Short Paper: Industrial Feasibility of Private Information Retrieval

Angela Jäschke¹, Björn Grohmann², Frederik Armknecht¹ and Andreas Schaad²

¹University of Mannheim, Germany

²Huawei German Research Institute, Darmstadt, Germany

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Abstract: A popular security problem in database management is how to guarantee to a querying party that the database owner will not learn anything about the data that is retrieved — a problem known as Private Information Retrieval (PIR). While a variety of PIR schemes are known, they are rarely considered for practical use cases yet. We investigate the feasibility of PIR in the telecommunications world to open up data of carriers to external parties. To this end, we first provide a comparative survey of the current PIR state of the art (including ORAM schemes as a generalized concept) as well as implementation and analysis of two PIR schemes for the considered use case. While an overall conclusion is that PIR techniques are not too far away from practical use in specific cases, we see ORAM as a more suitable candidate for further R&D investment.

1 BACKGROUND AND MOTIVATION

The telecommunications world is undergoing a transition where carriers not only provide services such as telephony or internet access, but also attempt to monetize the huge amount of data associated with their subscribers' activity. Analyzing data like call statistics or roaming behavior can be used to offer specifically tailored services and packages. The combination of such data with other data from 3rd parties can potentially result in even more value. As such, one direction is to open up the existing databases to subscribing external parties. In fact, it may well be the case that two rivaling carriers allow each other to query their subscriber databases, e.g. for detecting fraudulent activities or faults in the network. Another real-world scenario is that of answering to the demands of public authorities wanting to verify that a user has been making a call at a certain time or to assess whether a certain IMEI or IMSI is part of the carriers subscriber base.

An open practical problem is how to guarantee to the querying party that the database owner will not learn anything about the data that is retrieved — a problem known as Private Information Retrieval (PIR) (Goldreich and Ostrovsky, 1996). Accordingly, we assessed the feasibility of PIR schemes to support such use cases, where the typical database consists of 400.000-800.000 entries of IMEIs and/or IMSIs. This paper provides a comparative survey of PIR schemes as part of Section 2. We then discuss two schemes in detail, i.e. a Trapdoor Group scheme in Section 3.1 and an ORAM approach in Section 3.2. We provide detailed performance and runtime analysis data in Section 4.

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2 OVERVIEW AND COMPARISON OF EXISTING SCHEMES

The trivial solution for a user who wants to query a database without the database server learning about the query is to retrieve the entire database from the server and ignore all except the queried entries. Of course, this is very inefficient in terms of communication, but very efficient regarding computational effort because there is (almost) none. Thus, the incurred effort provides a good starting point in that any new solution should have less communication than this trivial solution, often trading this for computational complexity in some form.

We split existing works that realize some form of private information retrieval into four main approaches. In a forthcoming paper, we present a detailed overview of the different schemes, here we only categorize the schemes into these high-level approaches. Some of the mentioned schemes have also

Jäschke, A., Grohmann, B., Armknecht, F. and Schaad, A.

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been presented in (Ostrovsky and Skeith(III), 2007) and (Olumofin and Goldberg, 2011), and some observations about computational complexity can be found in (Gasarch, 2004) and (Sion and Carbunar, 2007).

- Homomorphic Approaches: The user masks (e.g., homomorphically encrypts) the queried index, and the server algebraically combines all indices with the database entries to obtain a masked version of only the queried entry. The user then removes the mask to obtain the result. Publications following this general idea are (Kushilevitz and Ostrovsky, 1997), (Chang, 2004), (Melchor et al., 2016) (Group Homomorphic), (Trostle and Parrish, 2010) (Trapdoor Group), (Kiayias et al., 2015; Lipmaa, 2009; Ishai and Paskin, 2007) (Branching Programs), (Melchor and Gaborit, 2007) (Lattice-based) and (Doröz et al., 2014) (FHE-based).
- ORAM Approaches: Comes from the field of software protection, but can also be used to protect privacy in databases. ORAM requires a slightly different setup: The database must be encrypted and thus there must be some key management mechanism. In contrast to pure PIR, ORAM offers the added option of writing, i.e., changing or adding entries. Publications based on ORAM are (Mayberry et al., 2014; Stefanov et al., 2013; Ma et al., 2016) (ORAM-Tree), (Devadas et al., 16 A) (Onion-ORAM), (Apon et al., 2014) (FHE-ORAM) and (Lorch et al., 2013) (Parallel-Tree-ORAM).
- Garbled Approaches: Since PIR consists of two parties (the user and the server) trying to compute a function (the correct database entry) without the server learning the users input (the query index), it is natural to look to Multiparty-Computation, where two or more parties compute a function together without learning any input except their own, and the result of the computation. Publications involving this approach are (Lu and Ostrovsky, 2013; Gentry et al., 2014a; Gentry et al., 2014b).
- Other Approaches: The φ-Hiding Approach (Cachin et al., 1999), the Trapdoor Permutation Approach (Kushilevitz and Ostrovsky, 2000), and the Sender Anonymity Approach (Trostle and Parrish, 2010).

Table 1 compares the schemes from the above approaches, indicating a particularly good value with a (light) green background and particularly unfavorable aspects with a (darker) red background. The aspects considered are Comm_{\mathcal{U}} (communication from user to the server), Comm_{\mathcal{S}} (communication from server

to the user), $Comp_{\mathcal{U}}$ (user computation effort) and $Comp_{\mathcal{S}}$ (server computation effort). The variables used are:

- *n* is the number of database elements
- *B* is the block size
- λ is the security parameter
- *M* (resp. *C*) is the message (resp. ciphertext) space of the encryption scheme
- *m* is a finite group order

The leftmost column denotes the approach as presented above: H for homomorphic, O for ORAM, G for garbled and "-" if none apply.

3 CHOOSING AND OPTIMIZING

To test performance for the use cases described in Section 1, we implemented two approaches — one homomorphic and one ORAM-approach, as these differ greatly, yet can both solve our problem of PIR. Concretely, we chose and modified a Trapdoor Group Scheme based on (Trostle and Parrish, 2010) and the Path-ORAM Scheme (Stefanov et al., 2013) for their conceptual simplicity.

3.1 The (Optimized) Trapdoor Group Scheme

The original scheme (Trostle and Parrish, 2010) only allows retrieval of an entire row (i.e., \sqrt{n} out of *n*) of database entries, which we extend to allow single-entry-retrieval and minimize communication. We present this optimized scheme as a protocol:

Database Structure: *n* elements of \mathbb{Z}_N arranged as a $\ln(n)$ -dimensional array with entries $x_{i_1,...,i_{\ln(n)}}, i_j =$

 $1, ..., n^{1/\ln(n)}$ for $j = 1, ..., \ln(n)$.

Prerequisites: We assume that we work in the group $(\mathbb{Z}_m, +)$ and that *m* and *N* are coprime.

Queries: Suppose the user wants to query the element $x_{i_1^*,...,i_{l_{n(n)}}^*}$.

- The user selects *m* as the group order above depending on the required security level, but at least *m* > N^{|ln(n)|} ⋅ n ⋅ (N − 1).
- 2. The user randomly selects secret $b^j \in \mathbb{Z}_m^*, j = 1, \ldots, \ln(n)$ and $\ln(n) \cdot n^{1/\ln(n)}$ coefficients $e_{i,j}, i = 1, \ldots, n^{1/\ln(n)}, j = 1, \ldots, \ln(n)$ with three restrictions:

i.
$$e_{i,j} < \frac{\ln(n)}{\sqrt{\frac{m}{n \cdot (N-1)}}}$$
 for all (i, j) .

ii. For $j = 1, ..., \ln(n)$: If $i_j^* \neq i, e_{i,j}$ is a multiple of N (i.e., $e_i = a_i \cdot N$ for some a_i).

Idea	Scheme	Comm	Comm _S	Comp _U	Comp _S	Comments	Code
-	Trivial	1	$n \cdot B$	-	-	-	x
Н	(Chang, 2004), (Melchor et al., 2016), [Kushilevitz and Ostrovsky, 1997] (Group Homomorphic)	$\sqrt{n} \cdot \log(C)$	$\sqrt{n} \cdot \log(C)$	\sqrt{n} encryptions, 1 decryption	n scalar ciphertext multiplications, $\sqrt{n} \cdot \log(\sqrt{n})$ ciphertext additions	<i>C</i> is the ciphertext space, log(<i>C</i>) is the size of a ciphertext.	x
Н	[Trostle and Parrish, 2010] (Trapdoor Group)	$\sqrt{n} \cdot \log_2(m)$	$O(\sqrt{n} \cdot \log_2(m) + n)$	Generating m, \sqrt{n} modular exponentiations/ multiplications $+\sqrt{n}$ discrete logs	n integer exponentiations/ multiplications $+\sqrt{n} \cdot \log(\sqrt{n})$ integer multiplications/ additions	Group order <i>m</i> can be chosen by user such that discrete log is efficient (e.g., additive group). Several queries can be sent at once, so amortized cost lower.	Not pub lic
н	This paper (Optimized Trapdoor Group)	$\frac{\ln(n) \cdot n^{1/\ln(n)}}{\log_2(m)}$	$O((\log_2(m))^{\ln(n)} + \sqrt{n})$	Generating m, $\ln(n) \cdot n^{1/\ln(n)}$ modular exponentiations/ multiplications + $\ln(n)$ discrete logs	O(n) integer exponentiations/ multiplications +O(n) integer multiplications/ additions	Group order <i>m</i> can be chosen by user such that discrete log is efficient (e.g., additive group).	Not pub lic
Н	(Kiayias et al., 2015), (Lipmaa, 2009), [Ishai and Paskin, 2007] (Branching Programs)	$\log(n) \cdot \sqrt{n} \cdot \log(C)$	$\sqrt{n} \cdot \log(C)$	log(n) encryptions and decryptions	For <i>k</i> -ary branching program (optimal $k = 5$): <i>n</i> multiplications, $\frac{n}{k} \cdot \sqrt{k} \cdot \log(\sqrt{k})$ additions	C is the ciphertext space of the Damgård-Jurik cryptosystem.	x
Н	[Melchor and Gaborit, 2007] (Lattice-based)	$O(n \cdot N^2 \cdot m)$	$N \cdot m$	$O(n \cdot N^x)$ where x depends on the matrix multiplication algorithm used, mostly a bit less than 3.	$2n \cdot N^2$ multiplications and $2N \cdot \log(n \cdot N)$ additions.	Recommended as $N = 50$.	√ C++
Н	(Doröz et al., 2014) (FHE-based)	$\log(C)$	log(C)	One encryption, one decryption	Depends on the concrete FHE scheme used, likely very expensive.	This is one extreme where the server does all the work and the user almost none.	x
0	[Mayberry et al., 2014], (Stefanov et al., 2013), (Ma et al., 2016) (ORAM-Tree)	$O(\log(n)^3 + \log(n)^2 \cdot \log(C))$	$O(\log(n)^3 + \log(n)^2 \cdot \log(C))$	log(n) recryptions for each operation	-	Supports writing as well. Could be combined with FHE to reduce user communication and transfer computation to the server.	√ Java
0	(Devadas et al., 16 A) (Onion-ORAM)	$O(\log(n))$	O(B)	$\tilde{O}(B \cdot \log^4(n))$	$\tilde{\omega}(B \cdot \log^4(n))$	The block size <i>B</i> needs to be very large $(\tilde{\Omega}(\log^5(n)))$.	x
0	(Apon et al., 2014) (FHE-ORAM)	$log(C) \cdot op ,$ op = ORAM operation written as circuit	$\log(C)$	Convert operation into circuit, encrypt values, decrypt result.	Again depends on concrete FHE scheme, likely very expensive.	This seems worse than the trivial FHE approach above, but ORAM has a write-operation which pure PIR does not.	x
0	(Lorch et al., 2013) (Parallel-Tree-ORAM)	$\log(n)$	O(B)		log(n) recryptions for each operation, but parallelized.	Tree-ORAM outsourced to server using secure coprocessors (with which the user communicates in non-oblivious fashion).	Not pub lic
G	Trivial Garbled Circuit	4 (>> n)	<i>O</i> (<i>B</i>)	Transform function into Boolean circuit, generate 4 keys for each gate, compute 2 MACS for each gate.	Evaluate the Boolean circuit with the garbled keys.	This is worse than the trivial solution in every aspect except server communication.	
G	[Lu and Ostrovsky, 2013], (Gentry et al., 2014a), (Gentry et al., 2014b) (Garbled RAM)	O(RAM- execution time of query)	O(B)	Garble the query (O(RAM-execution time of query))	Evaluate garbled query (O(RAM-execution time of query))	The user also has to garble and upload the database once in the beginning.	x
-	(Cachin et al., 1999) (φ-Hiding)	$\log(n) + \lambda$	λ	Effort of computing φ-hiding <i>m</i> plus 2 modular exponentiations	Hamming-weight(<i>n</i>) modular exponentiations	λ is logarithmic in <i>n</i> , with recommended settings total communication is $O(log^8(n)).$	Pseu do code
-	[Kushilevitz and Ostrovsky, 2000] (Trapdoor Permutation)	O(B)	$n - \frac{n}{2B}$ $(< O(n)$ while $n > B^2)$	O(B)	$O(n \cdot B)$	User computation depends on the trapdoor functions and hardcore predicates used, assumed $O(n)$.	x
-	[Trostle and Parrish, 2010] (Sender Anonymity)	$(\lambda+1)\cdot\sqrt{n}$	$(\lambda + 1) \cdot \sqrt{n}$	$O(\log(\lambda)\cdot\sqrt{n})$	$O(Q \cdot (\lambda + 1) \cdot \sqrt{n}), Q$ is number of separate queries sent (> 1!)	Very likely insecure, as summing up all subqueries yields sum of separate query vectors.	Not pub lic

- iii. For $j = 1, ..., \ln(n)$: If $i_j^* = i, e_{i,j}$ has the form $1 + a_l \cdot N$ for some a_l .
- 3. The user sends the $b_i^j = b^j \cdot e_{i,j} \mod m$ to the database. This constitutes the query.

Database Action: For $j = 1, ..., \ln(n)$: The database computes $x_{i_{1+j},...,i_{\ln(n)}} := \sum_{k=1}^{n^{1/\ln(n)}} b_k^j \cdot x_{k,i_{1+j},...,i_{\ln(n)}}$ and sends $x := x_{i_{\ln(n)+1}}$ to the user. Operations in this step are done over the integers, as the database does not know the group order.

User Decoding: For $j = 1, ..., \ln(n)$, the user sets $x = x \cdot (b^j)^{-1} \mod m$ and transforms the result to *N*-ary encoding. Then the least significant digit is the requested database item $x_{i_1^*,...,i_{\ln(n)}^*}$. **Security:** In this new protocol, the size limit of the

Security: In this new protocol, the size limit of the e_i 's has changed from the original version. This requirement ensures getting the correct result without wrapping around mod *m* in the decoding phase. The security of the original scheme relies on the assumption that given the \sqrt{n} PIR request elements

 $(b_1,\ldots,b_{\sqrt{n}})$, where $b_i = b \cdot e_i \mod m$ and the e_i 's are chosen according to the constraints detailed above (with the a_i's in 2.ii. and 2.iii. selected uniformly at random), any computationally bounded adversary can output the correct m only with negligible probability. Indicators for the hardness of this assumption (called Hidden Modular Group Order Assumption), i.e., how much information about the group order is leaked by the queries, are presented in the original paper (Trostle and Parrish, 2010), along with a reduction from the PIR protocol to this assumption. For our improved scheme, it can easily be verified that $\sqrt{n} > \ln(n) \cdot n^{1/\ln(n)}$ for n > 213. As databases are generally much larger than 213 elements, we can base security on the security of the original scheme, since we will be sending less query elements and thus leaking at most as much data as the original scheme.

3.2 The Path-ORAM Scheme

The second solution we implemented is the Path-ORAM scheme from (Stefanov et al., 2013) with non-recursive position map storage. We describe the scheme with some parameters as we implemented them instead of the generic version:

Database Structure: The database is held in a binary tree of height $L = \lceil \log_2(n) \rceil$ with 2^L leaves. Each leaf (called a "bucket") holds up to 5 database entries (and is filled with dummy entries if it contains less). There are far more buckets than database elements. The bucket is encrypted by the user with AES in CBC mode, where each database entry consists of 1 or 2 AES-Blocks (128 bits each) depending on the chosen parameter setting (see Section 4). Thus, each bucket contains 5 or 10 AES Blocks plus the IV, so 6 or 11 blocks in total. Also, the user maintains a local stash S (which acts as a temporary storage space) and a lookup table (called "position map") mapping database blocks to the leaves of the binary tree. We assume that the database is already initialized, as setup is rather tedious and must only be done once before the first query is made, making it irrelevant for performance comparisons.

Queries: To retrieve an entry, the user looks up what tree leaf the data block is mapped to in the position map and reads the entire path from root to leaf into the local stash S (which may contain some elements from previous queries), as the entry will be in some bucket on this path (or in the stash). The entry is mapped to a new leaf randomly and the data is replaced in case of a write operation. Then, all elements in the stash are reencrypted and written to the server in a bottom-up manner: Each entry in the stash is placed in a bucket on the path to the (old) leaf as far away from the root as possible, guaranteeing that the maximum amount

of blocks can be placed into the tree. The bucket is filled up with dummy blocks and encrypted with AES in CBC-mode with a random IV. Sometimes, some elements from the stash can't be placed into the tree, these remain in the client stash and are placed into a bucket in a future query. If too many of these elements accumulate and the stash overflows, we say that the ORAM has failed. We chose a stash size of 220 blocks.

Security: We implemented the scheme without changing it, so the original security analysis holds.

4 PERFORMANCE

We now present the performance of our two chosen schemes. Times were measured on an Intel Core i5-4570 CPU with 3.20GHz and constitute average values, and the number of database entries was derived from our use case (400.000 - 800.000) with some smaller numbers for scale). The entries are random numbers of lengths 256 (resp. 128) bits to simulate the IMEIs and (or) IMSIs. The AES implementation in the ORAM scheme was wolfcrypt. Regarding memory¹ for our use case, the Trapdoor Group scheme requires a group order m of at least 3756 bits. This implies a server memory of about 25.6MB for the database, and about 1.317GB for storing intermediate results, so roughly 1.345GB in total. The memory requirement on the user side is only about 34kB. In the ORAM-scheme, user memory is about 2.1MB, whereas server memory strongly depends on the number of entries and got so large that we could not supply data for 800.000 entries because our allotted memory limit was exceeded.

For the more traditional PIR metrics, we split the performance into three main components: Communication (Figure 1a), user computational effort (1b) and server computational effort (1c) and plot the effort for different numbers of database entries. In each diagram, the dotted plots represent entries of length 256 bits, and the solid plots are entries of length 128 bits. The green plots always correspond to the ORAM scheme, and the red plots to the Trapdoor-Group scheme. In the communication figure, red is the amount of data sent from the user to the server in the Trapdoor-Group scheme, blue is the amount of data sent from the server to the user in the Trapdoor-Group scheme, and green is the amount of data sent from user to server or vice versa (as these values are equal) in the ORAM scheme. User computation encompasses decrypting, reading and encrypting

¹Theoretical results, not actually measured.

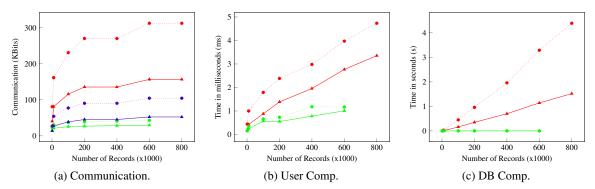


Figure 1: Performance of the two approaches: Red (top 2 lines) is Trapdoor-Group (user to server in communication), green (bottom 2 lines) is ORAM, blue (middle 2 lines) is server to user communication (Trapdoor-Group). Dotted is 256 bit, solid is 128 bit database entries.

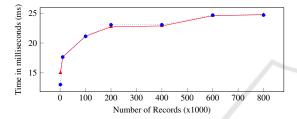


Figure 2: User setup without prime generation for 128 (red) and 256 (blue) bit inputs.

in the ORAM scheme, and the decoding step in the Trapdoor-Group scheme².

5 CONCLUSION AND FUTURE WORK

We see that ORAM performs better in all aspects, even though the Trapdoor-Group protocol actually performs worse in terms of user computation than Figure 1b implies (see Footnote 2). Thus, for the use case of this paper, ORAM is the better solution provided that the server has enough memory to store the tree. If, however, memory is the constraining factor rather than speed (which seems unlikely in today's world), the Trapdoor Group protocol would be the better choice both for user and for the server.

For future work, an interesting aspect could be the "levels" observed in Figure 1a for the Trapdoor Group scheme (i.e., the values for 200,000 and 400,000 entries seem similar, as do those for 600,000 and 800,000), which we suppose comes from the $\lceil \ln(n) \rceil$ exponent in the constraint for the size of the group order *m* (where *n* is the number of database entries).

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² There is a user setup phase which incurs computational effort but was not included in Figure 1b. The reason is that m was computed as a prime by calling nextprime () from the GMP-library in our code. This function's run-time varies enormously, dominating total time. This could be easily be circumvented in reality once the parameters of the database are set, e.g., by picking m randomly from a large list of primes, or choosing m as not prime and implementing constraints on the secret values instead. Either way, this additional cost really needs to be added to the time in Figure 1b. The time for user setup without this prime generation can be seen in Figure 2.

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