

# GPC AND NEURAL GENERALIZED PREDICTIVE CONTROL

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Abstract: An efficient implementation of Model Predictive Control (MPC) using a multilayer feed forward network as the plants linear model is presented. This paper presents a comparison between the Generalized Predictive Control and Neural Generalized Predictive Control with Newton-Raphson as minimization algorithm. Three different linear models are taken and their performances are tested. Simulation result shows the effect of neural network on Generalized Predictive Control for linear systems. The performance comparison of these system configurations has been given in terms of ISE and IAE.

## 1 INTRODUCTION

Model predictive control (MPC) has found a wide range of applications in the process, chemical, food processing, automotive, aerospace, metallurgy, and pulp and paper industries. (Qin and Badgwell, 2003; Yu, Yu and Gomm, 2006; Lawrynczuk, 2007). In recent years, the requirements for the quality of automatic control in the process industries increased significantly due to the increased complexity of the plants and sharper specifications of product quality. As a result, computer models that are computationally expensive became applicable even to rather complex problems. Intelligent and model based control techniques were developed to obtain tighter control for such applications. Neural network techniques has been found to be particularly useful for modeling and controlling highly uncertain nonlinear and complex systems. (Noorgard, Ravn, Poulsen and Hansen, 2000). The Model Predictive Control (MPC) techniques found to be very effective in control systems. MPC was introduced successfully in several industrial plants. Some of the most popular MPC algorithms that found a wide acceptance in industry are Dynamic Matrix Control (DMC), Model Algorithmic Control (MAC), Predictive Functional Control (PFC), Extended Prediction Self Adaptive Control (EPSAC), Extended Horizon Adaptive Control (EHAC) and Generalized Predictive Control (GPC). (Morari and Lee, 1999, Rossiter, 2003). In this work, comparison between GPC and Neural GPC has been carried out

for linear systems. The results show the efficacy of NGPC for such plants.

## 2 GENERALIZED PREDICTIVE CONTROL

The GPC method was proposed by Clarke et. al. (Clarke, Mohatadi and Tuffs, 1987) and has become one of the most popular MPC methods both in industry and academia.

The basic idea of GPC is to calculate a sequence of future control signals in such a way that it minimizes a multistage cost function defined over a prediction horizon. The index to be optimized is the expectation of a quadratic function measuring the distance between the predicted system output and some reference sequence over the horizon plus a quadratic function measuring the control effort. The GPC scheme consists of the plant to be controlled, a reference model that specifies the desired performance of the plant, a linear model of the plant, and the Cost Function Minimization (CFM) algorithm that determines the input needed to produce the plant's desired performance. The GPC system starts with the input signal,  $r(t)$ , which is presented to the reference model. This model produces a tracking reference signal,  $w(t)$  that is used as an input to the CFM block. The CFM algorithm produces an output, which is used as an input to the plant. Between samples, the CFM

algorithm uses this model to calculate the next control input,  $u(t+1)$ , from predictions of the response from the plant's model. Once the cost function is minimized, this input is passed to the plant.

### 3 NEURAL GENERALIZED PREDICTIVE CONTROL

The ability of the GPC to make accurate predictions can be enhanced if a neural network is used to learn the dynamics of the plant instead of standard nonlinear modeling techniques.(Noorgard, Ravn, Poulsen and Hansen, 2000). The selection of the minimization algorithm affects the computational efficiency of the algorithm. In this work Newton-Raphson method is used as the optimization algorithm. The main cost of the Newton-Raphson algorithm is in the calculation of the Hessian, but even with this overhead the low iteration numbers make Newton-Raphson a faster algorithm for real-time control. (Soloway, 1996). The Neural Generalized Predictive Control (NGPC) system can be seen in Fig. 1. It consists of four components, the plant to be controlled, a reference model that specifies the desired performance of the plant, a neural network that models the plant, and the Cost Function Minimization (CFM) algorithm that determines the input needed to produce the plant's desired performance. The NGPC algorithm consists of the CFM block and the neural net block.

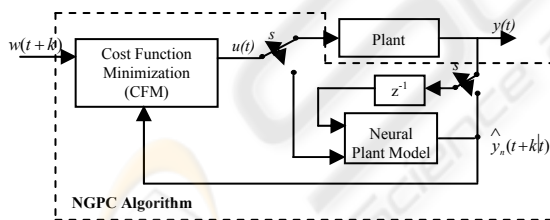


Figure 1: Block Diagram of NGPC System.

The NGPC system starts with the input signal,  $r(t)$ , which is presented to the reference model. This model produces a tracking reference signal,  $w(t+k)$ , that is used as an input to the CFM block. The CFM algorithm produces an output that is either used as an input to the plant or the plant's model. The double pole double throw switch,  $S$ , is set to the plant when the CFM algorithm has solved for the best input,  $u(t)$ , that will minimize a specified cost function. Between samples, the switch is set to the plant's model where the CFM algorithm uses this

model to calculate the next control input,  $u(t+1)$ , from predictions of the response from the plant's model. Once the cost function is minimized, this input is passed to the plant. The computational performance of a GPC implementation is largely based on the minimization algorithm chosen for the CFM block. Models using neural networks have been shown to have the capability to capture nonlinear dynamics. Improved predictions affect rise time, over-shoot, and the energy content of the control signal.

#### 3.1 Formulation of NGPC

##### 3.1.1 Cost Function

As mentioned earlier, the NGPC algorithm (Soloway, 1996) is based on minimizing a cost function over a finite prediction horizon. The cost function of interest to this application is

$$J(N_1, N_2, N_u) = \sum_{j=N_1}^{N_2} \delta(j) [\hat{y}(t+j|t) - u(t+j)]^2 + \sum_{j=1}^{N_u} \lambda(j) [\Delta u(t+j-1)]^2 \quad (1)$$

$N_1$  = Minimum Costing Prediction Horizon

$N_2$  = Maximum Costing Prediction Horizon

$N_u$  = Length of Control Horizon

$\hat{y}(t+k|t)$  = Predicted Output from Neural;

Network,  $u(t+k|t)$  = Manipulated Input

$w(t+k)$  = Reference Trajectory

$\delta$  and  $\lambda$  = Weighing Factor

When this cost function is minimized, a control input that meets the constraints is generated that allows the plant to track the reference trajectory within some tolerance. There are four tuning parameters in the cost function,  $N_1$ ,  $N_2$ ,  $N_u$ , and  $\lambda$ . The predictions of the plant will run from  $N_1$  to  $N_2$  future time steps. The bound on the control horizon is  $N_u$ . The only constraint on the values of  $N_u$  and  $N_1$  is that these bounds must be less than or equal to  $N_2$ . The second summation contains a weighting factor,  $\lambda$  that is introduced to control the balance between the first two summations. The weighting factor acts as a damper on the predicted  $u(n+1)$ .

##### 3.1.2 Cost Function Minimization Algorithm

The objective of the CFM algorithm is to minimize  $J$  in Equation (1) with respect to  $[u(n+1), u(n+2), \dots, u(n+N_u)]^T$ , denoted as  $U$ . This is accomplished by setting the Jacobian of Equation (1) to zero and solving for  $U$ . With Newton-Rhapson used as the CFM algorithm,  $J$  is minimized iteratively to

determine the best  $U$ . An iterative process yields intermediate values for  $J$  denoted  $J(k)$ . For each iteration of  $J(k)$  an intermediate control input vector is also generated and is denoted as:

$$U(k) = \begin{bmatrix} u(t+1) \\ u(t+2) \\ \vdots \\ u(t+N_u) \end{bmatrix} \quad k=1, \dots, N_u \quad (2)$$

Using this Newton-Raphson update rule,  $U(k+1)$  is

$$U(k+1) = U(k) - \left( \frac{\partial^2 J}{\partial U^2}(k) \right)^{-1} \frac{\partial J}{\partial U}(k)'$$

where  $f(x) = \frac{\partial J}{\partial U}$  (3)

where the Jacobian is denoted as

$$\frac{\partial J}{\partial U}(k) = \begin{bmatrix} \frac{\partial J}{\partial u(t+1)} \\ \vdots \\ \frac{\partial J}{\partial u(t+N_u)} \end{bmatrix} \quad (4)$$

and the Hessian as

$$\frac{\partial^2 J}{\partial U^2}(k) = \begin{bmatrix} \frac{\partial^2 J}{\partial u(t+1)^2} & \dots & \frac{\partial^2 J}{\partial u(t+1)\partial u(t+N_u)} \\ \vdots & \ddots & \vdots \\ \frac{\partial^2 J}{\partial u(t+N_u)\partial u(t+1)} & \dots & \frac{\partial^2 J}{\partial u(t+N_u)^2} \end{bmatrix} \quad (5)$$

The each element of the Jacobian is calculated by partially differentiating (4) with respect to vector  $U$ .

### 3.1.3 Neural Network Architecture

In NGPC the model of the plant is a neural network. This neural model is constructed and trained using MATLAB Neural Network System Identification Toolbox commands and Control System Design Toolkit (Noorgard, Ravn, Poulsen and Hansen, 2000).

The output of trained neural network is used as the predicted output of the plant. This predicted output is used in the Cost Function Minimization Algorithm. If  $y_n(t)$  is the neural network's output then it is nothing but plant's predicted output  $\hat{y}_n(t+k|t)$ .

The initial training of the neural network is typically done off-line before control is attempted

### 3.1.4 Prediction using Neural Network

The NGPC algorithm uses the output of the plant's model to predict the plant's dynamics to an arbitrary input from the current time,  $t$ , to some future time,  $t+k$ .

## 4 SIMULATION RESULTS

The objective of this study is to show how GPC and NGPC implementation can cope with linear systems. GPC is applied to the systems with changes in system order. The Neural based GPC is implemented using MATLAB Neural Network Based System Design Toolbox (Noorgard, Ravn, Poulsen and Hansen, 2000).

### 4.1 GPC and NGPC for Linear Systems

The GPC and NGPC algorithm was applied to the different linear models with varying system for simulation purpose. For all the systems Prediction Horizon  $N_1=1$ ,  $N_2=7$  and Control Horizon ( $N_u$ ) is 2 have been considered. The weighing factor  $\lambda$  for control signal is kept to 0.3 and  $\delta$  for reference trajectory is set to 0. The same controller setting is used for all the systems simulation. The following simulation results are obtained showing the plant output when GPC and NGPC are applied. Also the required control action for different systems is shown.

**System I.** The GPC and NGPC algorithms are applied to a second order system (6). Fig. 2 shows the plant output with GPC and NGPC. Fig. 3 shows the control efforts taken by both controllers.

$$G(s) = \frac{1}{1+10s+40s^2} \quad (6)$$

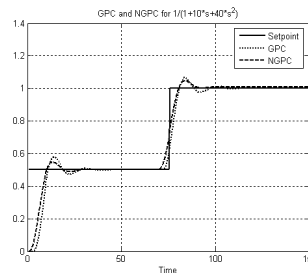


Figure 2: System I Output using GPC and NGPC.

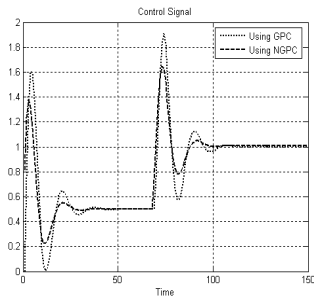


Figure 3: Control Signal for System I.

**System II.** A simple first order system (7) is controlled. Fig. 4 and Fig. 5 show the system output and control signal.

$$G(s) = \frac{1}{1+10s} \tag{7}$$

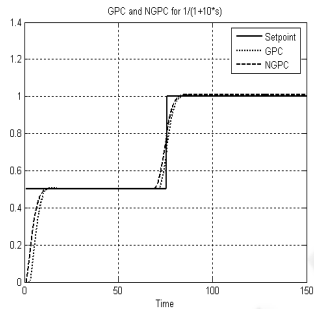


Figure 4: System II Output using GPC and NGPC.

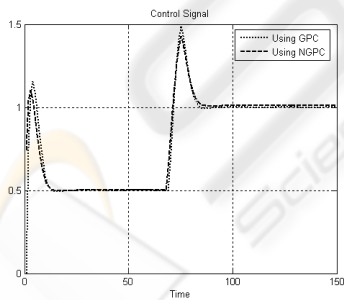


Figure 5: Control Signal for System II.

**System III.** A second order system (8) is controlled using GPC and NGPC. Fig.6 and Fig.7 Show the predicted output and control signal.

$$G(s) = \frac{1}{10s(1+2.5s)} \tag{8}$$

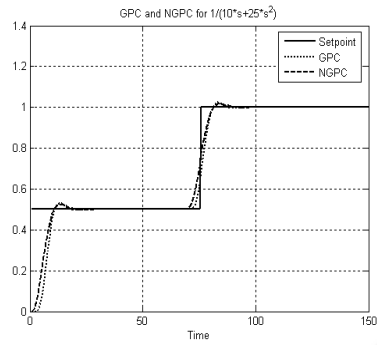


Figure 6: System III Output using GPC and NGPC.

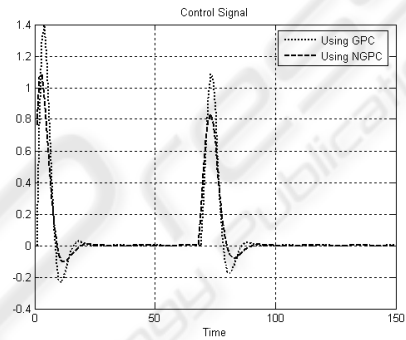


Figure 7: Control Signal for System III.

Initially systems were trained using Levenberg-Marquardt learning algorithm. Fig. 8 shows input data applied to the neural network for offline training purpose and corresponding neural network output.

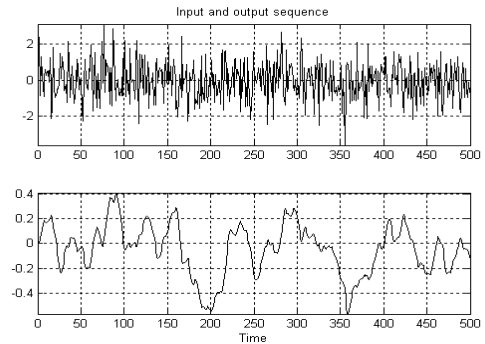


Figure 8: Input and output data for NN.

Performance evaluation of both the controller is carried out using ISE and IAE criteria. Table 1 gives ISE and IAE values for both GPC and NGPC implementation for all the linear systems considered. It was observed that for each system ISE and IAE using NGPC is smaller or equal to GPC.

Table 1: ISE and IAE Performance Comparison of GPC and NGPC for Linear System.

| Systems | Setpoint | GPC    |        | NGPC   |        |
|---------|----------|--------|--------|--------|--------|
|         |          | ISE    | IAE    | ISE    | IAE    |
| I       | 0.5      | 1.827  | 4.4107 | 1.6055 | 3.6351 |
|         | 1        | 0.2567 | 1.4492 | 0.1186 | 1.4312 |
| II      | 0.5      | 1.1803 | 3.217  | 0.7896 | 2.6894 |
|         | 1        | 0.1311 | 0.767  | 0.063  | 1.017  |
| III     | 0.5      | 1.4639 | 3.7625 | 1.1021 | 3.3424 |
|         | 1        | 0.1759 | 0.9065 | 0.0957 | 0.7062 |

## 5 CONCLUSIONS

In this paper a comparison between GPC and NGPC is carried out for linear systems. The performance of NGPC is better than GPC in terms of ISE and IAE Performance index.

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