before storing the images, a reduction of the dimensionality of the data can be performed with the goal of retaining the most relevant information of each scene. Since pixels tend to be very correlated data, a natural reduction step consists on performing Principal Components Analysis (PCA), as in (Kirby, 2001).

Each image $\bar{x}_j \in \mathcal{R}^{M \times 1}$; $j=1 \dots N$, being M the number of pixels and N the number of images, can be transformed in a feature vector (also named projection of the image) $\bar{p}_j \in \mathcal{R}^{K \times 1}$; $j=1 \dots N$, being K the PCA features containing the most relevant information of the image, $K \leq N$. In traditional PCA, first of all, the data matrix is built using the images of the environment. The PCA transformation is computed from the covariance of the data matrix using SVD and the Turk and Pentland's method (Turk, 1991). After the process, a new data matrix with the most relevant information is obtained.

In classical PCA approaches, all the images along the environment must be available before carrying out the compression. This way, the robots that follow the route should wait the leader one to run till the end. However, in collaborative tasks, it is usual that some robots follow the first one while it is still recording the information. Then, with this approach, the robot that is building the database should do it from the scratch when a new image along the route is captured, what is computationally very expensive. To overcome this disadvantage, a progressive construction of the database can be implemented, using the incremental PCA algorithm exposed in (Artac, 2002). When the leader captures a new image, it is added to the database, updating all the projections that were previously stored.

As can be proved, when having a set of eigenvectors from a set of views, when a new image is added to the database, these eigenvectors and the

projection of the existing images can be updated following the next four-step algorithm (Artac, 2002):

1. First, the mean must be updated with the expression:

$$\bar{m}' = \frac{1}{N+1}(N \cdot \bar{m} + \bar{x}_{N+1}). \quad (1)$$

2. Now, the set of eigenvectors must be updated so that they include the information of the new image \bar{x}_{N+1} . To do it, we compute the residual vector, that is the difference between the reconstruction and the original $N+1$ image $\bar{h}_{N+1} = (V \cdot \bar{p}_{N+1} + \bar{m}) - \bar{x}_{N+1}$. This vector is orthogonal to the old eigenvectors. Then, it must be normalized (so that it becomes a unit vector), obtaining \hat{h}_{N+1} .

3. The new matrix of eigenvectors V' can be obtained by appending \hat{h}_{N+1} to V and rotating them, according to the next expression:

$$V' = \begin{bmatrix} V & \hat{h}_{N+1} \end{bmatrix} \cdot R. \quad (2)$$

being R the solution to the eigenproblem $D \cdot R = R \cdot \Lambda'$ and D is:

$$D = \frac{N}{N+1} \begin{bmatrix} \Lambda & \bar{0} \\ \bar{0}^T & 0 \end{bmatrix} + \frac{N}{(N+1)^2} \begin{bmatrix} \bar{p} \cdot \bar{p}^T & \delta \cdot \bar{p} \\ \delta \cdot \bar{p}^T & \delta^2 \end{bmatrix}. \quad (3)$$

where $\delta = \bar{h}_{N+1} \cdot (\bar{x}_{N+1} - \bar{m})$, $\bar{p} = V^T \cdot (\bar{x}_{N+1} - \bar{m})$ and Λ is a diagonal matrix containing the original eigenvalues. This way, if $V \in \mathfrak{R}^{M \times K}$, then $V' \in \mathfrak{R}^{M \times (K+1)}$. It must be studied whether this new dimension is significant or not. In this work, two different criteria have been used with this goal. First, if the last eigenvalue is under a percentage of the first one, it is considered that it does not retain enough information so the last eigenvector is removed of the system. Also, if the new image can be correctly represented by the previous set of eigenvectors, the new dimension is not added. To know it, the module of the residual vector is computed. If this module is under a threshold, the new image can be represented with enough accuracy with the previous set of eigenvectors so the new dimension is not taken into account.

4. The image representations can be updated with the next expression:

$$\bar{p}_{i(N+1)} = (R')^T \cdot \begin{bmatrix} \bar{p}_{i(N)} \\ 0 \end{bmatrix} + [V' \cdot \hat{h}_{N+1}]^T \cdot (\bar{m} - \bar{m}'). \quad (4)$$

Then, when a new image arrives, the previous projections in the database and the eigenvectors are updated and the new projection is added. This

method has shown to be efficient in robot navigation (Payá, 2007).

3 LOCALIZATION AND CONTROL FOR ROUTE FOLLOWING

Once the database is created, one robot can follow the route running successively two tasks: auto-localization and control.

Auto-localization: The robot captures an image and using this information it must decide which of the set of the observations is the closest one. A projection of the current image on the current eigenspace calculated by the leader allows determining it. This returns a K -components vector that contains the main information of the view. Then, this vector has to be compared with those stored in the database. The one that offers the minimum Euclidean distance is the matching one. It is taken as the current position of the robot.

Control: From each image stored in the database, j , a set of N' sub-windows is obtained from the whole image where $\bar{w}_j^i \in \mathfrak{R}^{M' \times 1}$, is each sub-window. The sub-windows are obtained scanning the original scene with a step in the horizontal axis (fig. 1(a), 1(b)). Carrying out a process of PCA compression, the PCA components $\tilde{f}_j^i \in \mathfrak{R}^{K' \times 1}$, of each sub-image are calculated, where $K' \leq N'$. Fig. 1(c) shows these projections as black dots in the case $K'=3$. During the autonomous navigation, five sub-windows ($\bar{w}_j^A, \bar{w}_j^B, \bar{w}_j^C, \bar{w}_j^D, \bar{w}_j^E$) are taken on the currently captured view (fig. 1(d)) and tracked over the central band of the matching image. To do this, once the robot knows its location, the PCA components of these five sub-windows are calculated. This operation returns five K' -components vectors ($\tilde{f}_j^A, \tilde{f}_j^B, \tilde{f}_j^C, \tilde{f}_j^D, \tilde{f}_j^E$) that are shown as red crosses on fig. 1(c). Then, the most similar projections to each of them are extracted. These most similar projections are those that fall in five spheres whose centers are ($\tilde{f}_j^A, \tilde{f}_j^B, \tilde{f}_j^C, \tilde{f}_j^D, \tilde{f}_j^E$).

The radius of these spheres is chosen so that a number of corresponding windows is extracted. In this work, a total number of seven sub-windows are extracted. The linear and steering velocities are inferred using a controller, whose inputs are the most similar projections to each of the five sub-windows. Analyzing these data and solving possible inconsistencies, the controller infers the linear and

steering velocities of the robot to tend to the recorded route.

To do it, once the most similar sub-windows are recognized, the controller tries to arrange them and look for a correlation that shows clearly if the robot has to turn left or to turn right to tend to the pre-recorded route.

Fig. 2 shows an example of how the controller works. In this figure, the blue crosses are the seven most similar sub-windows. On this figure, the most similar window to \bar{w}_j^A is the window 8 (\bar{w}_j^8), the most similar to \bar{w}_j^B are the windows 12, 13 and 14 ($\bar{w}_j^{12}, \bar{w}_j^{13}, \bar{w}_j^{14}$), the most similar to \bar{w}_j^C are 15 and 16 ($\bar{w}_j^{15}, \bar{w}_j^{16}$), \bar{w}_j^D has no correspondences and the most similar to \bar{w}_j^E is the 3rd window (\bar{w}_j^3). This distribution of correspondences shows that the robot has to turn left so that the sub-windows fit with those of the corresponding image. The correspondence of \bar{w}_j^E has been considered as an outlier so it has been discarded. Actually, this is a wrong point due to the fact that this window falls out of the image \bar{x}_j . The steps that are followed to deduct the value of the control action are are:

1. Several least-squares fittings are done using the following data at each fitting:

- Correspondences of the 2 first sub-windows.
- Correspondences of the 3 first sub-windows.
- Correspondences of the 4 first sub-windows.
- All the correspondences.

- Correspondences of the 4 last sub-windows.
- Correspondences of the 3 last sub-windows.
- Correspondences of the 2 last sub-windows.

2. The most confident fitting of the previous ones is chosen. The criteria used to choose it are the number of correspondences used to do the fitting, the confidence and the slope of the fitted line (in this work, the slope has to be near to $N/5$).

3. The ordinate at the origin of the chosen linear regression shows how the steering of the robot should be to tend to the route correctly. If it is positive, the robot must turn left and if it is negative, the robot must turn right.

4. To improve this controller, a detector of outliers has been added so that they are removed before computing the final linear regression.

Fig. 3 and fig. 4 show two additional examples of distributions and the least squares fitted line that has been computed. On fig. 3, all the points are used to make the fitting and an outlier has been detected at position \bar{w}_j^D . In this case, the robot has to go straight to follow the route. On fig. 4, the windows corresponding to \bar{w}_j^D and \bar{w}_j^E have been used and an outlier has been detected. As a result, the robot has to turn right to follow the route, with a steering proportional to the ordinate in the origin.

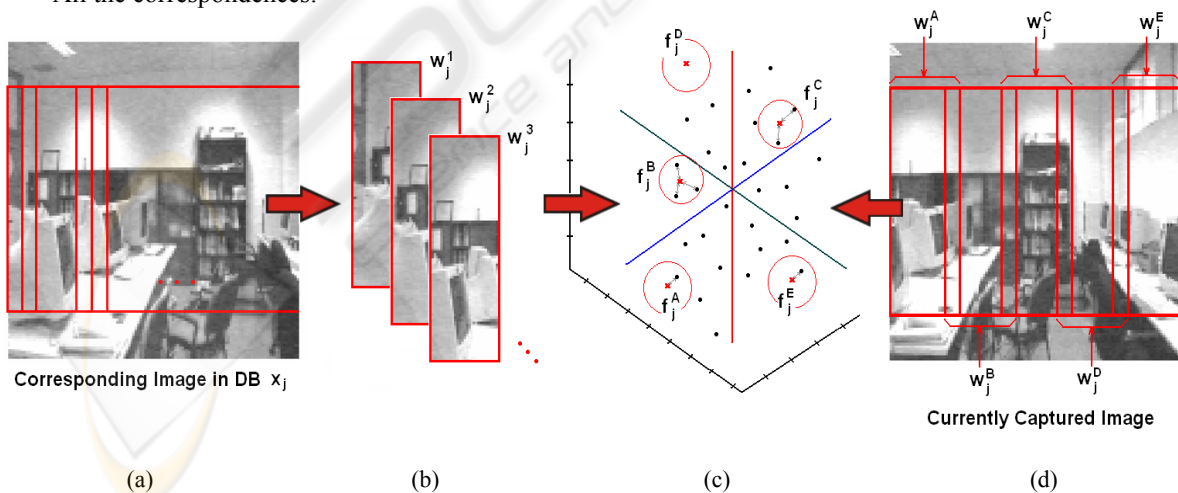


Figure 1: Calculating the linear and steering speeds of the follower robot. When it captures a new image, five sub-windows are extracted and tracked over the corresponding image in the DB. The most similar projections are the inputs of a controller that computes the necessary speeds of the robot.

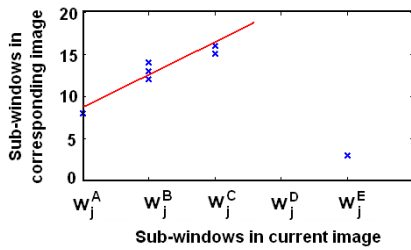


Figure 2: Calculation of the control action. Case 1: in this case, the robot has to turn left to follow the route.

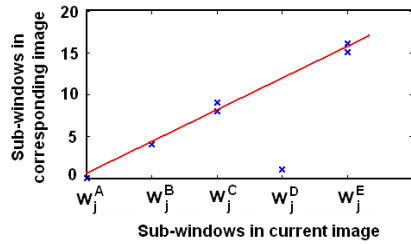


Figure 3: Calculation of the control action. Case 2: the robot has to go straight to follow the route.

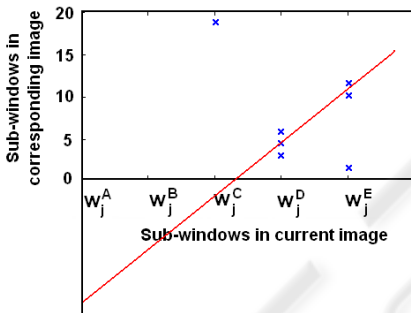


Figure 4: Calculation of the control action. Case 3: the robot has to turn right to follow the route.

4 IMPROVING VISUAL PATH FOLLOWING

In office environments, the simple localization method exposed tends to fail often as a result of ‘visual aliasing’. This means that the visual information captured at two different locations that are far away can be very similar. To avoid these problems, a probabilistic approach, based on a Markov process, has been used. The current position of the robot can be estimated using the Bayes rule:

$$p(x|z; \theta) \propto p(z|x; \theta) \cdot p(x) \quad (5)$$

where $p(x)$ denotes the probability that the robot is in the position x before observing z . This value is

estimated using the previous information and the motion model. $p(z|x)$ is the probability of observing z if the position of the robot is x . This way, a method to estimate the observation model must be deduced. In this work, the distribution $p(z|x)$ is modeled through a sum of Gaussian kernels, centered on the k most similar points of the route:

$$p(z|x) = \frac{1}{k} \cdot \sum_{i=1}^k \left(\gamma_j \cdot e^{-\left(\frac{x-x_j}{\sigma}\right)^2} \right); \quad j=1 \dots N. \quad (6)$$

Each kernel is weighted by a value of confidence $\gamma_j \in [0,1]$, that depends on the degree of similarity of the projection of the current image with the projections in the database. Then, these kernels are convolved with a Gaussian function that models the motion of the robot (knowing the previous position and velocity of the robot). At last, the contribution of each resulting kernel, c_j , is computed on each point, and the new position is considered at the point with highest contribution c_j^{\max} .

Fig. 5 shows this process for $k=5$ kernels. First, the five most similar positions are selected. Then, a kernel function is assigned to each position. After that, the motion model is applied and at the end, the contribution of each kernel to each position is computed, selecting the point with the maximum contribution.

This method works well only if a robust initial estimation of the position is available. Then, the beginning of the navigation could be a problem if the robot is far from the route. To solve this problem, a clustering approach has been used. The robot makes small angular and linear movements around the initial position, taking images during the movement. Each image is localized comparing the distance of its PCA components with the projections in the database. Then, it is classified into the group whose centre is closer to the localization of the image. If this distance is over a threshold, the new image will constitute a new cluster. Otherwise, it will be included in the corresponding cluster and its centre will be updated. Once all the images are classified, the groups with few images are discarded and the group in which the variance of the distance of the elements is the lowest is chosen. The corresponding location is calculated as the centre of the chosen cluster. Fig. 6 shows this approach. In this case, cluster 2 and position 9 would be selected.

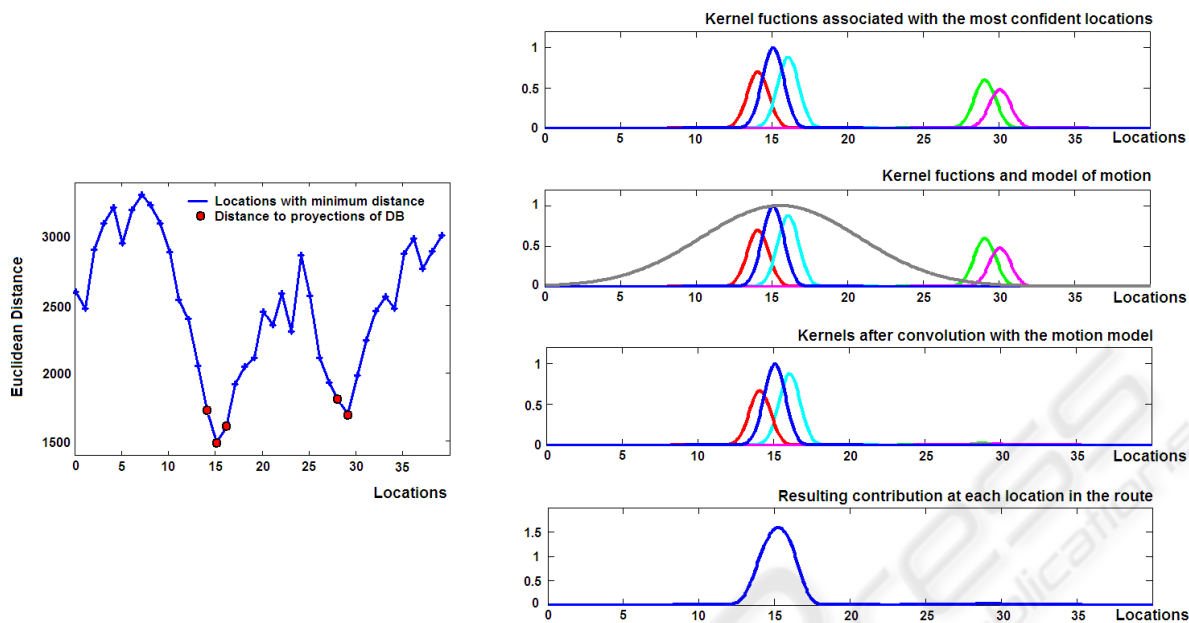


Figure 5: Improving localization through a probabilistic approach. In this case, after the process, it will be deducted that the current position is the 15th one.

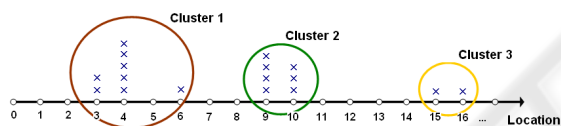


Figure 6: Clustering approach for initial localization of the follower robot.

5 RESULTS

Several experiments have been carried out to validate the approach. Fig. 7 and fig. 8 show a typical route recorded in an office environment and the route of the follower when it starts from two different points around it. Typically, the follower robot tends to the route and follows it, showing a great performance on the straight lines and a relatively bigger error in the turnings. However, with this approach, the robot is able to find the route and tend to it, showing a very stable behaviour till the end. Comparing incremental PCA with batch PCA, the batch one performs slightly better when calculating overall error, but incremental PCA performs correctly the task, as shown on fig. 7 and fig. 8, and with the advantages it supposes. Fig. 9 shows the evolution of the localization during the navigation of the follower robot and the probability calculated, what can be a measure of the precision.

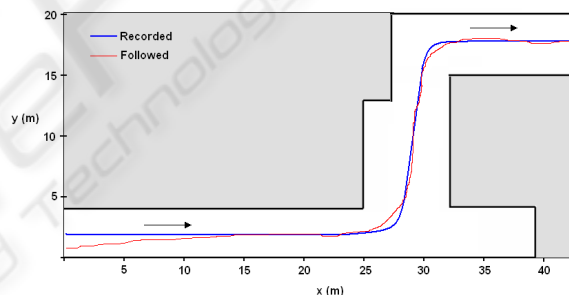


Figure 7: Results of navigation 1. Route recorded and route followed.

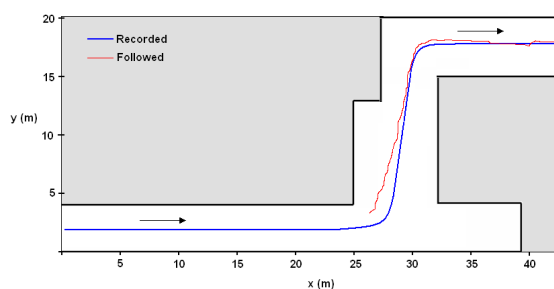


Figure 8: Results of navigation 2. Route recorded and route followed with a different initial point.

To carry out these experiments, two Pioneer P3-AT robots have been used with two processors onboard that communicate using a CORBA-based architecture where they interchange the necessary information. It is important to design an application

where the different robots can share the necessary information in an easy and quick way due to the fact that the follower robot has to use continuously the database that the leader one is computing. An additional processor has been added to the architecture to carry out some calculations to reduce the computational cost of the processes in the robots.

On fig. 9, the localization shows a correct evolution, despite the visual aliasing effect in such office environments, and the robot recovers correctly of some errors in localization (such as those in images 100 and 170). Also, the probability begins with quite low value (the robot is far from the route). Then, it tends to increase when the robot approaches to the straight line and decreases again in the turnings.

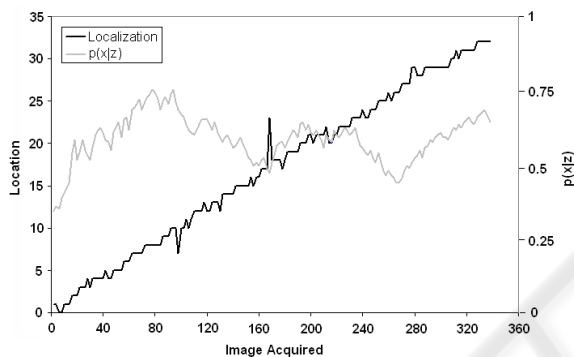


Figure 9: Localizations and final probability during navigation with the route of the figure 7.

6 CONCLUSIONS

In this paper, an appearance-based multi-robot following-route scheme is presented. The proposed solution uses low resolution images from a conventional video camera and PCA techniques to extract the most relevant information along the environment. To allow a new robot can follow the route that another robot is recording at the same time, an incremental PCA algorithm is employed.

The objective of the work is that other robots can follow this route from a distance (as in space or in time). To do it, a probabilistic algorithm has been implemented to calculate their current position among those that the leader has stored, and a controller has been implemented, also based on the appearance of the scenes, to calculate the linear and turning speeds of the robot. Also, a clustering method has been implemented to estimate the initial position of the robot in a robust way.

Some experiments have been carried out with two Pioneer 3-AT robots using a CORBA-based architecture for communication. These experiments show how the process employed allows following a route in an accurate and robust way.

We are now working in other control methods to reduce the error during the navigation, studying the effects of illumination changes and occlusions more accurately. Also, other techniques to compress the information are being analysed to achieve a higher speed of the follower robots. At last, more complicated ways of building a map are being evaluated so that the robot can find the route and follow it although its initial position is far from this route.

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