# Improved Binary Elk Herd Optimizer with Fitness Balance Distance for Feature Selection Using Gene Expression Data

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Keywords: Feature Selection, Optimization, Elk Herd Optimiser, Distance Balance Mechanism.

Abstract: This research paper introduces an enhanced version of the Binary Elk Herd Optimizer (BEHO), integrated with a Fitness Distance Balance (FDB) mechanism called FDB-BEHO, tailored for high-dimensional optimization tasks. This study evaluates the performance of FDB-BEHO across multiple gene expression datasets, focusing on feature selection in bioinformatics—a domain characterized by complex, high-dimensional data. The FDB mechanism is designed to prevent premature convergence by maintaining an optimal balance between exploration and exploitation, utilizing a diversity measure that adjusts dynamically based on the fitness-distance correlation among solutions. Comparative analyses demonstrate that FDB-BEHO surpasses traditional metaheuristic algorithms in fitness values and classification accuracy and reduces the number of selected features, thereby enhancing model simplicity and interpretability. These results validate the effectiveness of FDB-BEHO in navigating complex solution spaces efficiently and underscore its potential applicability in other domains requiring robust feature selection capabilities. The study's findings suggest that incorporating diversity-enhancing mechanisms like FDB can significantly improve the performance of binary optimization algorithms, offering promising directions for future research in optimization technology.

# 1 INTRODUCTION

In medical research, DNA microarray technology has revolutionized our ability to analyze gene expression data, enabling the simultaneous observation of thousands of genes in a single experiment. However, this advancement also presents a significant challenge: the curse of dimensionality. With such vast amounts of data, it becomes crucial to identify and select the most relevant features—genes that significantly contribute to accurate disease prediction and classification. Feature selection (FS) methods are pivotal in addressing this challenge, allowing researchers to eliminate irrelevant or redundant genes, thereby enhancing the performance of predictive models and reducing computational complexity (Zebari et al., 2020).

In recent years, the importance of FS has been underscored in various studies focused on cancer prediction (Haq et al., 2021), where identifying key genetic markers is essential for early diagnosis and treatment planning. Traditional FS methods, such as filter, wrapper, and embedded approaches, have been widely applied, each with its strengths and limitations (Venkatesh and Anuradha, 2019). Filters are independent of the learning algorithm but may overlook interactions between features (Bommert et al., 2022); wrappers are more accurate but computationally expensive (Maldonado and Weber, 2009); and embedded methods integrate FS within the model training process, offering a balanced approach (Wang et al., 2015).

Given the complexity and non-linearity of gene expression data, metaheuristic algorithms have emerged as powerful tools for FS (Dokeroglu et al., 2022). Inspired by natural, biological, or social processes, these optimization approaches are designed to solve complex problems efficiently (Ouertani et al., 2022a; Oueslati et al., 2024). Metaheuristics excels at exploring vast search spaces and avoiding suboptimal solutions, unlike traditional optimization methods, which may be constrained by linearity or continuity requirements (Ouertani et al., 2022b). Com-

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Ouertani, M. W., Oueslati, R. and Manita, G.

Improved Binary Elk Herd Optimizer with Fitness Balance Distance for Feature Selection Using Gene Expression Data. DOI: 10.5220/0013367600003890

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In Proceedings of the 17th International Conference on Agents and Artificial Intelligence (ICAART 2025) - Volume 2, pages 786-797 ISBN: 978-989-758-737-5; ISSN: 2184-433X

mon metaheuristics include evolutionary algorithms (Srinivas and Patnaik, 1994) such as Artificial Bee Colony (ABC) (Karaboga and Basturk, 2007), Genetic Algorithm (GA) (Holland, 1992), and Differential Evolution (DE) (Qin et al., 2008). Swarmbased optimization methods such as Elk Herd Optimizer (EHO) (Al-Betar et al., 2024), Particle Swarm Optimization (PSO) (Kennedy and Eberhart, 1995), and Social Spider Algorithm (SSA) (Mirjalili et al., 2017) have proven effective in various applications. Additionally, human-inspired metaheuristics such as Teaching-Learning Based Optimization (TLBO) (Rao et al., 2011), Soccer League Competition (SLC) (Moosavian and Roodsari, 2014), and Brain Storm Optimization (BSO) (Shi, 2011) leverage social behaviors and cognitive processes for optimization. Finally, physics-based metaheuristics such as Simulated Annealing (SA) (Bertsimas and Tsitsiklis, 1993), Atom Search Optimization (ASO) (Zhao et al., 2019), and Equilibrium Optimizer (EO) (Faramarzi et al., 2020) draw inspiration from physical phenomena like thermodynamics and gravitational forces to guide the search for optimal solutions. Their primary advantages lie in their flexibility and adaptability, making them suitable for various problems, particularly combinatorial optimization challenges. However, they can be computationally intensive and do not guarantee globally optimal solutions, often requiring careful parameter tuning to balance solution quality and computational cost (Nssibi et al., 2024).

In order to address the inherent challenges of gene expression data analysis (Nssibi et al., 2023) and as the field continues to evolve, the application of advanced metaheuristics in FS not only enhances model accuracy but also offers valuable insights into complex underlying processes, paving the way for more targeted and effective decision-making strategies across various domains in bioinformatics (Saeys et al., 2007). This study introduces an enhanced version of the Binary Elk Herd Optimizer (BEHO), named FDB-BEHO, which incorporates the Fitness Distance Balance (FDB) mechanism to overcome premature convergence and maintain an optimal balance between exploration and exploitation. The proposed algorithm is specifically designed to minimize the number of selected features, making it well-suited for addressing high-dimensional optimization challenges effectively. To evaluate its effectiveness, FDB-BEHO is tested on nine benchmark biological datasets for feature selection. Its performance is compared against state-of-the-art metaheuristic algorithms using metrics such as fitness values, classification accuracy, and feature selection efficiency.

The main objectives and contributions of this

work are as follows:

- Introduction of the Binary EHO (BEHO): A novel adaptation of the EHO algorithm tailored for feature selection problems. This binary variant enables the direct application of EHO in solving discrete optimization challenges associated with FS.
- Improvement of BEHO with the FDB Mechanism: A further enhancement of BEHO, incorporating the FDB mechanism to address issues of premature convergence. This improvement ensures a more effective balance between exploration and exploitation. The enhanced algorithm dynamically adjusts diversity to maintain robust performance across varying optimization landscapes.
- Evaluation of FDB-BEHO on gene expression data for FS: Assess the performance of the proposed FDB-BEHO algorithm on nine benchmark biological datasets for FS. The evaluation involves a comparative analysis with other state-of-the-art metaheuristics to validate its efficacy and robustness.

The remainder of this paper is structured as follows: Section 2 provides a detailed overview of metaheuristic optimization in feature selection, highlighting the effectiveness of various algorithms in managing high-dimensional data. Section 3 introduces the proposed Binary Elk Herd Optimizer (Binary EHO) and its enhancement with the Fitness Distance Balance (FDB) mechanism, including the technical details of its implementation. Section 4 presents the experimental setup and the results of applying the proposed method to gene expression datasets, comparing its performance with other state-of-the-art algorithms. Finally, Section 5 concludes the paper by discussing the findings, their implications for feature selection in bioinformatics, and potential avenues for future research.

# 2 METAHEURISTIC OPTIMIZATION IN FEATURE SELECTION

In this section, we explore the role of metaheuristic optimization in feature selection, offering a comprehensive overview of various algorithms and their successful applications in addressing the challenges of high-dimensional gene expression data.

In (Sönmez et al., 2021), the study explores the use of hybrid methods combining Genetic Algorithms (GA) with Support Vector Machines (SVM) and k-Nearest Neighbors (KNN) for feature selection and classification of gene expression datasets. The authors propose enhancing the GA through the integration of filter methods such as Pearson's correlation coefficient, Relief-F, and mutual information. The study evaluates these methods across eight gene expression datasets, primarily related to cancer classification. The proposed GA-SVM and GA-KNN methods demonstrate superior accuracy compared to traditional approaches, highlighting the effectiveness of hybrid techniques in reducing the dimensionality of high-throughput data while maintaining or improving classification accuracy. The research emphasizes the importance of hybrid methods in managing the computational complexity of large gene expression datasets and improving predictive performance in medical applications, particularly in cancer diagnosis and subtype classification.

Qin et al. proposed a two-stage feature selection framework tailored to classify high-dimensional gene expression data, utilizing an improved Salp Swarm Algorithm (SSA) (Qin et al., 2022). The first stage combines Weighted Gene Co-expression Network Analysis (WGCNA), Random Forest (RF), and Max-Relevance and Min-Redundancy (mRMR) to initially reduce the feature space by selecting the most relevant and non-redundant genes. In the second stage, the improved binary SSA is employed to refine the feature set further, ensuring a balance between classification accuracy and the number of selected features. The framework was tested across ten gene expression datasets and outperformed other intelligent optimization algorithms like PSO, GWO, and WOA. The results demonstrated that this method could achieve high classification accuracy with fewer selected features, making it a robust solution for gene expression data classification in cancer diagnosis.

In (Alzaqebah et al., 2021), Alzaqebah et al. proposed a Memory-Based Cuckoo Search (MBCS) algorithm for feature selection in gene expression datasets, particularly focusing on cancer prediction. The study addresses the challenges of high-dimensionality and feature redundancy in microarray data, which can hinder accurate classification. The MBCS algorithm enhances the traditional Cuckoo Search Algorithm (Gandomi et al., 2013) by incorporating a memory mechanism that records the best solutions found during the search process. This memory helps the algorithm avoid re-exploring suboptimal areas and focuses on promising regions of the search space. The study tested the algorithm on twelve different microarray datasets and found that MBCS outperformed other algorithms, such as Genetic Algorithms (GA), Particle Swarm Optimization (PSO), and Gravitational Search Algorithm (GSA), in terms of classification accuracy and the number of selected features. The results indicate that MBCS is particularly effective in reducing the dimensionality of the data while maintaining or improving the accuracy of cancer predictions.

Qu et al. introduced an improved Harris Hawks Optimization algorithm, tailored explicitly for feature selection in gene expression data, called the Variable Neighborhood Learning Harris Hawks Optimizer (VNLHHO) (Ou et al., 2021). This approach was designed to enhance the global exploration and local exploitation capabilities of the standard Harris Hawks Optimizer (HHO). The VNLHHO incorporates a dynamic neighborhood learning strategy and mutation operations to increase population diversity and prevent the algorithm from falling into local optima. The effectiveness of VNLHHO was validated across eight cancer gene expression datasets, demonstrating superior classification accuracy and convergence speed compared to traditional algorithms like PSO, GA, and the original HHO. The results showed that VNLHHO not only improved classification performance but also effectively reduced the number of selected features, making it a powerful tool for highdimensional biomedical data analysis.

# **3 PROPOSED APPROACH**

This section presents the proposed approach, which utilizes the Elk Herd Optimizer (EHO) (Al-Betar et al., 2024) as the core algorithm for feature selection in high-dimensional gene expression data. The approach is systematically organized into three main components: (i) Overview of EHO: We begin by introducing the EHO algorithm and highlighting its distinctive characteristics that make it suitable for complex optimization tasks, (ii) Transformation to Binary EHO: Next, we describe the adaptation of EHO into a binary format (Binary EHO), specifically tailored to meet the unique demands of feature selection problems, and (iii) Integration of Fitness Distance Balance (FDB): Finally, we incorporate the Fitness Distance Balance (FDB) mechanism into Binary EHO, significantly enhancing its capability to maintain a robust balance between exploration and exploitation while identifying optimal feature subsets. This structured approach ensures a comprehensive framework for addressing the challenges of feature selection in highdimensional datasets.

#### 3.1 Elk Herd Optimizer Overview

The Elk Herd Optimizer (EHO) is a novel metaheuristic algorithm inspired by the breeding behavior of elk herds. It mimics the seasonal dynamics within the herd, where more muscular bulls lead larger groups during the rutting season, and new solutions are generated during the calving season. This approach balances exploration and exploitation in optimization tasks, making EHO an effective tool for solving complex problems. Its design is particularly suited for navigating challenging search spaces and finding optimal solutions efficiently. The EHO is designed to simulate the natural dynamics of elk herds through a sequence of critical phases. It begins with the initialization of the population and the problem parameters. The algorithm then enters the rutting season, dividing the population into families led by the fittest bulls. In the calving season, these families produce new solutions based on the characteristics of the bull and its harems. Finally, during the selection season, all solutions are evaluated, and the fittest are selected to form the next generation, with this process repeating until the algorithm converges or the iteration limit is reached. The steps of the EHO are as follows :

1. Initialization: During the initialization phase of the EHO, the algorithm begins by setting up the population and defining the problem-specific parameters. The primary elements to initialize are the elk herd size (*EHS*), the bull rate (*Br*), and the search space boundaries. The elk herd *EH* is initialized as a matrix of size  $n \times$  EHS, where n is the problem's dimensionality, and each element in the matrix represents a potential solution (elk). Mathematically, each solution  $x_j$  in the population is generated within the defined search space boundaries using Equation 1:

$$x_i^i = \mathbf{lb}_i + (\mathbf{ub}_i - \mathbf{lb}_i) \times U(0, 1) \tag{1}$$

where  $x_i^i$  represents the *i*-th attribute of the *j*-th solution,  $lb_i$  and  $ub_i$  are the lower and upper bounds for the *i*-th attribute, and U(0,1) is a uniformly distributed random number between 0 and 1. The fitness of each solution is then calculated using the objective function f(x), and the solutions are sorted in ascending order based on their fitness values. This initial setup prepares the elk herd for the subsequent phases of the algorithm.

2. Generating the initial Elk Herd Solutions: In the second step, the algorithm focuses on creating the initial solutions population, representing the elk herd. After defining the problem-specific parameters and initializing the population matrix *EH* in the first step, this phase involves assigning fitness

values to each solution and organizing the herd structure. The elk herd **EH** is generated as a matrix of size  $n \times \text{EHS}$ , where each row corresponds to a potential solution in the search space as presented in Equation 2.

$$\mathbf{EH} = \begin{bmatrix} x_1^1 & x_2^1 & \cdots & x_n^1 \\ x_1^2 & x_2^2 & \cdots & x_n^2 \\ \vdots & \vdots & \cdots & \vdots \\ x_1^{EHS} & x_2^{EHS} & \cdots & x_n^{EHS} \end{bmatrix}$$
(2)

Once the initial population is generated, the fitness of each solution is evaluated using the objective function f(x). The herd is then sorted in ascending order of fitness, ensuring that the best solutions (strongest elks) are positioned at the top. This ordered structure sets the foundation for the subsequent rutting season phase, where the population will be divided into families.

3. Rutting season: In the third step, the EHO algorithm divides the initial population into families, with each family led by a bull (the fittest individual). The division is based on the fitness of the bulls, reflecting the natural behavior where stronger bulls lead larger groups. First, the algorithm determines the number of bulls B in the population using the bull rate Br and the elk herd size *EHS* as shown in Equation 3. :

$$B = Br \times EHS \tag{3}$$

where *B* is the number of bulls, *Br* is the bull rate, and *EHS* is the total population size. The top *B* individuals, based on their fitness values, are selected as bulls. Next, the bulls compete to form families, each consisting of a bull and its assigned harems (followers). The assignment of harems to each bull is done using a roulette-wheel selection process, where the probability  $p_j$  of a bull *j* attracting a harem is proportional to its fitness presented in Equation 4:

$$p_j = \frac{f(x_j)}{\sum_{k=1}^B f(x_k)} \tag{4}$$

Here,  $f(x_j)$  is the fitness of the *j*-th bull, and the sum in the denominator is the total fitness of all bulls. The roulette-wheel selection ensures that bulls with higher fitness are more likely to lead more harems. Once the harems are assigned, each bull leads its family, with the size of each family reflecting the strength of the bull. This structured division sets the stage for the calving season, where new solutions (calves) will be generated based on the bulls' characteristics and harems.

4. Calving season: In the fourth step, the EHO algorithm focuses on generating new solutions (calves) within each family based on the genetic traits of the bull (leader) and its harems (followers). This process mimics the natural reproduction process in elk herds, where the offspring inherit characteristics from both parents, promoting diversity within the population. For each family, new solutions  $x_j^i(t+1)$  are generated by combining attributes from the bull  $x_j$  and its harems  $x_j^i(t)$ . If the calf's index matches that of its bull father, the new solution is generated using Equation 5:

$$x_{j}^{i}(t+1) = x_{j}^{i}(t) + \alpha \cdot (x_{k}^{i}(t) - x_{j}^{i}(t))$$
 (5)

where  $\alpha$  is a random number between 0 and 1, and  $x_k^i(t)$  is a randomly selected attribute from the current population. This equation ensures that the new solution is influenced primarily by the bull, with some variation introduced by the random selection from the herd. If the calf's index matches that of its mother harem, the new solution is created by combining the attributes of both the mother and the bull, using Equation 6:

$$x_{j}^{i}(t+1) = x_{j}^{i}(t) + \beta \cdot (x_{hj}^{i}(t) - x_{j}^{i}(t)) + \gamma \cdot (x_{r}^{i}(t) - x_{j}^{i}(t))$$
(6)

Here,  $\beta$  and  $\gamma$  are random numbers in the range [0, 2],  $x_{hj}^i(t)$  represents the bull's attributes, and  $x_r^i(t)$  is a random attribute from another bull. This equation allows the calf to inherit traits from both parents, with additional diversity introduced by the random selection. This calving process continues for all families, producing a new generation of solutions that inherit their predecessors' strengths while introducing new variations, which is crucial for the algorithm's exploration and exploitation capabilities in the search space.

5. Selection season: In the fifth step, the EHO algorithm consolidates the newly generated solutions (calves) with the existing population of bulls and harems to form a unified herd. This phase aims to evaluate the fitness of all individuals in this combined population and select the best solutions to carry forward to the next generation. First, the bulls, harems, and newly generated calves are merged into a single matrix,  $EH_{temp}$ . Each individual's fitness in  $EH_{temp}$  is evaluated using the objective function, and the entire population is sorted in ascending order based on fitness values. From this sorted population, the top EHS individuals, where EHS is the elk herd size, are selected to form the new population for the next iteration. This selection process ensures that only the fittest individuals, whether they are bulls, harems, or calves, are retained in the herd. This method



Figure 1: Flowchart of the Elk Herd Optimizer.

of selection is akin to the  $\mu + \lambda$  selection strategy commonly used in evolutionary algorithms, where both parents (bulls and harems) and offspring (calves) compete equally for survival. By continuously selecting the fittest individuals, the algorithm iteratively refines the population, improving the overall fitness of the herd with each cycle. This selection process repeats until the termination criteria, such as a maximum number of iterations or convergence to an optimal solution, are met.

The flowchart and pseudocode of the EHO are presented in Figure 1 and Algorithm 1, respectively.

#### **3.2 Binary Elk Herd Optimizer**

Transforming the EHO into a Binary EHO is essential for adapting the algorithm to feature selection tasks, which require decisions to be made in a binary search space. In feature selection, each candidate solution is represented as a binary vector where each element indicates whether a particular feature is included (1) or excluded (0). The transformation of EHO to handle binary vectors involves the following technical steps: Algorithm 1: Elk Herd Optimizer (EHO) Algorithm.

- 1: **Input:** Population size (EHS), Bull rate (Br), Maximum iterations (MaxIter)
- 2: **Output:** Best solution found
- 3: Initialize population *EH* with *EHS* solutions randomly within the search space
- 4: Evaluate the fitness of each solution in *EH*
- 5: Sort EH based on fitness in ascending order
- 6: for iter = 1 to MaxIter do
- 7: Determine number of bulls  $B = [Br \times EHS]$
- 8: Select the top *B* solutions as bulls from *EH*
- 9: Assign harems to each bull using roulettewheel selection based on fitness
- 10: **for** each family (bull and its harems) **do**
- 11: **if** index matches bull **then**

12: 
$$x_{\text{new}} = x_{\text{bull}} + \alpha \times (x_{\text{random}} - x_{\text{bull}})$$

13: else

14:  $x_{\text{new}} = x_{\text{harem}} + \beta \times (x_{\text{bull}} - x_{\text{harem}}) + \gamma \times (x_{\text{random\_bull}} - x_{\text{harem}})$ 

- 15: end if
- 16: end for
- 17: Combine bulls, harems, and calves into  $EH_{temp}$
- 18: Evaluate fitness of all solutions in  $EH_{temp}$
- 19: Sort  $EH_{\text{temp}}$  based on fitness in ascending order
- 20: Select the top *EHS* solutions from  $EH_{\text{temp}}$  to form the new population *EH*

21: end for

- 22: Return the best solution in EH
- 1. Binary Representation: Instead of representing solutions as continuous vectors, each solution is now a binary vector  $\mathbf{x} = [x_1, x_2, \dots, x_n]$ , where  $x_i \in \{0, 1\}$  for each feature *i*. This change allows the algorithm to directly address feature selection by determining whether each feature should be included in the model.
- 2. Position Update with Transfer Functions: The core challenge in adapting EHO to a binary format lies in converting the continuous position updates, typical in EHO, to binary updates. This is achieved using transfer functions (Equations 7,8) (Mirjalili and Lewis, 2013; Nssibi et al., 2021). After the continuous update equation is computed for each element  $x_j^i$  of the solution vector, a transfer function TF(x) is applied to convert this continuous value into a probability. Common transfer functions include:
  - Sigmoid Function (S-shaped):

$$TF(x) = \frac{1}{1 + e^{-x}}$$
 (7)

• V-shaped Function:

$$TF(x) = |\tanh(x)| \tag{8}$$

The output of these functions lies between 0 and 1 and represents the probability that a particular feature will switch its state (from 0 to 1 or vice versa).

3. Binary Decision-Making: Once the probability  $P(x_j^i)$  is determined using the transfer function, the next step is to convert this probability into a binary decision. This is done by comparing the probability with a random number rand() generated uniformly between 0 and 1 as presented in Equation 9:

$$x_j^i = \begin{cases} 1, & \text{if } P(x_j^i) \ge \text{rand}() \\ 0, & \text{otherwise} \end{cases}$$
(9)

This comparison ensures that each feature's binary state is updated based on the likelihood calculated through the transfer function.

4. Fitness Evaluation: After updating the binary vectors, the fitness of each solution is evaluated. The fitness function typically balances the trade-off between maximizing classification accuracy (using a classifier like k-NN) and minimizing the number of features selected. This ensures that the selected subset is both practical and compact.

By incorporating these steps, the Binary EHO can effectively navigate binary search spaces, making it highly suitable for feature selection tasks. Transfer functions are critical in this transformation, as they bridge the gap between continuous optimization strategies and the discrete nature of feature selection problems, enabling the algorithm to retain its exploration and exploitation capabilities in a binary context.

#### 3.3 Fitness Distance Balance BEHO

Integrating the Fitness Distance Balance (FDB) (Kahraman et al., 2020) mechanism into the BEHO enhances its performance in feature selection by introducing a balance between exploration and exploitation. This mechanism evaluates each solution based not only on its fitness but also on its diversity relative to the best-known solution. Technically, this is achieved by first calculating the Euclidean distance  $D_j$  between each binary solution  $x_j$  and the current best solution Best<sub>current</sub>, using the formula in Equation 10:

$$D_j = \sqrt{\sum_{i=1}^{n} (x_j^i - \text{Best}_{\text{current}}^i)^2}$$
(10)

Next, both the fitness values and the distances are normalized to ensure no single metric dominates as presented in Equations 11 and 12 :

$$F_{\text{norm}}(j) = \frac{F(j) - \min(F)}{\max(F) - \min(F)}$$
(11)

$$D_{\text{norm}}(j) = \frac{D_j - \min(D)}{\max(D) - \min(D)}$$
(12)

These normalized values are then combined into a composite score  $S_j$  that balances fitness and diversity as presented in Equation 13:

$$S_j = \alpha \times F_{\text{norm}}(j) + (1 - \alpha) \times D_{\text{norm}}(j)$$
(13)

This score guides the selection process, with higherscoring solutions more likely to be retained or selected as bulls. Using this composite score, the algorithm avoids premature convergence and maintains a diverse population, which is crucial for effectively exploring the binary search space and identifying optimal feature subsets. This approach significantly enhances the robustness and effectiveness of Binary EHO in feature selection tasks. The complete pseudocode of the FDB-BEHO is presented in Algorithm 2.

Algorithm 2: Binary EHO with Fitness Distance Balance (FDB) Mechanism.

- 1: Initialize population EH as binary vectors
- 2: **for** iter = 1 to MaxIter **do**
- 3: Determine bulls and harems using binary fitness and distance evaluation
- 4: **for** each family **do**
- 5: Calculate continuous updates for positions
- 6: Apply transfer function to convert updates to probabilities
- 7: Update binary positions using the calculated probabilities
- 8: end for
- 9: Calculate distance  $D_j$  for each solution from the best solution
- 10: Normalize fitness and distance values
- 11: Compute composite score  $S_j$ 
  - $\alpha \times F_{\text{norm}}(j) + (1 \alpha) \times D_{\text{norm}}(j)$
- 12: Select the best solutions based on composite scores to form the new population
- 13: **end for**
- 14: **Return** the best binary solution

### **4 EXPERIMENTAL RESULTS**

In this section, we evaluate the performance of the proposed FDB-BEHO across various gene expression datasets. All experiments were conducted using MATLAB R2020a on an Intel Core i5 machine with a 3.3 GHz CPU and 12GB of RAM. Each experiment was repeated 30 times to ensure statistical significance.

#### 4.1 Datasets

We utilized the following nine benchmark biological datasets to assess the effectiveness of the FDB-BEHO: Leukemia (Golub et al., 1999), Prostate\_GE (Singh et al., 2002), Colon (Alon et al., 1999), Lung\_discrete (Bhattacharjee et al., 2001), SMK\_CAN\_187 (Spira et al., 2007), Lymphoma (Alizadeh et al., 2000), CLL\_SUB\_111 (Haslinger et al., 2004), Lung (Bhattacharjee et al., 2001), and nci9 (Ross et al., 2000). The details of these datasets, including the number of instances, features, and classes, are summarized in Table 1. The parameters for FDB-BEHO and the comparative metaheuristic algorithms are detailed in Table 2.

Table 1: Summary of Datasets Used in the Experiments.

Dataset	Instances	Features	Classes
CLL_SUB_111	111	11340	3
Colon	62	2000	2
Leukemia	72	7070	2
Lung	203	3312	5
Lung_discrete	73	325	7
Lymphoma	96	4026	9
nci9	60	9712	9
Prostate_GE	102	5966	2
SMK_CAN_187	187	19993	2

Table 2: Parameter Settings for the Algorithms.

Algorithm	Parameter					
EDD DEHO	EHS (Population Size)					
FDB-BEIIO	Br (Break Rate)					
SSA	c1 (leader position update probability)	0.5				
PSO	c1, c2 (acceleration coefficients)	2				
150	$\omega$ (inertia weight)	0.1				
CA	crossover rate					
GA	mutation rate					
FO	α					
EU	β	2				
	$\alpha$ (depth weight)	50				
ASO	$\beta$ (multiplier weight)					
	Vmax (maximum velocity)	6				
All of thom	search agents (bats, wolves, particles,)					
An or them	maximum iterations	200				

### 4.2 Results and Discussion

This section thoroughly examines various datasets, illustrating the performance of the FDB-BEHO optimization algorithm variants compared with established algorithms such as ABC, SSA, PSO, GA, EO, and ASO. The metrics for this comparison encompass fitness values, classification accuracy, the number of selected features, and statistical significance as assessed by the Wilcoxon test.

In Table 3, the analysis of fitness values shows FDB-BEHO-V as a standout performer, consistently achieving the lowest fitness scores on challenging datasets such as CLL\_SUB\_111, colon, and leukaemia. These results demonstrate the algorithm's superior capability in efficiently navigating complex solution spaces to identify highly optimal solutions. Moreover, FDB-BEHO-V exhibits the lowest standard deviations among the compared algorithms, emphasising its stability and reliability. Such consistency is crucial in optimization tasks where dependability and predictability of performance are as crucial as the performance itself.

The narrative continues in Table 4, focusing on classification accuracy. Here, FDB-BEHO-S frequently outperforms FDB-BEHO-V, indicating its enhanced capability in models where higher accuracy is paramount. However, the performance landscape is nuanced, with algorithms like EO and PSO excelling in specific datasets, particularly lung and Prostate\_GE. These observations underline the necessity of adaptive algorithm selection based on specific dataset characteristics, suggesting that no single algorithm uniformly outperforms others across all contexts. This variability also highlights the importance of understanding the underlying data characteristics and choosing algorithms that align well with those characteristics to optimize performance.

Table 5 sheds light on the efficiency of feature selection, a critical metric that affects both the complexity and the computational efficiency of the resulting models. FDB-BEHO-V is particularly adept at reducing the number of features required to achieve high performance, which is evident in its handling of datasets like CLL\_SUB\_111 and colon. By selecting fewer features, FDB-BEHO-V not only simplifies the complexity of the models but also potentially enhances the interpretability of the results, which is invaluable in applications where understanding the algorithm's decision-making process is essential. Moreover, models with fewer features generally train and deploy faster, offering practical advantages in real-time applications. Hence, Figure 2 provides a clearer visualization of the obtained results.

The robustness of these results is further validated in Table 6, where the Wilcoxon test results confirm the statistical significance of the improvements offered by FDB-BEHO-V over other algorithms in most datasets. However, in datasets like lymphoma and nci9, where no significant differences are found, the results suggest that FDB-BEHO-V may not always offer a decisive advantage, indicating potential areas for further algorithmic refinement and improvement.

This detailed analysis underscores FDB-BEHO-V's capabilities to deliver top-tier optimization performance with robust reliability across a range of domains, presenting it as an excellent candidate for tackling complex optimization problems in varied settings. The findings from this investigation are crucial for advancing the development and application of optimization methodologies in both academic research and practical industrial applications, driving innovation and efficiency in this vital field.

## **5** CONCLUSION

This study has meticulously explored the enhancements to the BEHO by integrating the Fitness Distance Balance (FDB) mechanism. The adapted BEHO has been rigorously tested across various gene expression datasets, demonstrating its ability to efficiently and reliably identify optimal solutions. Introducing a binary framework tailored for discrete optimization tasks such as feature selection has shown significant promise, particularly in bioinformatics, where the dimensionality and complexity of data often pose substantial challenges.

The FDB-BEHO variant has consistently outperformed traditional metaheuristic algorithms in terms of fitness values, classification accuracy, and feature selection efficiency. This robust performance underscores the algorithm's refined balance between exploration and exploitation, facilitated by the FDB mechanism, which integrates a diversity measure to prevent premature convergence. The findings from this study advocate for the potential of BEHO in bioinformatics and highlight its adaptability and efficiency in managing high-dimensional datasets.

Looking forward, optimization in highdimensional data analysis presents several avenues for further research. BEHO's adaptability could be explored in other complex optimization scenarios beyond bioinformatics, such as in finance, robotics, and climate modeling, where similar challenges regarding high dimensionality and feature redundancy exist. Future studies could also delve into hybrid approaches combining BEHO with other metaheuristic



(i) SMK\_CAN\_187

Figure 2: Average selected number of features for CLL\_SUB\_111, Colon, Leukemia, Lung, Lung discrete, Lymphoma, nci9, Prostate\_GE, and SMK\_CAN\_187 datasets.

Dataset	Metric	FDB-	FDB-	ABC	SSA	PSO	GA	EO	ASO
		<b>BEHO-V</b>	<b>BEHO-S</b>						
CLL_SUB_111	Best	0,0469	0,0524	0,0948	0,0472	0,0500	0,0499	0,0914	0,0949
	Avg	0,0872	0,1019	0,1646	0,1526	0,1505	0,1458	0,1410	0,1585
	Std	0,0169	0,0223	0,0302	0,0308	0,0387	0,0310	0,0294	0,0326
colon	Best	0,0002	0,0046	0,0045	0,0014	0,0044	0,0045	0,0006	0,0045
	Avg	0,0005	0,0050	0,0047	0,0022	0,0047	0,0047	0,0013	0,0048
	Std	0,0001	0,0004	7,64E-05	0,0003	0,0001	5,18E-05	0,0003	9,09E-05
leukemia	Best	0,0001	0,0048	0,0047	0,0014	0,0046	0,0047	0,0002	0,0047
	Avg	0,0002	0,0049	0,0048	0,0016	0,0047	0,0047	0,0006	0,0048
	Std	6,63E-05	4,03E-05	3,88E-05	0,0001	4,99E-05	2,30E-05	0,0002	5,37E-05
lung	Best	0,0002	0,0047	0,0045	0,0013	0,0044	0,0045	0,0005	0,0046
	Avg	0,0003	0,0048	0,0047	0,0018	0,0046	0,0047	0,0011	0,0047
	Std	0,0001	5,55E-05	5,67E-05	0,0002	7,69E-05	3,39E-05	0,0002	5,64E-05
lung_discrete	Best	0,0002	0,0042	0,0039	0,0012	0,0035	0,0038	0,0008	0,0039
	Avg	0,0004	0,0047	0,0042	0,0019	0,0041	0,0042	0,0014	0,0043
	Std	8,76E-05	0,0002	0,0001	0,0002	0,0002	0,0001	0,0003	0,0002
lymphoma	Best	0,0521	0,05222	0,1086	0,1056	0,1086	0,1087	0,0522	0,1088
	Avg	0,0543	0,09718	0,1088	0,1057	0,1087	0,1088	0,0901	0,1089
	Std	0,0101	0,01807	6,22E-05	7,55E-05	6,83E-05	3,23E-05	0,0234	5,15E-05
nci9	Best	0,0845	0,1651	0,0875	0,0861	0,1698	0,0874	0,0843	0,1698
	Avg	0,1478	0,2244	0,2314	0,2161	0,2217	0,2087	0,2203	0,2120
	Std	0,0348	0,03755	0,0398	0,0342	0,0470	0,0402	0,0429	0,0461
Prostate_GE	Best	0,0003	0,0048	0,0047	0,0015	0,0046	0,0047	0,0006	0,0047
	Avg	0,0006	0,0049	0,0048	0,0020	0,0048	0,0048	0,0015	0,0048
	Std	0,0001	5,71E-05	4,05E-05	0,0003	5,40E-05	3,54E-05	0,0004	7,09E-05
SMK_CAN_187	Best	0,0555	0,0348	0,0851	0,0554	0,1119	0,0852	0,0827	0,0852
	Avg	0,0961	0,1010	0,1419	0,1417	0,1413	0,1326	0,1394	0,1466
	Std	0,0170	0,0179	0,0182	0,0233	0,0201	0,0185	0,0241	0,0202

Table 3: Comparison of FDB-BEHO versus other optimization algorithms in terms of fitness values.

Table 4: Comparison of FDB-BEHO versus other optimization algorithms in terms of average classification accuracy.

Dataset	FDB-BEHO-V	<b>FDB-BEHO-S</b>	ABC	SSA	PSO	GA	EO	ASO
CLL_SUB_111	0,5606	0,5891	0,5517	0,5294	0,5267	0,5303	0,5472	0,5544
colon	0,8023	0,8137	0,7745	0,7418	0,7778	0,7794	0,7418	0,7696
leukemia	0,895	0,909	0,888	0,8641	0,8613	0,8711	0,8711	0,8838
lung	0,9358	0,948	0,9529	0,948	0,948	0,9515	0,9554	0,9583
lung_discrete	0,7969	0,7661	0,8347	0,8039	0,8515	0,8347	0,8417	0,8389
lymphoma	0,8369	0,8710	0,8638	0,8503	0,8648	0,8555	0,8689	0,8596
nci9	0,4003	0,4134	0,4003	0,40458	0,4003	0,3905	0,4003	0,4003
Prostate_GE	0,849	0,8265	0,8412	0,8569	0,8667	0,8716	0,8275	0,8343
SMK_CAN_187	0,6571	0,6412	0,6402	0,6423	0,6439	0,6471	0,6767	0,6449

or machine learning methods to enhance its efficiency and effectiveness further.

Moreover, the impact of different parameter settings on BEHO's performance could be subjected to a more granular analysis to optimize its application across various domains. Integrating advanced machine learning techniques, such as deep learning, within the BEHO framework could provide a deeper understanding of the data structures and feature interactions, potentially leading to more innovative solutions and applications.

Additionally, parallel versions of BEHO could be developed to leverage modern computational architectures, significantly reducing the time required for large-scale computations and making the algorithm more practical for real-world applications that demand rapid processing speeds.

As the field of optimization continues to evolve, BEHO's flexibility and robustness, particularly in its binary incarnation with the FDB mechanism, position it as a potent tool capable of making significant contributions to various scientific and engineering disciplines. The insights gained from this study pave the way for more targeted and effective optimization strategies, facilitating advancements in both theoretical research and practical applications. ICAART 2025 - 17th International Conference on Agents and Artificial Intelligence

Table 5: Comparison of FDB-BEHO versus other optimization algorithms in terms of average selected number of features.

Dataset	FDB-BEHO-V	FDB-BEHO-S	ABC	SSA	PSO	GA	EO	ASO
CLL_SUB_111	2837,16	8502,69	5627,75	3042,80	5626,82	5638,17	2898,14	5645,71
colon	102,41	1008,31	943,96	446,08	944,82	943,82	269,14	962,33
leukemia	189,06	3473,45	3402,10	1184,12	3364,12	3391,89	450,22	3440,25
lung	130,45	1605,61	1561,96	626,45	1536,14	1558,65	366,61	1589,00
lung_discrete	13,02	153,67	138,33	62,55	134,08	137,07	45,53	142,86
lymphoma	96,43	92,48	1850,75	636,55	1820,10	1879,19	84,02	1908,35
nci9	2172,55	2167,76	4797,90	2561,59	4800,18	4799,96	1876,92	4806,20
Prostate_GE	387,94	2952,61	2890,92	1231,06	2878,24	2885,34	900,16	2919,59
SMK_CAN_187	5522,69	15338,35	9969,24	5502,22	9944,98	9964,37	5124,49	10021,29

Table 6: *p*-values of the Wilcoxson test of FDB-BEHO-V versus other optimization algorithms ( $p \ge 0.05$  are underlined).

Dataset	FDB-BEHO-S	ABC	SSA	PSO	GA	EO	ASO
CLL_SUB_111	1,83E-06	6,15E-10	2,80E-09	1,77E-09	8,27E-10	1,05E-09	5,14E-10
colon	5,14E-10	5,13E-10	5,14E-10	5,14E-10	5,13E-10	5,46E-10	5,14E-10
leukemia	5,14E-10	5,13E-10	5,14E-10	5,14E-10	5,14E-10	6,53E-10	5,14E-10
lung	5,14E-10	5,14E-10	5,14E-10	5,14E-10	5,13E-10	5,14E-10	5,13E-10
lung_discrete	5,04E-10	5,00E-10	5,07E-10	5,09E-10	4,98E-10	5,09E-10	5,08E-10
lymphoma	0,0608	5,14E-10	5,14E-10	5,13E-10	5,13E-10	4,17E-08	5,14E-10
nci9	0,0608	8,77E-10	6,92E-09	5,15E-10	5,15E-10	2,44E-08	5,15E-10
Prostate_GE	5,14E-10	5,14E-10	5,14E-10	5,14E-10	5,14E-10	5,79E-10	5,14E-10
SMK_CAN_187	6,08E-02	5,15E-10	2,23E-09	5,15E-10	1,05E-09	4,42E-09	6,93E-10

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